# Eulerian integral associated with product of two Prasad's multivariable I-functions, a generalized Lauricella function and a class of polynomials

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#### ABSTRACT

The present paper is evaluated a new Eulerian integral associated with the product of two multivariable I-functions defined by Prasad [1] a generalized Lauricella function and a class of multivariable polynomials with general arguments. Several particular cases are given.

Keywords: Eulerian integral, multivariable I-function, generalized Lauricella function of several variables, multivariable H-function, generalized hypergeometric function, class of polynomials

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#### 1. Introduction

In this paper, we evaluate a new Eulerian integral of most general characters associated with the products of two multivariable I-functions defined by Prasad [1] and a class of polynomials with general arguments but of greater order. Several particular cases are given.

The multivariable I-function of r-variables is defined in term of multiple Mellin-Barnes type integral:

$$I(z_{1}, \dots, z_{r}) = I_{p_{2}, q_{2}, p_{3}, q_{3}; \dots; p_{r}, q_{r}; p^{(1)}, q^{(1)}; \dots; p^{(r)}, q^{(r)}}^{(1)} = \begin{pmatrix} z_{1} & (a_{2j}; \alpha'_{2j}, \alpha''_{2j})_{1, p_{2}}; \dots; \\ \vdots & \vdots & \vdots \\ z_{r} & (b_{2j}; \beta'_{2j}, \beta''_{2j})_{1, q_{2}}; \dots; \end{pmatrix}$$

$$(\mathbf{a}_{rj}; \alpha_{rj}^{(1)}, \cdots, \alpha_{rj}^{(r)})_{1,p_r} : (a_j^{(1)}, \alpha_j^{(1)})_{1,p^{(1)}}; \cdots ; (a_j^{(r)}, \alpha_j^{(r)})_{1,p^{(r)}})$$

$$(\mathbf{b}_{rj}; \beta_{rj}^{(1)}, \cdots, \beta_{rj}^{(r)})_{1,q_r} : (b_j^{(1)}, \beta_j^{(1)})_{1,q^{(1)}}; \cdots ; (b_j^{(r)}, \beta_j^{(r)})_{1,q^{(r)}})$$

$$(1.1)$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_1} \cdots \int_{L_r} \phi(s_1, \cdots, s_r) \prod_{i=1}^r \theta_i(s_i) z_i^{s_i} \mathrm{d}s_1 \cdots \mathrm{d}s_r \tag{1.2}$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [1]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as:

$$|argz_i|<rac{1}{2}\Omega_i\pi$$
 , where

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$$\Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left(\sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)}\right) + \dots + \frac{1}{n^{(i)}} \alpha_{2k}^{(i)} + \frac{1}{$$

$$\left(\sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)}\right) - \left(\sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \dots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)}\right)$$
(1.3)

where  $i = 1, \dots, r$ 

The complex numbers  $z_i$  are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the the asymptotic expansion in the following convenient form:

$$I(z_1, \dots, z_r) = 0(|z_1|^{\alpha_1}, \dots, |z_r|^{\alpha_r}), max(|z_1|, \dots, |z_r|) \to 0$$

$$I(z_1, \dots, z_r) = 0(|z_1|^{\beta_1}, \dots, |z_r|^{\beta_r}), min(|z_1|, \dots, |z_r|) \to \infty$$

where 
$$k=1,\cdots,r: \alpha_k'=min[Re(b_j^{(k)}/\beta_j^{(k)})], j=1,\cdots,m_k$$
 and

$$\beta'_{k} = max[Re((a_{j}^{(k)} - 1)/\alpha_{j}^{(k)})], j = 1, \cdots, n_{k}$$

Condider a second multivariable I-function defined by Panda [1]

$$I(z'_{1}, \cdots, z'_{s}) = I_{p'_{2}, q'_{2}, p'_{3}, q'_{3}; \cdots; p'_{s}, q'_{s}; p'(1), q'(1); \cdots; p'(s), q'(s)}^{0, n'_{1}; \dots; m'(s), n'(s)} \begin{pmatrix} z'_{1} \\ \vdots \\ \vdots \\ \vdots \\ z'_{s} \end{pmatrix} (a'_{2j}; \alpha'_{2j}^{(1)}, \alpha'_{2j}^{(2)})_{1, p'_{2}}; \cdots; (a'_{2j}; \alpha'_{2j}^{(1)}, \alpha'_{2j}^{(2)})_{1, p'_{2}}; \cdots; (a'_{2j}; \alpha'_{2j}^{(1)}, \alpha'_{2j}^{(2)})_{1, q'_{2}}; \cdots; (b'_{2j}; \beta'_{2j}^{(1)}, \beta'_{2j}^{(2)})_{1, q'_{2}}; \cdots; (b'_{2j}; \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)})_{1, q'_{2}}; \cdots; (b'_{2j}; \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)}, \beta'_{2j}^{(2)}; \cdots; (b'_{2j}; \beta'_{2j}^{(2)}, \beta'_{2j}^{(2$$

$$(a'_{sj}; \alpha'^{(1)}_{sj}, \cdots, \alpha'_{sj}{}^{(s)})_{1,p'_{s}} : (a'^{(1)}_{j}, \alpha'^{(1)}_{j})_{1,p'^{(1)}}; \cdots; (a'_{j}{}^{(s)}, \alpha'^{(s)}_{j})_{1,p'^{(s)}}$$

$$(b'_{sj}; \beta'^{(1)}_{sj}, \cdots, \beta'_{sj}{}^{(s)})_{1,q'_{s}} : (b'^{(1)}_{j}, \beta'^{(1)}_{j})_{1,q'^{(1)}}; \cdots; (b'_{j}{}^{(s)}, \beta'^{(s)}_{j})_{1,q'^{(s)}}$$

$$(1.4)$$

$$= \frac{1}{(2\pi\omega)^s} \int_{L_1'} \cdots \int_{L_s'} \psi(t_1, \cdots, t_s) \prod_{i=1}^s \xi_i(t_i) z_i^{t_i} dt_1 \cdots dt_s$$

$$(1.5)$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [1]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as:

where  $|argz_i'|<rac{1}{2}\Omega_i'\pi$  ,

$$\Omega_{i}^{\prime} = \sum_{k=1}^{n^{\prime(i)}} \alpha_{k}^{\prime(i)} - \sum_{k=n^{\prime(i)}+1}^{p^{\prime(i)}} \alpha_{k}^{\prime(i)} + \sum_{k=1}^{m^{\prime(i)}} \beta_{k}^{\prime(i)} - \sum_{k=m^{(i)}+1}^{q^{\prime(i)}} \beta_{k}^{\prime(i)} + \left(\sum_{k=1}^{n_{2}^{\prime}} \alpha_{2k}^{\prime(i)} - \sum_{k=n_{2}+1}^{p_{2}^{\prime}} \alpha_{2k}^{\prime(i)}\right)$$

$$+\dots + \left(\sum_{k=1}^{n'_s} \alpha'_{sk}{}^{(i)} - \sum_{k=n'_s+1}^{p'_s} \alpha'_{sk}{}^{(i)}\right) - \left(\sum_{k=1}^{q'_2} \beta'_{2k}{}^{(i)} + \sum_{k=1}^{q'_3} \beta'_{3k}{}^{(i)} + \dots + \sum_{k=1}^{q'_s} \beta'_{sk}{}^{(i)}\right)$$
(1.6)

where  $i = 1, \dots, s$ 

The complex numbers  $z_i$  are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the the asymptotic expansion in the following convenient form:

$$I(z'_{1}, \dots, z'_{s}) = 0(|z'_{1}|^{\alpha'_{1}}, \dots, |z'_{s}|^{\alpha'_{s}}), max(|z'_{1}|, \dots, |z'_{s}|) \to 0$$
$$I(z'_{1}, \dots, z'_{s}) = 0(|z'_{1}|^{\beta'_{1}}, \dots, |z'_{s}|^{\beta'_{s}}), min(|z'_{1}|, \dots, |z'_{s}|) \to \infty$$

where 
$$k=1,\cdots,z$$
:  $\alpha_k''=min[Re(b_j'^{(k)}/\beta_j'^{(k)})], j=1,\cdots,m_k'$  and 
$$\beta_k''=max[Re((a_j'^{(k)}-1)/\alpha_j'^{(k)})], j=1,\cdots,n_k'$$

Srivastava and Garg [4] introduced and defined a general class of multivariable polynomials as follows

$$S_L^{h_1,\dots,h_u}[z_1,\dots,z_u] = \sum_{R_1,\dots,R_u=0}^{h_1R_1+\dots h_vR_u \leqslant L} (-L)_{h_1R_1+\dots+h_uR_u} B(E;R_1,\dots,R_u) \frac{z_1^{R_1}\dots z_u^{R_u}}{R_1!\dots R_u!}$$
(1.7)

#### 2. Integral representation of generalized Lauricella function of several variables

The following generalized hypergeometric function in terms of multiple contour integrals is also required [5, page 39] eq .30]

$$\frac{\prod_{j=1}^{P} \Gamma(A_j)}{\prod_{j=1}^{Q} \Gamma(B_j)} {}_{P}F_{Q} \left[ (A_P); (B_Q); -(x_1 + \dots + x_r) \right]$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_i''} \cdots \int_{L_i''} \frac{\prod_{j=1}^P \Gamma(A_j + s_1 + \dots + s_r)}{\prod_{j=1}^Q \Gamma(B_j + s_1 + \dots + s_r)} \Gamma(-s_1) \cdots \Gamma(-s_r) x_1^{s_1} \cdots x_r^{s_r} ds_1 \cdots ds_r$$
(2.1)

where the contours are of Barnes type with indentations, if necessary, to ensure that the poles of  $\Gamma(A_i + s_1 + \cdots + s_r)$ are separated from those of  $\Gamma(-s_i)$ ,  $i=1,\cdots,r$ . The above result (1.23) can be easily established by an appeal to the calculus of residues by calculating the residues at the poles of  $\Gamma(-s_j)$ ,  $j=1,\cdots,r$ In order to evaluate a number of integrals of multivariable I-function, we first establish the formula

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$$\int_{a}^{b} (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^{l} \left[ 1 - \tau_{j} (t-a)^{h_{i}} \right]^{-\lambda_{j}} \prod_{j=1}^{k} (f_{j}t + g_{j})^{\sigma_{j}} dt = (b-a)^{\alpha+\beta-1} B(\alpha,\beta) \prod_{j=1}^{k} (af_{j} + g_{j})^{\sigma_{j}} dt$$

$$F_{1:0,\cdots,0;0,\cdots,0}^{1:1,\cdots,1;1\cdots,1} \begin{pmatrix} (\alpha:h_1,\cdots,h_l,1,\cdots,1):(\lambda_1:1),\cdots,(\lambda_l:1);(-\sigma_1:1),\cdots,(-\sigma_k:1)\\ & \ddots & \\ (\alpha+\beta:h_1,\cdots,h_l,1,\cdots,1):-,\cdots,-;-,\cdots,- \end{pmatrix}$$

$$; \tau_1(b-a)^{h_1}, \cdots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1 + g_1}, \cdots, -\frac{(b-a)f_k}{af_k + g_k}$$
 (2.2)

where  $a, b \in \mathbb{R}(a < b), \alpha, \beta, f_i, g_i, \sigma_i, \tau_j, h_j \in \mathbb{C}, \lambda_j \in \mathbb{R}^+ (i = 1, \dots, k; j = 1, \dots, l)$ 

$$\min(\operatorname{Re}(\alpha),\operatorname{Re}(\beta)) > 0, \max_{1 \leqslant j \leqslant l} \left\{ \left| \tau_j(b-a)^{h_j} \right| \right\} < 1, \max_{1 \leqslant j \leqslant k} \left\{ \left| \frac{(b-a)f_i}{af_i + g_i} \right| \right\} < 1,$$

and  $F_{1:0,\cdots,0;0,\cdots,0}^{1:1,\cdots,1;1\cdots,1}$  is a particular case of the generalized Lauricella function introduced by Srivastava-Daoust[3,page 454] given by :

$$F_{1:0,\cdots,0;0,\cdots,0}^{1:1,\cdots,1;1\cdots,1} \begin{pmatrix} (\alpha:h_1,\cdots,h_l,1,\cdots,1):(\lambda_1:1),\cdots,(\lambda_l:1);(-\sigma_1:1),\cdots,(-\sigma_k:1)\\ & \ddots \\ & (\alpha+\beta:h_1,\cdots,h_l,1,\cdots,1):-,\cdots,-;-,\cdots,- \end{pmatrix}$$

$$; \tau_1(b-a)^{h_1}, \cdots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1+g_1}, \cdots, -\frac{(b-a)f_k}{af_k+g_k} \right) = \frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha) \prod_{j=1}^{l} \Gamma(\lambda_j) \prod_{j=1}^{k} \Gamma(-\sigma_j)}$$

$$\frac{1}{(2\pi\omega)^{l+k}} \int_{L_1} \cdots \int_{L_{l+k}} \frac{\Gamma\left(\alpha + \sum_{j=1}^{l} h_j s_j + \sum_{j=1}^{k} s_{l+j}\right)}{\Gamma\left(\alpha + \beta + \sum_{j=1}^{l} h_j s_j + \sum_{j=1}^{k} s_{l+j}\right)} \prod_{j=1}^{l} \Gamma(\lambda_j + s_j) \prod_{j=1}^{k} \Gamma(-\sigma_j + s_{l+j})$$

$$\prod_{j=1}^{l+k} \Gamma(-s_j) z_1^{s_1} \cdots z_l^{s_l} z_{l+1}^{s_{l+1}} \cdots, z_{l+k}^{s_{l+k}} \, \mathrm{d} s_1 \cdots \mathrm{d} s_{l+k}$$
(2.3)

Here the contour  $L_j's$  are defined by  $L_j=L_{w\zeta_j\infty}(Re(\zeta_j)=v_j'')$  starting at the point  $v_j''-\omega\infty$  and terminating at the point  $v_j''+\omega\infty$  with  $v_j''\in\mathbb{R}(j=1,\cdots,l)$  and each of the remaining contour  $L_{l+1},\cdots,L_{l+k}$  run from  $-\omega\infty$  to  $\omega\infty$ 

(2.2) can be easily established by expanding 
$$\prod_{j=1}^{l} \left[1 - \tau_j (t-a)^{h_i}\right]^{-\lambda_j}$$
 by means of the formula : 
$$(1-z)^{-\alpha} = \sum_{r=0}^{\infty} \frac{(\alpha)_r}{r!} z^r (|z| < 1)$$
 (2.4)

integrating term by term with the help of the integral given by Saigo and Saxena [2, page 93, eq.(3.2)] and applying the definition of the generalized Lauricella function [5, page 454].

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### 3. Eulerian integral

In this section, we note:

$$\theta_i = \prod_{j=1}^l \left[ 1 - \tau_j (t-a)^{h_i} \right]^{-\zeta_j^{(i)}}, \zeta_j^{(i)} > 0 \\ (i = 1, \dots, r); \theta_i' = \prod_{j=1}^l \left[ 1 - \tau_j (t-a)^{h_i} \right]^{-\zeta_j'^{(i)}}, \zeta_j'^{(i)} > 0 \\ (i = 1, \dots, s)$$

$$\theta_i'' = \prod_{j=1}^l \left[ 1 - \tau_j (t - a)^{h_i} \right]^{-\zeta_j''(i)}, \zeta_j''(i) > 0 (i = 1, \dots, u)$$
(3.1)

$$U = p_2, q_2; p_3, q_3; \cdots; p_{r-1}, q_{r-1}; p_2', q_2'; p_3', q_3'; \cdots; p_{s-1}', q_{s-1}'; 0, 0; \cdots; 0, 0; 0, 0; \cdots; 0, 0$$
(3.2)

$$V = 0, n_2; 0, n_3; \dots; 0, n_{r-1}; 0, n'_2; 0, n'_3; \dots; 0, n'_{s-1}; 0, 0; \dots; 0, 0; 0, 0; \dots; 0, 0$$
(3.3)

$$X = m^{(1)}, n^{(1)}; \dots; m^{(r)}, n^{(r)}; m'^{(1)}, n'^{(1)}; \dots; m'^{(s)}, n'^{(s)}; 1, 0; \dots; 1, 0; 1, 0; \dots; 1, 0$$
(3.4)

$$Y = p^{(1)}, q^{(1)}; \dots; p^{(r)}, q^{(r)}; p'^{(1)}, q'^{(1)}; \dots; p'^{(s)}, q'^{(s)}; 0, 1; \dots; 0, 1; 0, 1; \dots; 0, 1$$
(3.5)

$$A = (a_{2k}; \alpha_{2k}^{(1)}, \alpha_{2k}^{(2)}); \cdots; (a_{(r-1)k}; \alpha_{(r-1)k}^{(1)}, \alpha_{(r-1)k}^{(2)}, \cdots, \alpha_{(r-1)k}^{(r-1)}); (a'_{2k}; \alpha'_{2k}^{(1)}, \alpha'_{2k}^{(2)}); \cdots;$$

$$(a'_{(s-1)k}; \alpha'^{(1)}_{(s-1)k}, \alpha'^{(2)}_{(s-1)k}, \cdots, \alpha'^{(s-1)}_{(s-1)k})$$
(3.6)

$$; (b'_{2k}; \beta'^{(1)}_{2k}, \beta'^{(2)}_{2k}); \cdots; B = (b_{2k}; \beta^{(1)}_{2k}, \beta^{(2)}_{2k}); \cdots; (b_{(r-1)k}; \beta^{(1)}_{(r-1)k}, \beta^{(2)}_{(r-1)k}, \cdots; \beta^{(r-1)}_{(r-1)k})$$

$$(b'_{(s-1)k}; \beta'^{(1)}_{(s-1)k}, \beta'^{(2)}_{(s-1)k}, \cdots, \beta'^{(s-1)k}_{(s-1)k})$$
 (3.7)

$$\mathfrak{A} = (a_{rk}; \alpha_{rk}^{(1)}, \alpha_{rk}^{(2)}, \cdots, \alpha_{rk}^{(r)}, 0, \cdots, 0, 0, \cdots, 0)$$
(3.8)

$$\mathfrak{A}' = (a'_{sk}; 0, \cdots, 0, \alpha'^{(1)}_{sk}, \alpha'^{(2)}_{sk}, \cdots, \alpha'^{(s)}_{sk}, 0, \cdots, 0, 0, \cdots, 0)$$
(3.9)

$$\mathfrak{B} = (b_{rk}; \beta_{rk}^{(1)}, \beta_{rk}^{(2)}, \cdots, \beta_{rk}^{(r)}, 0, \cdots, 0, 0, \cdots, 0, 0, \cdots, 0)$$
(3.10)

$$\mathfrak{B}' = (b'_{sk}; 0, \cdots, 0, \beta'^{(1)}_{sk}, \beta'^{(2)}_{sk}, \cdots, \beta'^{(s)}_{sk}, 0, \cdots, 0, 0, \cdots, 0)$$
(3.11)

$$\mathfrak{A}_{\mathbf{1}} = (a_k^{(1)}, \alpha_k^{(1)})_{1,p^{(1)}}; \cdots; (a_k^{(r)}, \alpha_k^{(r)})_{1,p^{(r)}}; (a_k'^{(1)}, \alpha_k^{(1)})_{1,p^{(1)}}; \cdots; (a_k'^{(s)}, \alpha_k'^{(s)})_{1,p'^{(s)}};$$

$$(1,0); \cdots; (1,0); (1.0); \cdots; (1.0)$$
 (3.12)

$$\mathfrak{B}_{1} = (b_{k}^{(1)},\beta_{k}^{(1)})_{1,q^{(1)}}; \cdots; (b_{k}^{(r)},\beta_{k}^{(r)})_{1,q^{(r)}}; (b_{k}^{\prime(1)},\beta_{k}^{\prime(1)})_{1,q^{\prime(1)}}; \cdots; (b_{k}^{\prime(s)},\beta_{k}^{\prime(s)})_{1,q^{\prime(s)}};$$

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$$(0,1); \cdots; (0,1); (0,1); \cdots; (0,1)$$
 (3.13)

$$K_1 = (1 - \alpha - \sum_{i=1}^{u} R_i a_i; \mu_1, \dots, \mu_r, \mu'_1, \dots, \mu'_s, h_1, \dots, h_l, 1, \dots, 1)$$
(3.14)

$$K_2 = (1 - \beta - \sum_{i=1}^{u} R_i b_i; \rho_1, \dots, \rho_r, \rho'_1, \dots, \rho'_s, 0, \dots, 0, 0 \dots, 0)$$
(3.15)

$$K_{j} = [1 - \lambda_{j} - \sum_{i=1}^{u} R_{i} \zeta_{j}^{\prime\prime\prime(i)}; \lambda_{j}^{(1)}, \cdots, \zeta_{j}^{(r)}, \zeta_{j}^{\prime\prime(1)}, \cdots, \zeta_{j}^{\prime\prime(s)}, 0, \cdots, 1, \cdots, 0, 0, \cdots, 0]_{1,l}$$

$$j$$
(3.16)

$$K'_{j} = [1 + \sigma_{j} - \sum_{i=1}^{u} R_{i} \lambda_{j}^{\prime\prime(i)}; \lambda_{j}^{(1)}, \cdots, \lambda_{j}^{(r)}, \lambda_{j}^{\prime(1)}, \cdots, \lambda_{j}^{\prime(s)}, 0, \cdots, 0, 0, \cdots, 1, \cdots, 0]_{1,k}$$

$$j$$
(3.17)

$$L_{1} = (1 - \alpha - \beta - \sum_{i=1}^{u} R_{i}(a_{i} + b_{i}); \mu_{1} + \rho_{1}, \dots, \mu_{r} + \rho_{r}, \mu'_{1} + \rho'_{1}, \dots, \mu'_{r} + \rho'_{r},$$

$$h_{1}, \dots, h_{l}, 1, \dots, 1)$$
(3.18)

$$L_{j} = [1 - \lambda_{j} - \sum_{i=1}^{u} R_{i} \zeta_{j}^{\prime\prime(i)}; \zeta_{j}^{(1)}, \cdots, \zeta_{j}^{(r)}, \zeta_{j}^{\prime(1)}, \cdots, \zeta_{j}^{\prime(s)}, 0, \cdots, 0, 0, \cdots, 0]_{1,l}$$
(3.19)

$$L'_{j} = [1 + \sigma_{j} - \sum_{i=1}^{u} R_{i} \lambda''_{j}^{(i)}; \lambda_{j}^{(1)}, \dots, \lambda_{j}^{(r)}, \lambda'_{j}^{(1)}, \dots, \lambda'_{j}^{(s)}, 0, \dots, 0, 0, \dots, 0]_{1,k}$$
(3.20)

$$P_1 = (b - a)^{\alpha + \beta - 1} \left\{ \prod_{j=1}^k (af_j + g_j)^{\sigma_j} \right\}$$
 (3.21)

$$P_u = (b - a)^{\sum_{i=1}^u (a_i + b_i) R_i} \left\{ \prod_{j=1}^h (af_j + g_j)^{-\sum_{l=1}^u \lambda_j''(i)} R_i \right\}$$
(3.22)

$$B_u = \frac{(-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u)}{R_1! \dots R_u!}$$
(3.23)

We the following generalized Eulerian integral:

$$\int_{a}^{b} (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^{l} \left[ 1 - \tau_{j} (t-a)^{h_{i}} \right]^{-\lambda_{j}} \prod_{j=1}^{k} (f_{j}t + g_{j})^{\sigma_{j}}$$

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$$S_L^{h_1,\dots,h_u} \begin{pmatrix} z_1''\theta_1''(t-a)^{a_1}(b-t)^{b_1} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j''(1)} \\ \vdots \\ \vdots \\ z_u''\theta_u''(t-a)^{a_u}(b-t)^{b_u} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j''(u)} \end{pmatrix}$$

$$I\left(\begin{array}{c} z_{1}\theta_{1}(t-a)^{\mu_{1}}(b-t)^{\rho_{1}}\prod_{j=1}^{k}(f_{j}t+g_{j})^{-\lambda_{j}^{(1)}} \\ \vdots \\ \vdots \\ z_{r}\theta_{r}(t-a)^{\mu_{r}}(b-t)^{\rho_{r}}\prod_{j=1}^{k}(f_{j}t+g_{j})^{-\lambda_{j}^{(r)}} \end{array}\right)$$

$$I\begin{pmatrix} z_1'\theta_1'(t-a)^{\mu_1'}(b-t)^{\rho_1'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z_s'\theta_s'(t-a)^{\mu_s'}(b-t)^{\rho_s'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(s)}} \end{pmatrix} dt =$$

$$= P_1 \sum_{R_1, \dots, R_u = 0}^{h_1 R_1 + \dots + h_v R_u \leqslant L} \prod_{k=1}^{u} z_k^{"R_k} P_u B_u$$

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We obtain the I-function of r+s+k+l variables. The quantities  $U, V, X, Y, A, B, K_1, K_2, K_j, K'_j, \mathfrak{A}, \mathfrak{A}', \mathfrak{A}_1, L_1, L_j, L'_j, \mathfrak{B}, \mathfrak{B}', P_1, P_u, B_u$  and  $\mathfrak{B}_1$  are defined above.

Provided that

(A) 
$$a, b \in \mathbb{R}(a < b); \mu_i, \mu'_u, \rho_i, \rho'_u, \lambda^{(i)}_j, \lambda^{(u)}_j, h_v \in \mathbb{R}^+, f_i, g_j, \tau_v, \sigma_j, \lambda_v \in \mathbb{C} \ (i = 1, \dots, r; j = 1, \dots; k; u = 1, \dots, s; v = 1, \dots, l), a_i, b_i, \lambda^{((i))}_j \in \mathbb{R}^+, (i = 1, \dots, u; j = 1, \dots, k)$$

**(B)** 
$$a_{ij}, b_{ik}, \in \mathbb{C} \ (i = 1, \dots, r; j = 1, \dots, p_i; k = 1, \dots, q_i); a_i^{(i)}, b_i^{(k)} \in \mathbb{C}$$

$$(i = 1, \dots, r; j = 1, \dots, p^{(i)}; k = 1, \dots, q^{(i)})$$

$$a'_{ij}, b'_{ik}, \in \mathbb{C} \ (i=1, \cdots, s; j=1, \cdots, p'_i; k=1, \cdots, q'_i); a'_i{}^{(i)}, b'_i{}^{(k)}, \in \mathbb{C}$$

$$(i = 1, \dots, r; j = 1, \dots, p^{(i)}; k = 1, \dots, q^{(i)})$$

$$\alpha_{ij}^{(k)}, \beta_{ij}^{(k)} \in \mathbb{R}^+ \text{ ( } (i=1,\cdots,r,j=1,\cdots,p_i, k=1,\cdots,r) \text{ ; } \alpha_{j}^{(i)}, \beta_{i}^{(i)} \in \mathbb{R}^+ \text{ } (i=1,\cdots,r; j=1,\cdots,p_i) \text{ }$$

$$\alpha_{ij}^{\prime\,(k)},\beta_{ij}^{\prime\,(k)}\in\mathbb{R}^{+}\text{ ( }(i=1,\cdots,s,j=1,\cdots,p_{i}^{\prime},k=1,\cdots,s)\text{ ; }\alpha_{j}^{\prime\,(i)},\beta_{i}^{\prime\,(i)}\in\mathbb{R}^{+}\text{ }(i=1,\cdots,s;j=1,\cdots,p_{i}^{\prime})\text{ }(i=1,\cdots,s;j=1,\cdots,$$

(C) 
$$\max_{1 \leqslant j \leqslant k} \left\{ \left| \frac{(b-a)f_i}{af_i + g_i} \right| \right\} < 1, \max_{1 \leqslant j \leqslant l} \left\{ \left| \tau_j (b-a)^{h_j} \right| \right\} < 1$$

(D) 
$$Re\left[\alpha + \sum_{j=1}^{r} \mu_{j} \min_{1 \leqslant k \leqslant m^{(i)}} \frac{b_{k}^{(j)}}{\beta_{k}^{(j)}} + \sum_{j=1}^{s} \mu'_{i} \min_{1 \leqslant k \leqslant m'^{(i)}} \frac{b'_{k}^{(j)}}{\beta_{k}^{\prime(j)}}\right] > 0$$

$$Re\left[\beta + \sum_{i=1}^{r} \rho_{j} \min_{1 \leqslant k \leqslant m^{(i)}} \frac{b_{k}^{(j)}}{\beta_{k}^{(j)}} + \sum_{i=1}^{s} \rho'_{i} \min_{1 \leqslant k \leqslant m'^{(i)}} \frac{b'_{k}^{(j)}}{\beta'_{k}^{(j)}}\right] > 0$$

(E) 
$$Re\left(\alpha + \sum_{i=1}^{u} R_{i}a_{i} + \sum_{i=1}^{r} \mu_{i}s_{i} + \sum_{i=1}^{s} t_{i}\mu'_{i}\right) > 0$$
;  $Re\left(\beta + \sum_{i=1}^{u} R_{i}b_{i} + \sum_{i=1}^{r} v_{i}s_{i} + \sum_{i=1}^{s} t_{i}\rho'_{i}\right) > 0$ 

$$Re\left(\lambda_{j} + \sum_{i=1}^{u} R_{i} \lambda_{j}^{"(i)} + \sum_{i=1}^{r} s_{i} \zeta_{j}^{(i)} + \sum_{i=1}^{s} t_{i} \zeta_{j}^{"(i)}\right) > 0 (j = 1, \dots, l);$$

$$Re\left(-\sigma_{j} + \sum_{i=1}^{u} R_{i}\lambda_{j}^{\prime\prime(i)} + \sum_{i=1}^{r} s_{i}\lambda_{j}^{(i)} + \sum_{i=1}^{s} t_{i}\lambda_{j}^{\prime(i)}\right) > 0 (j = 1, \dots, k);$$

$$\textbf{(F)}\ \Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left(\sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)}\right) + \dots + \frac{1}{n^{(i)}} \alpha_{2k}^{(i)} + \frac{1}{n^{(i)}} \alpha_{2k}^{(i)}$$

$$\left(\sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)}\right) - \left(\sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \dots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)}\right) - \mu_i - \rho_i$$

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$$-\sum_{l=1}^{k} \lambda_{j}^{(i)} - \sum_{l=1}^{l} \zeta_{j}^{(i)} > 0 \quad (i = 1, \dots, r)$$

$$\Omega_{i}^{\prime} = \sum_{k=1}^{n^{\prime(i)}} \alpha_{k}^{\prime(i)} - \sum_{k=n^{\prime(i)}+1}^{p^{\prime(i)}} \alpha_{k}^{\prime(i)} + \sum_{k=1}^{m^{\prime(i)}} \beta_{k}^{\prime(i)} - \sum_{k=m^{(i)}+1}^{q^{\prime(i)}} \beta_{k}^{\prime(i)} + \left(\sum_{k=1}^{n_{2}^{\prime}} \alpha_{2k}^{\prime(i)} - \sum_{k=n_{2}+1}^{p_{2}^{\prime}} \alpha_{2k}^{\prime(i)}\right) + \sum_{k=1}^{n^{\prime(i)}} \alpha_{k}^{\prime(i)} + \sum_{k=1}^{n^{\prime(i)}} \beta_{k}^{\prime(i)} - \sum_{k=n_{2}+1}^{n^{\prime(i)}} \alpha_{2k}^{\prime(i)} - \sum_{k=n_{2}+1}^{n^{\prime(i)}} \alpha_{2k}^{\prime(i)} + \sum_{k=1}^{n^{\prime(i)}} \alpha_{2k}^{\prime(i)} - \sum_{k=n_{2}+1}^{n^{\prime(i)}} \alpha_{2k}^{\prime(i)} - \sum_{k=n_{2}+1}$$

$$\cdots + \left(\sum_{k=1}^{n_s'} \alpha_{sk}'^{(i)} - \sum_{k=n_s'+1}^{p_s'} \alpha_{sk}'^{(i)}\right) - \left(\sum_{k=1}^{q_2'} \beta_{2k}'^{(i)} + \sum_{k=1}^{q_3'} \beta_{3k}'^{(i)} + \cdots + \sum_{k=1}^{q_s'} \beta_{sk}'^{(i)}\right) - \mu_i' - \rho_i'$$

$$-\sum_{l=1}^{k} \lambda_{j}^{\prime(i)} - \sum_{l=1}^{l} \zeta_{j}^{\prime(i)} > 0 \quad (i = 1, \dots, s)$$

(G) 
$$\left| arg \left( z_i \prod_{j=1}^l \left[ 1 - \tau_j (t-a)^{h_i} \right]^{-\zeta_j^{(i)}} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(i)}} \right) \right| < \frac{1}{2} \Omega_i \pi \ (a \leqslant t \leqslant b; i = 1, \dots, r)$$

$$\left| arg \left( z_i' \prod_{j=1}^{l} \left[ 1 - \tau_j'(t-a)^{h_i'} \right]^{-\zeta_j'^{(i)}} \prod_{j=1}^{k} (f_j t + g_j)^{-\lambda_j'^{(i)}} \right) \right| < \frac{1}{2} \Omega_i' \pi \quad (a \leqslant t \leqslant b; i = 1, \dots, s)$$

#### **Proof**

To prove (3.24), first, we express in serie a class of multivariable polynomials defined by Srivastava et al [4],  $S_L^{h_1,\cdots,h_u}[.]$  with the help of (1.7), espressing the I-function of r variables by the Mellin-Barnes contour integral with the help of the equation (1.2), the I-function of s variables by the Mellin-Barnes contour integral with the help of the equation (1.5). Now collect the power of  $\left[1-\tau_j(t-a)^{h_i}\right]$  with  $(i=1,\cdots,r;j=1,\cdots,l)$  and collect the power of  $(f_jt+g_j)$  with  $j=1,\cdots,k$ . Use the equations (2.2) and (2.3) and express the result in Mellin-Barnes contour integral. Interpreting the (r+s+k+l) dimensional Mellin-Barnes integral to multivariable I-function of Prasad, we obtain the equation (3.24).

#### Remarks

If a) 
$$\rho_1 = \cdots, \rho_r = \rho_1' = \cdots, \rho_s' = 0$$
; b)  $\mu_1 = \cdots, \mu_r = \mu_1' = \cdots, \mu_s' = 0$ 

we obtain the similar formulas that (3.24) with the corresponding simplifications.

## 4. Particular cases

a) If U=V=A=B=0, the multivariable I-function defined by Prasad reduces to multivariable H-function defined by Srivastava et al [6] and we obtain :

$$\int_{a}^{b} (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^{l} \left[ 1 - \tau_{j} (t-a)^{h_{i}} \right]^{-\lambda_{j}} \prod_{j=1}^{k} (f_{j}t + g_{j})^{\sigma_{j}}$$

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$$S_L^{h_1,\dots,h_u} \begin{pmatrix} z_1''\theta_1''(t-a)^{a_1}(b-t)^{b_1} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j''(1)} \\ \vdots \\ \vdots \\ z_u''\theta_u''(t-a)^{a_u}(b-t)^{b_u} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j''(u)} \end{pmatrix}$$

$$H\begin{pmatrix} z_1\theta_1(t-a)^{\mu_1}(b-t)^{\rho_1} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r\theta_r(t-a)^{\mu_r}(b-t)^{\rho_r} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j^{(r)}} \end{pmatrix}$$

$$H\begin{pmatrix} z_1'\theta_1'(t-a)^{\mu_1'}(b-t)^{\rho_1'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z_s'\theta_s'(t-a)^{\mu_s'}(b-t)^{\rho_s'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(s)}} \end{pmatrix} dt =$$

$$= P_1 \sum_{R_1, \dots, R_u = 0}^{h_1 R_1 + \dots + h_u R_u \leqslant L} \prod_{k=1}^{u} z_k^{"R_k} P_u B_u$$

$$= P_{1} \sum_{R_{1}, \dots, R_{u}=0}^{n_{1} R_{1} + \dots + n_{u}} \prod_{k=1}^{u} z_{k}^{"R_{k}} P_{u} B_{u}$$

$$\begin{pmatrix} \frac{z_{1}(b-a)^{\mu_{1} + \mu_{1}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{(1)}}} & \\ \vdots & \vdots & \\ \frac{z_{r}(b-a)^{\mu_{r} + \mu_{r}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{(1)}}} \\ \frac{z_{1}^{\prime}(b-a)^{\mu_{1}^{\prime} + \mu_{1}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{\prime}(1)}} & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \frac{z_{s}^{\prime}(b-a)^{\mu_{s}^{\prime} + \mu_{s}^{\prime}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{\prime}(1)}} & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \frac{z_{s}^{\prime}(b-a)^{\mu_{s}^{\prime} + \mu_{s}^{\prime}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{\prime}(1)}} & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \frac{z_{s}^{\prime}(b-a)^{\mu_{1}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{\prime}(1)}} & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \frac{z_{s}^{\prime}(b-a)^{\mu_{1}}}{\prod_{j=1}^{k} (af_{j} + g_{j})^{\lambda_{j}^{\prime}(1)}} & \vdots \\ \vdots & \vdots & \vdots & \vdots \\ \frac{(b-a)f_{k}}{af_{k} + g_{k}} & \vdots \\ \end{bmatrix}$$

$$L_{1}, L_{j}, L_{j}^{\prime}, \mathfrak{B}, \mathfrak{B}^{\prime}; \mathfrak{B}_{1}$$

ISSN: 2231-5373 http://www.ijmttjournal.org under the same notations and conditions that (3.24) with U=V=A=B=0

b) If 
$$B(L; R_1, \dots, R_u) = \frac{\prod_{j=1}^{\bar{A}} (a_j)_{R_1 \theta'_j + \dots + R_u \theta_j^{(u)}} \prod_{j=1}^{B'} (b'_j)_{R_1 \phi'_j} \dots \prod_{j=1}^{B^{(u)}} (b_j^{(u)})_{R_u \phi_j^{(u)}}}{\prod_{j=1}^{\bar{C}} (c_j)_{m_1 \psi'_j + \dots + m_u \psi_j^{(u)}} \prod_{j=1}^{D'} (d'_j)_{R_1 \delta'_j} \dots \prod_{j=1}^{D^{(u)}} (d_j^{(u)})_{R_u \delta_j^{(u)}}}$$
 (4.2)

then the general class of multivariable polynomial  $S_L^{h_1,\cdots,h_u}[z_1,\cdots,z_u]$  reduces to generalized Lauricella function defined by Srivastava et al [3].

$$F_{\bar{C}:D';\cdots;D^{(u)}}^{1+\bar{A}:B';\cdots;B^{(u)}}\begin{pmatrix} \mathbf{z}_{1} \\ \dots \\ \mathbf{z}_{u} \end{pmatrix} [(-\mathbf{L});\mathbf{R}_{1},\cdots,\mathbf{R}_{u}][(a);\theta',\cdots,\theta^{(u)}]:[(b');\phi'];\cdots;[(b^{(u)});\phi^{(u)}] \\ [(c);\psi',\cdots,\psi^{(u)}]:[(d');\delta'];\cdots;[(d^{(u)});\delta^{(u)}] \end{pmatrix}$$
(4.3)

and we have the following formula

$$\int_{a}^{b} (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^{l} \left[ 1 - \tau_{j} (t-a)^{h_{i}} \right]^{-\lambda_{j}} \prod_{j=1}^{k} (f_{j}t + g_{j})^{\sigma_{j}}$$

$$[(-L); R_1, \dots, R_u][(a); \theta', \dots, \theta^{(u)}] : [(b'); \phi']; \dots; [(b^{(u)}); \phi^{(u)}]$$

$$[(c); \psi', \dots, \psi^{(u)}] : [(d'); \delta']; \dots; [(d^{(u)}); \delta^{(u)}]$$

$$I\begin{pmatrix} z_1\theta_1(t-a)^{\mu_1}(b-t)^{\rho_1} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r\theta_r(t-a)^{\mu_r}(b-t)^{\rho_r} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j^{(r)}} \end{pmatrix}$$

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$$I\begin{pmatrix} z_1'\theta_1'(t-a)^{\mu_1'}(b-t)^{\rho_1'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z_s'\theta_s'(t-a)^{\mu_s'}(b-t)^{\rho_s'} \prod_{j=1}^k (f_jt+g_j)^{-\lambda_j'^{(s)}} \end{pmatrix} dt =$$

$$= P_1 \sum_{R_1, \dots, R_n = 0}^{h_1 R_1 + \dots + h_u R_u \leqslant L} \prod_{k=1}^{u} z_k^{"R_k} P_u B_u'$$

$$I_{U:p_r+p_s'+l+k+2;X}^{V;0,n_r+n_s'+l+k+2;X} = \begin{pmatrix} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} \\ \vdots \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(r)}}} \\ \frac{z_1(b-a)^{\mu_1'+\rho_1'}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} \\ \vdots \\ \vdots \\ \frac{z_s'(b-a)^{\mu_s'+\rho_s'}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} \\ \frac{z_1(b-a)^{\mu_1'+\rho_1'}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} \\ \vdots \\ \vdots \\ \vdots \\ \vdots \\ \frac{(b-a)f_1}{af_1+g_1} \\ \vdots \\ \vdots \\ \vdots \\ \frac{(b-a)f_k}{af_k+g_k} \end{pmatrix}$$

$$A; K_1, K_2, K_j, K_j', \mathfrak{A}, \mathfrak{A}'; \mathfrak{A}_1$$

$$\vdots \\ \vdots \\ \vdots \\ \vdots \\ B; L_1, K_j, K_j', \mathfrak{A}, \mathfrak{A}'; \mathfrak{A}_1$$

under the same conditions that (3.24)

and 
$$B_u'=\frac{(-L)_{h_1R_1+\cdots+h_uR_u}B(E;R_1,\cdots,R_u)}{R_1!\cdots R_u!}$$
 ;  $B(L;R_1,\cdots,R_u)$  is defined by (4.2)

#### Remark:

By the following similar procedure, the results of this document can be extented to product of any finite number of multivariable I-functions of Prasad [1] and a class of multivariable polynomials defined by Srivastava et al [4].

#### 5. Conclusion

In this paper we have evaluated a generalized Eulerian integral involving the product of two multivariable I-functions

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defined by Prasad [1] and a class of multivariable polynomials defined by Srivastava et al [4] with general arguments. The formulae established in this paper is very general nature. Thus, the results established in this research work would serve as a key formula from which, upon specializing the parameters, as many as desired results involving the special functions of one and several variables can be obtained.

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