

# Contra Weakly $\pi$ Generalized Continuous Mapping in Intuitionistic Fuzzy Topological Space

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## ABSTRACT

In this paper the concepts of intuitionistic fuzzy contra weakly  $\pi$  generalized continuous mapping in fuzzy topological spaces is introduced with numerical examples. Some of their basic properties and characterizations are investigated.

## KEY WORDS

Intuitionistic Fuzzy (IF) topology, IF weakly  $\pi$  generalized closed set and open set, IF weakly  $\pi$  generalized continuous mappings and closed mapping, IF contra weakly  $\pi$  generalized continuous mapping.

## AMS CLASSIFICATION CODE (2000)

54A40, 54A99, 03F55.

## I. INTRODUCTION

In 1965, the concept of Fuzzy set (FS) theory and its applications are first proposed by Zadeh [19]. It provides a framework to encounter uncertainty, vagueness and partial truth. It is represented by introducing degree of membership for each member of the universe of discourse to a subset of it. In 1968, the concept of fuzzy topology has been introduced by Chang [2]. The concept of FS has generalized into intuitionistic fuzzy (IF) by Atanassov [1] in 1986. They are referred as a concept and its context. After that many research articles have been published in the study of examining and exploring, how far the basic concepts and theorems, defined in crisp sets and in fuzzy sets remain true in IF sets. In 1997, Coker [3] has initiated the concept of generalization of fuzzy topology into IF topology. In his research article, the apprehension of semi closed,  $\alpha$  closed, semi pre-closed, weakly closed are introduced. Further its properties are derived.

In this paper, the concept of contra weakly  $\pi$  generalized continuous mapping in IF topological space is introduced. Suitable examples are given and investigated some of its characteristics. Numerical illustrations are also presented to substantiate the derived results on the characteristics of the newly defined IF topological space.

This paper is organized into four sections. In the first section, the historical development of the concepts is briefed. The basic definitions and results, needed for this work are listed in the second section. Section three discusses the Contra weakly  $\pi$  generalized continuous mapping in intuitionistic fuzzy topological space and suitable examples are given. Section four contains the conclusion remarks.

## II. PRELIMINARIES

**Definition 2.1:** [1] Let  $X$  be a non-empty crisp set. An intuitionistic fuzzy (IF) set  $A$ , in  $X$  is defined as an object of the form

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle \mid x \in X \},$$

where the functions  $\mu_A(x) : X \rightarrow [0, 1]$  and  $\nu_A(x) : X \rightarrow [0, 1]$  denote respectively the degree of membership (briefly  $\mu_A$ ) and the degree of non-membership (briefly  $\nu_A$ ) of each element  $x \in X$  to the set  $A$ , for each  $x \in X$  and  $0 \leq \mu_A(x) + \nu_A(x) \leq 1$ .

The collection of all IF sub-sets in  $X$ , is denoted by IFS( $X$ ).

**Definition 2.2:** [1] Let  $A$  and  $B$  be two different IFSs defined by,

$$A = \{ \langle x, \mu_A(x), \nu_A(x) \rangle \mid x \in X \},$$

$$B = \{ \langle x, \mu_B(x), \nu_B(x) \rangle \mid x \in X \} \text{ or briefly,}$$

$A = \langle x, \mu_A, \nu_A \rangle$  and  $B = \langle x, \mu_B, \nu_B \rangle$  respectively.

The operations  $\wedge$  and  $\vee$  on  $A$  and  $B$  are defined with respect to  $\mu_A, \mu_B, \nu_A$ , and  $\nu_B$  as follows:



- i)  $\mu_A \vee \mu_B = \max \{ \mu_A, \mu_B \}$ ,
- ii)  $\mu_A \wedge \mu_B = \min \{ \mu_A, \mu_B \}$ ,
- iii)  $\nu_A \vee \nu_B = \max \{ \nu_A, \nu_B \}$ , and
- iv)  $\nu_A \wedge \nu_B = \min \{ \nu_A, \nu_B \}$ .

Then,

- i)  $A \subseteq B$ , if and only if,  $\mu_A \leq \mu_B$  and  $\nu_A \geq \nu_B$  for all  $x \in X$ , similarly  $A \supseteq B$  can be defined.
- ii)  $A = B$ , if and only if, both  $A \subseteq B$  and  $B \subseteq A$  are valid.
- iii)  $A^c = \{ \langle x, \mu'_A, \nu'_A \rangle \mid x \in X \}$ , where  $\mu'_A = \nu_A$  and  $\nu'_A = \mu_A$ .
- iv)  $A \cap B = \{ \langle x, \mu_A \wedge \mu_B, \nu_A \vee \nu_B \rangle \mid x \in X \}$ , and
- v)  $A \cup B = \{ \langle x, \mu_A \vee \mu_B, \nu_A \wedge \nu_B \rangle \mid x \in X \}$ .

The intuitionistic fuzzy sets  $0_\nu$  and  $1_\nu$  are defined respectively as,  $0_\nu = \{ \langle x, 0, 1 \rangle \mid x \in X \}$  and  $1_\nu = \{ \langle x, 1, 0 \rangle \mid x \in X \}$ . The sets  $0_\nu$  and  $1_\nu$  are known as the empty IF set and the whole IF set of  $X$  respectively.

**Definition 2.3:** [3] An intuitionistic fuzzy topology (IFT) is a family  $\tau$  of IFS defined on  $X$ , satisfying the following axioms:

- i)  $0_\nu, 1_\nu \in \tau$ ,
- ii)  $G_1 \cap G_2 \in \tau$ , whenever  $G_1, G_2 \in \tau$ ,
- iii)  $\cup \{ G_i \in \tau \mid i \in J \} \in \tau$ .

Then the pair  $(X, \tau)$  is called an intuitionistic fuzzy topological space (IFTS) and any IFS in  $\tau$  are known as an intuitionistic fuzzy open set (IFOS) in  $X$ .

If,  $A$  is an IFOS, in an IFTS  $(X, \tau)$ , then its complement  $A^c$  is called an intuitionistic fuzzy closed set (IFCS) in  $X$ .

**Definition 2.4:** [3] Let  $(X, \tau)$  be an IFTS and  $A = \langle x, \mu_A, \nu_A \rangle$  be an IFS in  $X$ . Then the intuitionistic fuzzy closure and an intuitionistic fuzzy interior are defined by ,

$$cl(A) = \cap \{ G \mid G \text{ is an IFCS in } X \text{ and } A \subseteq G \}, \text{ and}$$

$$int(A) = \cup \{ K \mid K \text{ is an IFOS in } X \text{ and } K \subseteq A \}.$$

Note that for any IFS,  $A$  in  $X$ ,  $cl(A^c) = (int(A))^c$  and  $int(A^c) = (cl(A))^c$ .

**Definition 2.5:** [3] An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS  $(X, \tau)$  is said to be an,

- i) intuitionistic fuzzy closed set (IFCS) in  $X \Leftrightarrow cl(A) = A$ , and
- ii) intuitionistic fuzzy open set (IFOS) in  $X \Leftrightarrow int(A) = A$ .

**Definition 2.6:** [15] A subset  $A$  of a space  $(X, \tau)$  is called,

- i) regular open, if,  $A = int(cl(A))$ , and
- ii)  $\pi$  open, if,  $A$  is the union of regular open sets, symbolically  $A$  is an IF $\pi$ OS in  $X$ .

**Definition 2.7:** [5] An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS  $(X, \tau)$  is said to be an,

- i) intuitionistic fuzzy semi-closed set (IFSCS) if  $int(cl(A)) \subseteq A$ , and
- ii) intuitionistic fuzzy semi-open set (IFSOS) if  $A \subseteq cl(int(A))$ .

**Definition 2.8:** [18] Let  $A$  be an IFS of an IFTS  $(X, \tau)$ . Then the semi-closure of  $A$  (simply  $scl(A)$ ) and semi-interior of  $A$  (simply  $sint(A)$ ) are defined as,

$$i) scl(A) = \cap \{ G \mid G \text{ is an IFSCS in } X \text{ and } A \subseteq G \},$$

$$ii) sint(A) = \cup \{ K \mid K \text{ is an IFSOS in } X \text{ and } K \subseteq A \}.$$

**Result 2.1:** [16] Let  $A$  be an IFS in  $(X, \tau)$ , then

- i)  $scl(A) = A \cup int(cl(A))$ , and
- ii)  $sint(A) = A \cap cl(int(A))$ .

**Definition 2.9:** [5] An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS  $(X, \tau)$  is said to be an,

- i) intuitionistic fuzzy  $\alpha$  closed set (IF $\alpha$ CS), if,  $cl(int(cl(A))) \subseteq A$ , and
- ii) intuitionistic fuzzy  $\alpha$  open set (IF $\alpha$ OS), if,  $A \subseteq int(cl(int(A)))$ .

**Definition 2.10:** [11] Let  $A = \langle x, \mu_A, \nu_A \rangle$  be an IFS of an IFTS  $(X, \tau)$ . Then, the  $\alpha$  closure of  $A$  ( $\alpha cl(A)$ ) and  $\alpha$  interior of  $A$  ( $\alpha int(A)$ ) are defined as,

$$\alpha cl(A) = \cap \{G \mid G \text{ is an IF}\alpha\text{CS in } X \text{ and } A \subseteq G\},$$

and

$$\alpha int(A) = \cup \{K \mid K \text{ is an IF}\alpha\text{OS in } X \text{ and } K \subseteq A\}.$$

**Result 2.2:** [12] Let  $A$  be an IFS in  $(X, \tau)$ , then,

- i)  $\alpha cl(A) = A \cup cl(int(cl(A)))$ , and
- ii)  $\alpha int(A) = A \cap int(cl(int(A)))$ .

**Definition 2.11:** An IFS,  $A = \langle x, \mu_A, \nu_A \rangle$  in an IFTS  $(X, \tau)$  is said to be an

- i) intuitionistic fuzzy pre-closed set [5] (IFPCS) if,  $cl(int(A)) \subseteq A$ ,
- ii) intuitionistic fuzzy regular closed set [5] (IFRCS) if,  $cl(int(A)) = A$ ,
- iii) intuitionistic fuzzy generalized closed set [17] (IFGCS) if,  $cl(A) \subseteq U$  whenever  $A \subseteq U$ ,  $U$  is an IFOS in  $X$ ,
- iv) intuitionistic fuzzy generalized semi closed set [14] (IFGSCS) if,  $scl(A) \subseteq U$  whenever  $A \subseteq U$ ,  $U$  is an IFOS in  $X$ ,
- v) intuitionistic fuzzy  $\alpha$  generalized closed set [12] (IF $\alpha$ GCS) if,  $\alpha cl(A) \subseteq U$  whenever  $A \subseteq U$ ,  $U$  is an IFOS in  $X$ .

**Definition 2.12:** [6] An IFS,  $A$  is said to be an intuitionistic fuzzy weakly  $\pi$  generalized closed set (IFW $\pi$ GCS) in  $(X, \tau)$  if,  $cl(int(A)) \subseteq U$  whenever  $A \subseteq U$  and  $U$  is an IF $\pi$ OS in  $X$ .

The family of all IFW $\pi$ GCS of an IFTS  $(X, \tau)$  is denoted by IFW $\pi$ GCS( $X$ ).

**Result 2.3:**[6] Every IFCS, IF $\alpha$ CS, IFGCS, IFRCS, IFPCS, IF $\alpha$ GCS are IFW $\pi$ GCS but the converse need not be true.

**Definition 2.13:** [6] An IFS,  $A$  is said to be an intuitionistic fuzzy weakly  $\pi$  generalized open set (IFW $\pi$ GOS) in  $(X, \tau)$  if, the complement  $A^c$  is an IFW $\pi$ GCS in  $X$ .

The family of all IFW $\pi$ GOS of an IFTS  $(X, \tau)$  is denoted by IFW $\pi$ GOS ( $X$ ).

**Definition 2.14:** [5] Let  $f$  be a mapping defined on an IFTS  $(X, \tau)$  into IFTS  $(Y, \sigma)$ . Then  $f$  is said intuitionistic fuzzy continuous (IF cts) if,  $f^{-1}(B) \in \text{IFOS}(X)$  for every  $B \in \sigma$ .

**Definition 2.15:**[7] A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy weakly  $\pi$  generalized continuous mapping (IFW $\pi$ G cts) if,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $(X, \tau)$  for every IFCS,  $B$  of  $(Y, \sigma)$ .

**Definition 2.16:** Let  $f$  be a mapping from an IFTS  $(X, \tau)$  into IFTS  $(Y, \sigma)$ . Then  $f$  is said to be

- i) intuitionistic fuzzy contra [4] continuous mapping if,  $f^{-1}(B) \in \text{IFCS}(X)$ , for every  $B \in \sigma$ ,
- ii) intuitionistic fuzzy contra  $\alpha$  continuous mapping [4] (If contra  $\alpha$  cts) if,  $f^{-1}(B) \in \text{IF}\alpha\text{C}(X)$ , for every  $B \in \sigma$ ,
- iii) intuitionistic fuzzy contra pre-continuous mapping [4] if,  $f^{-1}(B) \in \text{IFPC}(X)$ , for every  $B \in \sigma$ ,
- iv) intuitionistic fuzzy contra  $\alpha$  generalized continuous mapping [13] if,  $f^{-1}(B) \in \text{IF}\alpha\text{GC}(X)$ , for every  $B \in \sigma$ ,
- v) intuitionistic fuzzy contra semi-continuous mapping [4] if,  $f^{-1}(B) \in \text{IFSC}(X)$ , for every  $B \in \sigma$ ,

**Definition 2.17:** [8] Let  $(X, \tau)$  and  $(Y, \sigma)$  be two IFTS. A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy weakly  $\pi$  generalized closed mapping (IFW $\pi$ GCM) if,  $f(A)$  is an IFW $\pi$ GCS in  $Y$ , for every IFCS,  $A$  in  $X$ . In other words, every IFCS in  $X$  are mapped into IFW $\pi$ GCS in  $Y$ .

**Definition 2.18:** [9] Let  $(X, \tau)$  and  $(Y, \sigma)$  be two IFTS. A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy completely weakly  $\pi$  generalized continuous mapping (IF completely W $\pi$ G cts) if,  $f^{-1}(B)$  is an IFRCS in  $(X, \tau)$  for every IFW $\pi$ GCS,  $B$  of  $(Y, \sigma)$ .

**Definition 2.19:** [10] Let  $(X, \tau)$  and  $(Y, \sigma)$  be two IFTS. A bijection mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy weakly  $\pi$  generalized (IFW $\pi$ G) homeomorphism if, both the functions,  $f$  and  $f^{-1}$  are IFW $\pi$ G continuous mappings.

**Definition 2.20:** [6] An IFTS  $(X, \tau)$  is called an intuitionistic fuzzy  ${}_{w\pi g}T_{1/2}$  (IF  ${}_{w\pi}T_{1/2}$ ) space if, every IFW $\pi$ GCS in  $X$  is an IFCS in  $X$ .

**Definition 2.21:** [6] An IFTS  $(X, \tau)$  is called an intuitionistic fuzzy  ${}_{w\pi g}T_q$  (IF  ${}_{w\pi g}T_q$ ) space,  $(0 < q < 1)$  if, every IFW $\pi$ GCS in  $X$  is an IFPCS in  $X$ .

### III. Intuitionistic Fuzzy Contra Weakly $\pi$ Generalized Continuous Mapping

The main objective of this section is to study the Intuitionistic Fuzzy contra weakly  $\pi$  generalized continuous mapping on a topological spaces, in this connection some of its properties are obtained.

**Definition 3.1:** A mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  is called an intuitionistic fuzzy contra weakly  $\pi$  generalized continuous mapping (IFcontraW $\pi$ G cts) if,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $(X, \tau)$  for every IFOS,  $B$  of  $(Y, \sigma)$ .

**Example 3.1:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.3, 0.2), (0.6, 0.7) \rangle$ ,  $G_2 = \langle y, (0.5, 0.6), (0.4, 0.3) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is an IFcontraW $\pi$ G continuous mapping.

**Proposition 3.1:** Every IF contra continuous mapping is an IFcontraW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF contra continuous mapping. Let  $B$  be an IFOS in  $Y$ . Since  $f$  is IF contra continuous mapping,  $f^{-1}(B)$  is an IFCS in  $X$ . Since every IFCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $X$ . Therefore  $f$  is an IFcontraW $\pi$ G continuous mapping.

**Example 3.2:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.2, 0.4), (0.8, 0.6) \rangle$ ,  $G_2 = \langle y, (0.2, 0.1), (0.8, 0.7) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . The IFS,  $B = \langle y, (0.2, 0.1), (0.8, 0.7) \rangle$  is IFCS in  $Y$ . Then  $f^{-1}(B)$  is IFW $\pi$ GCS in  $X$ , but not IFOS in  $X$ . Therefore  $f$  is an IFcontraW $\pi$ G continuous mapping but not an IF contra continuous mapping.

**Proposition 3.2:** Every IF contra  $\alpha$  continuous mapping is an IFcontraW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF contra  $\alpha$  continuous mapping. Let  $B$  be an IFOS in  $Y$ . Then by definition  $f^{-1}(B)$  is an IF $\alpha$ CS in  $X$ . Since every IF $\alpha$ CS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $X$ . Thus  $f$  is an IFcontraW $\pi$ G continuous mapping.

**Example 3.3:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.5, 0.4), (0.5, 0.6) \rangle$ ,  $G_2 = \langle y, (0.3, 0.2), (0.6, 0.8) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . The IFS,  $B = \langle y, (0.3, 0.2), (0.6, 0.8) \rangle$  is IFOS in  $Y$ . Then  $f^{-1}(B)$  is IFW $\pi$ GCS in  $X$ , but not IF $\alpha$ CS in  $X$ . Then  $f$  is an IFcontraW $\pi$ G continuous mapping but not an IF $\alpha$  continuous mapping.

**Proposition 3.3:** Every IF pre-continuous mapping is an IFcontraW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF pre-continuous mapping. Let  $B$  be an IFOS in  $Y$ . Then  $f^{-1}(B)$  is an IFPCS in  $X$ . Since every IFPCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $X$ . Therefore  $f$  is an IFcontraW $\pi$ G continuous mapping.

**Example 3.4:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.4, 0.3), (0.6, 0.7) \rangle$ ,  $G_2 = \langle y, (0.6, 0.4), (0.4, 0.4) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . The IFS,  $B = \langle y, (0.4, 0.4), (0.6, 0.4) \rangle$  is IFOS in  $Y$ . Then  $f^{-1}(B)$  is IFW $\pi$ GCS in  $X$ , but not IFPCS in  $X$ . Therefore  $f$  is IFcontraW $\pi$ G continuous mapping but not an IF pre-continuous mapping.

**Proposition 3.4:** Every IF contra  $\alpha$  generalized continuous mapping is an IFW $\pi$ G continuous mapping but not conversely.

**Proof:** Let  $f: (X, \tau) \rightarrow (Y, \sigma)$  be an IF contra  $\alpha$  generalized continuous mapping. Let  $B$  be an IFOS in  $Y$ . Then by definition,  $f^{-1}(B)$  is an IF $\alpha$ GCS in  $X$ . Since every IF $\alpha$ GCS is an IFW $\pi$ GCS,  $f^{-1}(B)$  is an IFW $\pi$ GCS in  $X$ . So,  $f$  is an IFcontraW $\pi$ G continuous mapping.

**Example 3.5:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.4, 0.6), (0.2, 0.2) \rangle$ ,  $G_2 = \langle y, (0.3, 0.2), (0.4, 0.3) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . The IFS,  $B = \langle y, (0.3, 0.2), (0.4, 0.3) \rangle$  is IFOS in  $Y$ . Then  $f^{-1}(B)$  is IFW $\pi$ GCS in  $X$ , but not IF $\alpha$ GCS in  $X$ . Therefore  $f$  is IFcontraW $\pi$ G continuous mapping but not an IF contra  $\alpha$  generalized continuous mapping.

**Remark 3.1:** IF contra semi-continuous mapping and IFcontraW $\pi$ G continuous mapping are independent to each other.

**Example 3.6:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.3, 0.4), (0.7, 0.6) \rangle$ ,  $G_2 = \langle y, (0.3, 0.4), (0.7, 0.6) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is IF contra semi-continuous mapping but not an IFcontraW $\pi$ G continuous mapping, since  $B = \langle y, (0.3, 0.4), (0.7, 0.6) \rangle$  is an IFSOS in  $Y$ , but  $f^{-1}(B) = \langle x, (0.3, 0.4), (0.7, 0.6) \rangle$  is not an IFW $\pi$ GCS in  $X$ .

**Example 3.7:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.9, 0.7), (0.1, 0.2) \rangle$ ,  $G_2 = \langle y, (0.3, 0.4), (0.7, 0.6) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is IFcontraW $\pi$ G continuous mapping, but not an IF contra semi-continuous mapping, since  $B = \langle y, (0.7, 0.6), (0.3, 0.4) \rangle$  is an IFW $\pi$ GCS in  $Y$ , but  $f^{-1}(B) = \langle x, (0.7, 0.6), (0.3, 0.4) \rangle$  is not an IFSCS in  $X$ .

**Remark 3.2:** IF contra generalized semi-continuous mapping and IFcontraW $\pi$ G continuous mapping are independent to each other.

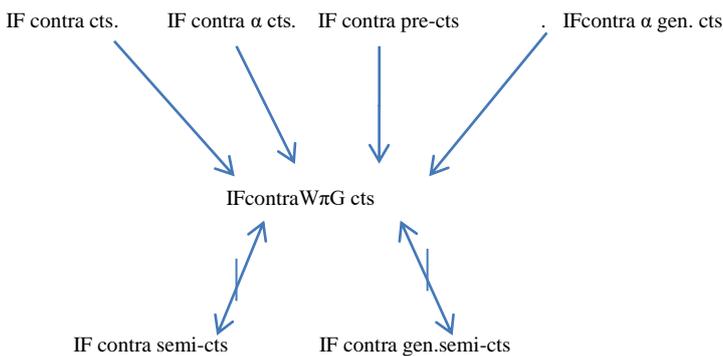
**Example 3.8:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.2, 0.3), (0.5, 0.5) \rangle$ ,  $G_2 = \langle y, (0.5, 0.5), (0.2, 0.3) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is IF contra generalized semi-continuous mapping, but not an IFcontraW $\pi$ G continuous mapping, since  $B = \langle y, (0.2, 0.3), (0.5, 0.5) \rangle$  is an IFGSCS in  $Y$ , but  $f^{-1}(B) = \langle x, (0.2, 0.3), (0.5, 0.5) \rangle$  is not an IFW $\pi$ GCS in  $X$ .

**Example 3.9:** Let  $X = \{a, b\}$ ,  $Y = \{u, v\}$  and  $G_1 = \langle x, (0.5, 0.6), (0.2, 0.2) \rangle$ ,  $G_2 = \langle y, (0.6, 0.6), (0.3, 0.2) \rangle$ .

Then  $\tau = \{0_\sim, G_1, 1_\sim\}$  and  $\sigma = \{0_\sim, G_2, 1_\sim\}$  are IFTs on  $X$  and  $Y$  respectively. Define a mapping  $f: (X, \tau) \rightarrow (Y, \sigma)$  by  $f(a) = u$  and  $f(b) = v$ . Then  $f$  is IFcontraW $\pi$ G continuous mapping, but not an IF contra generalized semi-continuous mapping, since  $B = \langle y, (0.3, 0.2), (0.6, 0.6) \rangle$  is an IFW $\pi$ GCS in  $Y$  but  $f^{-1}(B) = \langle x, (0.3, 0.2), (0.6, 0.6) \rangle$  is not an IFGSCS in  $X$ .

**Remark 3.3:**The derived relationship among the terms can be schematically presented as follows.



**Fig.3.1 Relationships between the contra weakly  $\pi$  generalized continuous mapping, and the other existing contra continuous mapping on intuitionistic fuzzy sets.**

#### IV. CONCLUSION

In this paper, a special type of continuous mapping, namely contra weakly  $\pi$  generalized continuous mapping in Intuitionistic Fuzzy Topological Spaces is introduced. Some of the basic properties of contra weakly  $\pi$  generalized continuous mapping in intuitionistic fuzzy topological spaces are derived. Also the relationship among the intuitionistic fuzzy contra weakly  $\pi$  generalized continuous mapping and other existing intuitionistic fuzzy contra continuous mapping are studied. By means of suitable numerical examples, it is established that the converse of the propositions describing the properties, need not be true.

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