

Eulerian integral associated with product of two multivariable

Prasad's I-functions and classes of polynomials

F.Y. AYANT¹

¹ Teacher in High School , France

ABSTRACT

The present paper is evaluated a new Eulerian integral associated with the product of two multivariable I-functions defined by Prasad [1] a generalized Lauricella function , a classes of multivariable polynomials with general arguments . We will study the case concerning the multivariable H-function defined by Srivastava et al [7] and Srivastava-Daoust polynomial [4].

Keywords: Eulerian integral, multivariable I-function, generalized Lauricella function of several variables, multivariable H-function, generalized hypergeometric function, class of polynomials

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1. Introduction

In this paper, we evaluate a new Eulerian integral of most general characters associated with the products of two multivariable I-functions defined by Prasad [1] , and classes of polynomials with general arguments.

First time, we define the multivariable *I*-function by :

The multivariable I-function of r-variables is defined in term of multiple Mellin-Barnes type integral :

$$I(z_1, \dots, z_r) = I_{p_2, q_2, p_3, q_3, \dots; p_r, q_r; p^{(1)}, q^{(1)}, \dots; p^{(r)}, q^{(r)}}^{0, n_2; 0, n_3; \dots; 0, n_r; m^{(1)}, n^{(1)}, \dots; m^{(r)}, n^{(r)}} \left(\begin{matrix} z_1 \\ \cdot \\ \cdot \\ z_r \end{matrix} \middle| \begin{matrix} (a_{2j}; \alpha'_{2j}, \alpha''_{2j})_{1, p_2}; \dots; \\ (b_{2j}; \beta'_{2j}, \beta''_{2j})_{1, q_2}; \dots; \end{matrix} \right)$$

$$(a_{rj}; \alpha_{rj}^{(1)}, \dots, \alpha_{rj}^{(r)})_{1, p_r} : (a_j^{(1)}, \alpha_j^{(1)})_{1, p^{(1)}}; \dots; (a_j^{(r)}, \alpha_j^{(r)})_{1, p^{(r)}} \left(\begin{matrix} (b_{rj}; \beta_{rj}^{(1)}, \dots, \beta_{rj}^{(r)})_{1, q_r} : (b_j^{(1)}, \beta_j^{(1)})_{1, q^{(1)}}; \dots; (b_j^{(r)}, \beta_j^{(r)})_{1, q^{(r)}} \end{matrix} \right) \quad (1.1)$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_1} \dots \int_{L_r} \phi(s_1, \dots, s_r) \prod_{i=1}^r \theta_i(s_i) z_i^{s_i} ds_1 \dots ds_r \quad (1.2)$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [1]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

$$|arg z_i| < \frac{1}{2} \Omega_i \pi, \text{ where}$$

$$\Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left(\sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)} \right) + \dots +$$

$$\left(\sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)} \right) - \left(\sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \cdots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)} \right) \quad (1.3)$$

where $i = 1, \dots, r$

The complex numbers z_i are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the asymptotic expansion in the following convenient form :

$$I(z_1, \dots, z_r) = O(|z_1|^{\alpha_1}, \dots, |z_r|^{\alpha_r}), \max(|z_1|, \dots, |z_r|) \rightarrow 0$$

$$I(z_1, \dots, z_r) = O(|z_1|^{\beta_1}, \dots, |z_r|^{\beta_r}), \min(|z_1|, \dots, |z_r|) \rightarrow \infty$$

where $k = 1, \dots, r : \alpha'_k = \min[Re(b_j^{(k)} / \beta_j^{(k)})], j = 1, \dots, m_k$ and

$$\beta'_k = \max[Re(a_j^{(k)} - 1) / \alpha_j^{(k)}], j = 1, \dots, n_k$$

Consider a second multivariable I-function defined by Prasad [1]

$$I(z'_1, \dots, z'_s) = I_{\substack{0, n'_2; 0, n'_3; \dots; 0, n'_r; m'^{(1)}, n'^{(1)}; \dots; m'^{(s)}, n'^{(s)} \\ p'_2, q'_2, p'_3, q'_3; \dots; p'_s, q'_s; p'^{(1)}, q'^{(1)}; \dots; p'^{(s)}, q'^{(s)}}} \left(\begin{matrix} z'_1 \\ \vdots \\ z'_s \end{matrix} \middle| \begin{matrix} (a'_{2j}; \alpha'_{2j}{}^{(1)}, \alpha'_{2j}{}^{(2)})_{1, p'_2}; \dots; \\ (b'_{2j}; \beta'_{2j}{}^{(1)}, \beta'_{2j}{}^{(2)})_{1, q'_2}; \dots; \end{matrix} \right) \quad (1.4)$$

$$= \frac{1}{(2\pi\omega)^s} \int_{L_1} \cdots \int_{L_s} \psi(t_1, \dots, t_s) \prod_{i=1}^s \xi_i(t_i) z_i^{t_i} dt_1 \cdots dt_s \quad (1.5)$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [1]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

where $|\arg z'_i| < \frac{1}{2} \Omega'_i \pi$,

$$\Omega'_i = \sum_{k=1}^{n'^{(i)}} \alpha'_k{}^{(i)} - \sum_{k=n'^{(i)}+1}^{p'^{(i)}} \alpha'_k{}^{(i)} + \sum_{k=1}^{m'^{(i)}} \beta'_k{}^{(i)} - \sum_{k=m'^{(i)}+1}^{q'^{(i)}} \beta'_k{}^{(i)} + \left(\sum_{k=1}^{n'_2} \alpha'_{2k}{}^{(i)} - \sum_{k=n_2+1}^{p'_2} \alpha'_{2k}{}^{(i)} \right)$$

$$+ \cdots + \left(\sum_{k=1}^{n'_s} \alpha'_{sk}{}^{(i)} - \sum_{k=n'_s+1}^{p'_s} \alpha'_{sk}{}^{(i)} \right) - \left(\sum_{k=1}^{q'_2} \beta'_{2k}{}^{(i)} + \sum_{k=1}^{q'_3} \beta'_{3k}{}^{(i)} + \cdots + \sum_{k=1}^{q'_s} \beta'_{sk}{}^{(i)} \right) \quad (1.6)$$

where $i = 1, \dots, s$

The complex numbers z_i are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the asymptotic expansion in the following convenient form :

$$I(z'_1, \dots, z'_s) = O(|z'_1|^{\alpha'_1}, \dots, |z'_s|^{\alpha'_s}), \max(|z'_1|, \dots, |z'_s|) \rightarrow 0$$

$$I(z'_1, \dots, z'_s) = O(|z'_1|^{\beta'_1}, \dots, |z'_s|^{\beta'_s}), \min(|z'_1|, \dots, |z'_s|) \rightarrow \infty$$

where $k = 1, \dots, s : \alpha''_k = \min[Re(b_j^{(k)}/\beta_j^{(k)})], j = 1, \dots, m'_k$ and

$$\beta''_k = \max[Re((a_j^{(k)} - 1)/\alpha_j^{(k)}), j = 1, \dots, n'_k]$$

where $k = 1, \dots, s : \alpha''_k = \min[Re(b_j^{(k)}/\beta_j^{(k)})], j = 1, \dots, m'_k$ and

$$\beta''_k = \max[Re((a_j^{(k)} - 1)/\alpha_j^{(k)}), j = 1, \dots, n'_k]$$

The generalized polynomials of multivariables defined by Srivastava [3], is given in the following manner :

$$S_{N_1, \dots, N_v}^{\mathfrak{M}_1, \dots, \mathfrak{M}_v}[y_1, \dots, y_v] = \sum_{K_1=0}^{[N_1/\mathfrak{M}_1]} \cdots \sum_{K_v=0}^{[N_v/\mathfrak{M}_v]} \frac{(-N_1)_{\mathfrak{M}_1 K_1}}{K_1!} \cdots \frac{(-N_v)_{\mathfrak{M}_v K_v}}{K_v!} A[N_1, K_1; \dots; N_v, K_v] y_1^{K_1} \cdots y_v^{K_v} \quad (1.7)$$

where $\mathfrak{M}_1, \dots, \mathfrak{M}_v$ are arbitrary positive integers and the coefficients $A[N_1, K_1; \dots; N_v, K_v]$ are arbitrary constants, real or complex.

Srivastava and Garg [5] introduced and defined a general class of multivariable polynomials as follows

$$S_L^{h_1, \dots, h_u}[z_1, \dots, z_u] = \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} (-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u) \frac{z_1^{R_1} \cdots z_u^{R_u}}{R_1! \cdots R_u!} \quad (1.8)$$

The coefficients are $B[E; R_1, \dots, R_u]$ arbitrary constants, real or complex.

We will note $a_v = \frac{(-N_1)_{\mathfrak{M}_1 K_1}}{K_1!} \cdots \frac{(-N_v)_{\mathfrak{M}_v K_v}}{K_v!} A[N_1, K_1; \dots; N_v, K_v]$ and

$$b_u = \frac{(-E)_{F_1 L_1 + \dots + F_u L_u} B(E; L_1, \dots, L_u)}{L_1! \cdots L_u!} \quad (1.9)$$

2. Integral representation of generalized Lauricella function of several variables

The following generalized hypergeometric function in terms of multiple contour integrals is also required [6, page 39 eq .30]

$$\frac{\prod_{j=1}^P \Gamma(A_j)}{\prod_{j=1}^Q \Gamma(B_j)} {}_P F_Q [(A_P); (B_Q); -(x_1 + \cdots + x_r)]$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_1} \cdots \int_{L_r} \frac{\prod_{j=1}^P \Gamma(A_j + s_1 + \cdots + s_r)}{\prod_{j=1}^Q \Gamma(B_j + s_1 + \cdots + s_r)} \Gamma(-s_1) \cdots \Gamma(-s_r) x_1^{s_1} \cdots x_r^{s_r} ds_1 \cdots ds_r \quad (2.1)$$

where the contours are of Barnes type with indentations, if necessary, to ensure that the poles of $\Gamma(A_j + s_1 + \cdots + s_r)$ are separated from those of $\Gamma(-s_j), j = 1, \cdots, r$. The above result (1.23) can be easily established by an appeal to the calculus of residues by calculating the residues at the poles of $\Gamma(-s_j), j = 1, \cdots, r$

In order to evaluate a number of integrals of multivariable I-function, we first establish the formula

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1 - \tau_j(t-a)^{h_j}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j} dt = (b-a)^{\alpha+\beta-1} B(\alpha, \beta) \prod_{j=1}^k (af_j + g_j)^{\sigma_j}$$

$$F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1} \left(\begin{matrix} (\alpha : h_1, \dots, h_l, 1, \dots, 1) : (\lambda_1 : 1), \dots, (\lambda_l : 1); (-\sigma_1 : 1), \dots, (-\sigma_k : 1) \\ \vdots \\ (\alpha + \beta : h_1, \dots, h_l, 1, \dots, 1) : -, \dots, -; -, \dots, - \end{matrix} \right)$$

$$; \tau_1(b-a)^{h_1}, \dots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1 + g_1}, \dots, -\frac{(b-a)f_k}{af_k + g_k} \quad (2.2)$$

where $a, b \in \mathbb{R} (a < b), \alpha, \beta, f_i, g_i, \sigma_i, \tau_j, h_j \in \mathbb{C}, \lambda_j \in \mathbb{R}^+ (i = 1, \dots, k; j = 1, \dots, l)$

$$\min(\operatorname{Re}(\alpha), \operatorname{Re}(\beta)) > 0, \max_{1 \leq j \leq l} \{|\tau_j(b-a)^{h_j}|\} < 1, \max_{1 \leq j \leq k} \left\{ \left| \frac{(b-a)f_j}{af_j + g_j} \right| \right\} < 1,$$

and $F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1}$ is a particular case of the generalized Lauricella function introduced by Srivastava-Daoust[3, page 454] given by :

$$F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1} \left(\begin{matrix} (\alpha : h_1, \dots, h_l, 1, \dots, 1) : (\lambda_1 : 1), \dots, (\lambda_l : 1); (-\sigma_1 : 1), \dots, (-\sigma_k : 1) \\ \vdots \\ (\alpha + \beta : h_1, \dots, h_l, 1, \dots, 1) : -, \dots, -; -, \dots, - \end{matrix} \right)$$

$$; \tau_1(b-a)^{h_1}, \dots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1 + g_1}, \dots, -\frac{(b-a)f_k}{af_k + g_k} \Bigg) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha) \prod_{j=1}^l \Gamma(\lambda_j) \prod_{j=1}^k \Gamma(-\sigma_j)}$$

$$\frac{1}{(2\pi\omega)^{l+k}} \int_{L_1} \cdots \int_{L_{l+k}} \frac{\Gamma\left(\alpha + \sum_{j=1}^l h_j s_j + \sum_{j=1}^k s_{l+j}\right)}{\Gamma\left(\alpha + \beta + \sum_{j=1}^l h_j s_j + \sum_{j=1}^k s_{l+j}\right)} \prod_{j=1}^l \Gamma(\lambda_j + s_j) \prod_{j=1}^k \Gamma(-\sigma_j + s_{l+j})$$

$$\prod_{j=1}^{l+k} \Gamma(-s_j) z_1^{s_1} \cdots z_l^{s_l} z_{l+1}^{s_{l+1}} \cdots z_{l+k}^{s_{l+k}} ds_1 \cdots ds_{l+k} \quad (2.3)$$

Here the contour $L'_j s$ are defined by $L_j = L_{w\zeta_j\infty}(Re(\zeta_j) = v''_j)$ starting at the point $v''_j - \omega\infty$ and terminating at the point $v''_j + \omega\infty$ with $v''_j \in \mathbb{R}(j = 1, \dots, l)$ and each of the remaining contour L_{l+1}, \dots, L_{l+k} run from $-\omega\infty$ to $\omega\infty$

(2.2) can be easily established by expanding $\prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\lambda_j}$ by means of the formula :

$$(1-z)^{-\alpha} = \sum_{r=0}^{\infty} \frac{(\alpha)_r}{r!} z^r (|z| < 1) \quad (2.4)$$

integrating term by term with the help of the integral given by Saigo and Saxena [3, page 93, eq.(3.2)] and applying the definition of the generalized Lauricella function [6, page 454].

3. Eulerian integral

In this section , we note :

$$\theta_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\zeta_j^{(i)}}, \zeta_j^{(i)} > 0 (i = 1, \dots, r); \theta'_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\zeta_j'^{(i)}}, \zeta_j'^{(i)} > 0 (i = 1, \dots, s)$$

$$\theta''_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\zeta_j''^{(i)}}, \zeta_j''^{(i)} > 0 (i = 1, \dots, u)$$

$$\theta'''_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\zeta_j'''^{(i)}}, \zeta_j'''^{(i)} > 0 (i = 1, \dots, v) \quad (3.1)$$

$$U = p_2, q_2; p_3, q_3; \cdots; p_{r-1}, q_{r-1}; p'_2, q'_2; p'_3, q'_3; \cdots; p'_{s-1}, q'_{s-1}; 0, 0; \cdots; 0, 0; 0, 0; \cdots; 0, 0 \quad (3.2)$$

$$V = 0, n_2; 0, n_3; \cdots; 0, n_{r-1}; 0, n'_2; 0, n'_3; \cdots; 0, n'_{s-1}; 0, 0; \cdots; 0, 0; 0, 0; \cdots; 0, 0 \quad (3.3)$$

$$X = m^{(1)}, n^{(1)}; \cdots; m^{(r)}, n^{(r)}; m'^{(1)}, n'^{(1)}; \cdots; m'^{(s)}, n'^{(s)}; 1, 0; \cdots; 1, 0; 1, 0; \cdots; 1, 0 \quad (3.4)$$

$$Y = p^{(1)}, q^{(1)}; \cdots; p^{(r)}, q^{(r)}; p'^{(1)}, q'^{(1)}; \cdots; p'^{(s)}, q'^{(s)}; 0, 1; \cdots; 0, 1; 0, 1; \cdots; 0, 1 \quad (3.5)$$

$$A = (a_{2k}; \alpha_{2k}^{(1)}, \alpha_{2k}^{(2)}; \cdots; (a_{(r-1)k}; \alpha_{(r-1)k}^{(1)}, \alpha_{(r-1)k}^{(2)}, \cdots, \alpha_{(r-1)k}^{(r-1)}); (a'_{2k}; \alpha_{2k}'^{(1)}, \alpha_{2k}'^{(2)}; \cdots; (a'_{(s-1)k}; \alpha_{(s-1)k}'^{(1)}, \alpha_{(s-1)k}'^{(2)}, \cdots, \alpha_{(s-1)k}'^{(s-1)}) \quad (3.6)$$

$$; (b'_{2k}; \beta_{2k}'^{(1)}, \beta_{2k}'^{(2)}); \cdots; B = (b_{2k}; \beta_{2k}^{(1)}, \beta_{2k}^{(2)}); \cdots; (b_{(r-1)k}; \beta_{(r-1)k}^{(1)}, \beta_{(r-1)k}^{(2)}, \cdots, \beta_{(r-1)k}^{(r-1)})$$

$$(b'_{(s-1)k}; \beta_{(s-1)k}'^{(1)}, \beta_{(s-1)k}'^{(2)}, \cdots, \beta_{(s-1)k}'^{(s-1)}) \quad (3.7)$$

$$A = (a_{rk}; \alpha_{rk}^{(1)}, \alpha_{rk}^{(2)}, \cdots, \alpha_{rk}^{(r)}, 0, \cdots, 0, 0, \cdots, 0, 0, \cdots, 0) \quad (3.8)$$

$$A' = (a'_{sk}; 0, \dots, 0, \alpha'^{(1)}_{sk}, \alpha'^{(2)}_{sk}, \dots, \alpha'^{(s)}_{sk}, 0, \dots, 0, 0, \dots, 0) \quad (3.9)$$

$$B = (b_{rk}; \beta^{(1)}_{rk}, \beta^{(2)}_{rk}, \dots, \beta^{(r)}_{rk}, 0, \dots, 0, 0, \dots, 0, 0, \dots, 0) \quad (3.10)$$

$$B' = (b'_{sk}; 0, \dots, 0, \beta'^{(1)}_{sk}, \beta'^{(2)}_{sk}, \dots, \beta'^{(s)}_{sk}, 0, \dots, 0, 0, \dots, 0) \quad (3.11)$$

$$A' = (a_k^{(1)}, \alpha_k^{(1)})_{1,p^{(1)}}; \dots; (a_k^{(r)}, \alpha_k^{(r)})_{1,p^{(r)}}; (a_k'^{(1)}, \alpha_k'^{(1)})_{1,p^{(1)}}; \dots; (a_k'^{(s)}, \alpha_k'^{(s)})_{1,p^{(s)}}; \\ (1, 0); \dots; (1, 0); (1, 0); \dots; (1, 0) \quad (3.12)$$

$$B' = (b_k^{(1)}, \beta_k^{(1)})_{1,q^{(1)}}; \dots; (b_k^{(r)}, \beta_k^{(r)})_{1,q^{(r)}}; (b_k'^{(1)}, \beta_k'^{(1)})_{1,q^{(1)}}; \dots; (b_k'^{(s)}, \beta_k'^{(s)})_{1,q^{(s)}}; \\ (0, 1); \dots; (0, 1); (0, 1); \dots; (0, 1) \quad (3.13)$$

$$K_1 = (1 - \alpha - \sum_{i=1}^u R_i a_i - \sum_{i=1}^v K_i a'_i; \mu_1, \dots, \mu_r, \mu'_1, \dots, \mu'_s, h_1, \dots, h_l, 1, \dots, 1) \quad (3.14)$$

$$K_2 = (1 - \beta - \sum_{i=1}^u R_i b_i - \sum_{i=1}^v K_i b'_i; \rho_1, \dots, \rho_r, \rho'_1, \dots, \rho'_s, 0, \dots, 0, 0, \dots, 0) \quad (3.15)$$

$$K_j = [1 - \lambda_j - \sum_{i=1}^u R_i \zeta_j^{(i)} - \sum_{i=1}^v K_i \zeta_j^{(i)}; \zeta_j^{(1)}, \dots, \zeta_j^{(r)}, \zeta_j'^{(1)}, \dots, \zeta_j'^{(s)}, \\ 0, \dots, 1, \dots, 0, 0, \dots, 0]_{1,l} \quad (3.16)$$

$$K'_j = [1 + \sigma_j - \sum_{i=1}^u R_i \lambda_j^{(i)} - \sum_{i=1}^v K_i \lambda_j^{(i)}; \lambda_j^{(1)}, \dots, \lambda_j^{(r)}, \lambda_j'^{(1)}, \dots, \lambda_j'^{(s)}, \\ 0, \dots, 0, 0, \dots, 1, \dots, 0]_{1,k} \quad (3.17)$$

$$L_1 = (1 - \alpha - \beta - \sum_{i=1}^u R_i (a_i + b_i) - \sum_{i=1}^v (a'_i + b'_i) K_i; \mu_1 + \rho_1, \dots, \mu_r + \rho_r, \mu'_1 + \rho'_1, \dots, \mu'_r + \rho'_r, \\ h_1, \dots, h_l, 1, \dots, 1) \quad (3.18)$$

$$L_j = [1 - \lambda_j - \sum_{i=1}^u R_i \zeta_j^{(i)} - \sum_{i=1}^v \zeta_j^{(i)} K_i; \zeta_j^{(1)}, \dots, \zeta_j^{(r)}, \zeta_j'^{(1)}, \dots, \zeta_j'^{(s)}, 0, \dots, 0, 0, \dots, 0]_{1,l} \quad (3.19)$$

$$L'_j = [1 + \sigma_j - \sum_{i=1}^u R_i \lambda_j^{(i)} - \sum_{i=1}^v \lambda_j^{(i)} K_i; \lambda_j^{(1)}, \dots, \lambda_j^{(r)}, \lambda_j'^{(1)}, \dots, \lambda_j'^{(s)}, 0, \dots, 0, 0, \dots, 0]_{1,k} \quad (3.20)$$

$$P_1 = (b - a)^{\alpha + \beta - 1} \left\{ \prod_{j=1}^h (af_j + g_j)^{\sigma_j} \right\} \quad (3.21)$$

$$B_{u,v} = (b-a)^{\sum_{i=1}^v K_i(a'_i+b'_i)+\sum_{i=1}^u (a_i+b_i)R_i} \left\{ \prod_{j=1}^h (af_j + g_j)^{-\sum_{i=1}^v K_i \lambda_i''' - \sum_{i=1}^u \lambda_i'' R_i} \right\} \quad (3.22)$$

$$\mathfrak{A} = A, A'; \mathfrak{B} = B, B' \quad (3.23)$$

We have the general Eulerian integral.

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1-\tau_j(t-a)^{h_i}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$S_L^{h_1, \dots, h_u} \left(\begin{array}{c} z_1'' \theta_1'' (t-a)^{a_1} (b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''^{(1)}} \\ \vdots \\ z_u'' \theta_u'' (t-a)^{a_u} (b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''^{(u)}} \end{array} \right)$$

$$S_{N_1, \dots, N_v}^{\mathfrak{M}_1, \dots, \mathfrak{M}_v} \left(\begin{array}{c} z_1''' \theta_1''' (t-a)^{a'_1} (b-t)^{b'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''^{(1)}} \\ \vdots \\ z_v''' \theta_v''' (t-a)^{a'_v} (b-t)^{b'_v} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''^{(v)}} \end{array} \right)$$

$$I \left(\begin{array}{c} z_1 \theta_1 (t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r (t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{array} \right)$$

$$I \left(\begin{array}{c} z'_1 \theta'_1 (t-a)^{\mu'_1} (b-t)^{\rho'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z'_s \theta'_s (t-a)^{\mu'_s} (b-t)^{\rho'_s} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(s)}} \end{array} \right) dt$$

$$= P_1 \sum_{K_1=0}^{[N_1/\mathfrak{M}_1]} \cdots \sum_{K_v=0}^{[N_v/\mathfrak{M}_v]} \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} a_v b_u B_{u,v} \prod_{k=1}^u z''^{R_k} \prod_{k=1}^v z'''^{K_k}$$

$$I_{U;p_r+p'_s+l+k+2,q_r+q'_s+l+k+1;Y}^{V;0,n_r+n'_s+l+k+2;X} \left(\begin{array}{c|ccc} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} & & A ; K_1, K_2, K_j, K'_j, \mathfrak{A} : A' \\ \cdot \cdot \cdot & & \cdot \\ \cdot \cdot \cdot & & \cdot \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(r)}}} & & \cdot \\ \frac{z'_1(b-a)^{\mu'_1+\rho'_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j{}^{(1)}}} & & \cdot \\ \cdot \cdot \cdot & & \cdot \\ \cdot \cdot \cdot & & \cdot \\ \frac{z'_s(b-a)^{\mu'_s+\rho'_s}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j{}^{(s)}}} & & \cdot \\ \tau_1(b-a)^{h_1} & & \cdot \\ \cdot \cdot \cdot & & \cdot \\ \cdot \cdot \cdot & & \cdot \\ \tau_l(b-a)^{h_l} & & \cdot \\ \frac{(b-a)f_1}{af_1+g_1} & & \cdot \\ \cdot \cdot \cdot & B ; L_1, L_j, L'_j : D_1, \mathfrak{B} : B' \\ \cdot \cdot \cdot & & \cdot \\ \frac{(b-a)f_k}{af_k+g_k} & & \end{array} \right) \quad (3.24)$$

We obtain the I-function of $r + s + k + l$ variables. The quantities $U, V, X, Y, A, B, K_1, K_2, K_j, K'_j, \mathfrak{A}, \mathfrak{A}', \mathfrak{A}_1, L_1, L_j, L'_j, \mathfrak{B}, \mathfrak{B}', P_1, B_u, B_{u,v}$ and \mathfrak{B}_1 are defined above.

Provided that

(A) $a, b \in \mathbb{R} (a < b); \mu_i, \mu'_u, \rho_i, \rho'_u, \lambda_j^{(i)}, \lambda_j^{(u)}, h_v \in \mathbb{R}^+, f_i, g_j, \tau_v, \sigma_j, \lambda_v \in \mathbb{C} \ (i = 1, \dots, r; j = 1, \dots, k;$

$$u = 1, \dots, s; v = 1, \dots, l, a_i, b_i, \lambda_j^{(i)}, \zeta_j^{(i)} \in \mathbb{R}^+, (i = 1, \dots, u; j = 1, \dots, k)$$
$$a'_i, b'_i, \lambda_i'''^{(i)}, \zeta_i'''^{(i)} \in \mathbb{R}^+, (i = 1, \dots, v; j = 1, \dots, k)$$
$$\textbf{(B)} \quad a_{ij}, b_{ik}, \in \mathbb{C} \ (i = 1, \cdots, r; j = 1, \cdots, p_i; k = 1, \cdots, q_i); a_j^{(i)}, b_j^{(k)} \in \mathbb{C}$$
$$(i = 1, \dots, r; j = 1, \dots, p^{(i)}; k = 1, \dots, q^{(i)})$$
$$a'_{ij}, b'_{ik}, \in \mathbb{C} \ (i = 1, \dots, s; j = 1, \dots, p'_i; k = 1, \dots, q'_i); a_j^{(i)}, b_j^{(k)}, \in \mathbb{C}$$
$$(i = 1, \cdots, r; j = 1, \cdots, p'^{(i)}; k = 1, \cdots, q'^{(i)})$$
$$\alpha_{ii}^{(k)}, \beta_{ii}^{(k)} \in \mathbb{R}^+ \ (i = 1, \dots, r, j = 1, \dots, p_i, k = 1, \dots, r); \alpha_i^{(i)}, \beta_i^{(i)} \in \mathbb{R}^+ \ (i = 1, \dots, r; j = 1, \dots, p_i)$$
$$\alpha_{ij}^{(k)}, \beta_{ij}'^{(k)} \in \mathbb{R}^+ ((i = 1, \dots, s, j = 1, \dots, p'_i, k = 1, \dots, s); \alpha_j'^{(i)}, \beta_i'^{(i)} \in \mathbb{R}^+ (i = 1, \dots, s; j = 1, \dots, p'_i)$$

$$(C) \max_{1 \leq j \leq k} \left\{ \left| \frac{(b-a)f_i}{af_i + g_i} \right| \right\} < 1, \max_{1 \leq j \leq l} \{ |\tau_j(b-a)^{h_j}| \} < 1$$

$$(D) Re \left[\alpha + \sum_{j=1}^r \mu_j \min_{1 \leq k \leq m^{(i)}} \frac{b_k^{(j)}}{\beta_k^{(j)}} + \sum_{j=1}^s \mu'_j \min_{1 \leq k \leq m'^{(i)}} \frac{b_k'^{(j)}}{\beta_k'^{(j)}} \right] > 0$$

$$Re \left[\beta + \sum_{j=1}^r \rho_j \min_{1 \leq k \leq m^{(i)}} \frac{b_k^{(j)}}{\beta_k^{(j)}} + \sum_{j=1}^s \rho'_j \min_{1 \leq k \leq m'^{(i)}} \frac{b_k'^{(j)}}{\beta_k'^{(j)}} \right] > 0$$

$$(E) Re \left(\alpha + \sum_{i=1}^v K_i a'_i + \sum_{i=1}^u R_i a_i + \sum_{i=1}^r \mu_i s_i + \sum_{i=1}^s t_i \mu'_i \right) > 0$$

$$Re \left(\beta + \sum_{i=1}^v K_i b'_i + \sum_{i=1}^u R_i b_i + \sum_{i=1}^r v_i s_i + \sum_{i=1}^s t_i \rho'_i \right) > 0$$

$$Re \left(\lambda_j + \sum_{i=1}^v K_i \lambda_j^{(i)} + \sum_{i=1}^u R_i \lambda_j^{(i)} + \sum_{i=1}^r s_i \zeta_j^{(i)} + \sum_{i=1}^s t_i \zeta_j'^{(i)} \right) > 0 (j = 1, \dots, l);$$

$$Re \left(-\sigma_j + \sum_{i=1}^v K_i \lambda_j^{(i)} + \sum_{i=1}^u R_i \lambda_j^{(i)} + \sum_{i=1}^r s_i \lambda_j^{(i)} + \sum_{i=1}^s t_i \lambda_j'^{(i)} \right) > 0 (j = 1, \dots, k)$$

$$(F) \Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left(\sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)} \right) + \dots +$$

$$\left(\sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)} \right) - \left(\sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \dots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)} \right) - \mu_i - \rho_i$$

$$- \sum_{l=1}^k \lambda_j^{(i)} - \sum_{l=1}^l \zeta_j^{(i)} > 0 \quad (i = 1, \dots, r)$$

$$\Omega'_i = \sum_{k=1}^{n'^{(i)}} \alpha'_k{}^{(i)} - \sum_{k=n'^{(i)}+1}^{p'^{(i)}} \alpha'_k{}^{(i)} + \sum_{k=1}^{m'^{(i)}} \beta'_k{}^{(i)} - \sum_{k=m'^{(i)}+1}^{q'^{(i)}} \beta'_k{}^{(i)} + \left(\sum_{k=1}^{n'_2} \alpha'_{2k}{}^{(i)} - \sum_{k=n'_2+1}^{p'_2} \alpha'_{2k}{}^{(i)} \right) +$$

$$\dots + \left(\sum_{k=1}^{n'_s} \alpha'_{sk}{}^{(i)} - \sum_{k=n'_s+1}^{p'_s} \alpha'_{sk}{}^{(i)} \right) - \left(\sum_{k=1}^{q'_2} \beta'_{2k}{}^{(i)} + \sum_{k=1}^{q'_3} \beta'_{3k}{}^{(i)} + \dots + \sum_{k=1}^{q'_s} \beta'_{sk}{}^{(i)} \right) - \mu'_i - \rho'_i$$

$$- \sum_{l=1}^k \lambda'_j{}^{(i)} - \sum_{l=1}^l \zeta'_j{}^{(i)} > 0 \quad (i = 1, \dots, s)$$

$$(G) \left| arg \left(z_i \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\zeta_j^{(i)}} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(i)}} \right) \right| < \frac{1}{2} \Omega_i \pi \quad (a \leq t \leq b; i = 1, \dots, r)$$

$$\left| \arg \left(z'_i \prod_{j=1}^l [1 - \tau'_j(t-a)^{h'_i}]^{-\zeta'^{(i)}} \prod_{j=1}^k (f_j t + g_j)^{-\lambda'^{(i)}} \right) \right| < \frac{1}{2} \Omega'_i \pi \quad (a \leq t \leq b; i = 1, \dots, s)$$

Proof

To prove (3.24), first expressing a class of multivariable polynomials $S_{N_1, \dots, N_v}^{\mathfrak{M}_1, \dots, \mathfrak{M}_v}[\cdot]$ defined by Srivastava [3] in serie with the help of (1.7), a class of multivariable polynomials $S_L^{h_1, \dots, h_u}[\cdot]$ defined by Srivastava et al [5] in serie with the help of (1.8) and we interchange the order of summations and t-integral (which is permissible under the conditions stated). Expressing the I-functions of r-variables and s-variables defined by Prasad [1] in terms of Mellin-Barnes type contour integral with the help of (1.2) and (1.4) respectively and interchange the order of integrations which is justifiable due to absolute convergence of the integral involved in the process. Now collect the power of $[1 - \tau_j(t-a)^{h_i}]$ with $(i = 1, \dots, r; j = 1, \dots, l)$ and collect the power of $(f_j t + g_j)$ with $j = 1, \dots, k$. Use the equations (2.2) and (2.3) and express the result in Mellin-Barnes contour integral. Interpreting the $(r + s + k + l)$ dimensional Mellin-Barnes integral in multivariable I-function defined by Prasad [1], we obtain the equation (3.24).

Remarks

If a) $\rho_1 = \dots, \rho_r = \rho'_1 = \dots, \rho'_s = 0$; b) $\mu_1 = \dots, \mu_r = \mu'_1 = \dots, \mu'_s = 0$, we obtain the similar formulas that (3.24) with the corresponding simplifications.

4. Particular cases

a) If $U = V = A = B = 0$, the multivariable I-functions defined by Prasad [1] reduce to multivariable H-function defined by Srivastava et al [7]. We obtain.

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$S_L^{h_1, \dots, h_u} \left(\begin{matrix} z_1'' \theta_1''(t-a)^{a_1} (b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''(1)} \\ \vdots \\ z_u'' \theta_u''(t-a)^{a_u} (b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''(u)} \end{matrix} \right)$$

$$S_{N_1, \dots, N_v}^{\mathfrak{M}_1, \dots, \mathfrak{M}_v} \left(\begin{matrix} z_1''' \theta_1'''(t-a)^{a'_1} (b-t)^{b'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''(1)} \\ \vdots \\ z_v''' \theta_v'''(t-a)^{a'_v} (b-t)^{b'_v} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''(v)} \end{matrix} \right)$$

$$H \left(\begin{matrix} z_1 \theta_1(t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r(t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{matrix} \right)$$

$$H \begin{pmatrix} z'_1 \theta'_1 (t-a)^{\mu'_1} (b-t)^{\rho'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda'_j(1)} \\ \vdots \\ z'_s \theta'_s (t-a)^{\mu'_s} (b-t)^{\rho'_s} \prod_{j=1}^k (f_j t + g_j)^{-\lambda'_j(s)} \end{pmatrix} dt$$

$$= P_1 \sum_{K_1=0}^{[N_1/\mathfrak{M}_1]} \cdots \sum_{K_v=0}^{[N_v/\mathfrak{M}_v]} h_1 R_1 + \cdots h_u R_u \leq L \sum_{R_1, \dots, R_u=0} a_v b_u B_{u,v} \prod_{k=1}^u z''^{R_k} \prod_{k=1}^v z'''^{K_k}$$

$$H_{p_r+n'_s+l+k+2;X}^{0,n_r+n'_s+l+k+2;q_r+q'_s+l+k+1;Y} \left(\begin{array}{c|c} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} & K_1, K_2, K_j, K'_j, \mathfrak{A} : A' \\ \vdots & \vdots \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(r)}}} & \vdots \\ \frac{z'_1(b-a)^{\mu'_1+\rho'_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j(1)}} & \vdots \\ \vdots & \vdots \\ \frac{z'_s(b-a)^{\mu'_s+\rho'_s}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j(s)}} & \vdots \\ \tau_1(b-a)^{h_1} & \vdots \\ \vdots & \vdots \\ \tau_l(b-a)^{h_l} & \vdots \\ \frac{(b-a)f_1}{af_1+g_1} & \vdots \\ \vdots & \vdots \\ \frac{(b-a)f_k}{af_k+g_k} & L_1, L_j, L'_j : D_1, \mathfrak{B} : B' \end{array} \right) \quad (4.1)$$

under the same notations and conditions that (3.25) with $U = V = A = B = 0$

$$\text{b) If } B(L; R_1, \dots, R_u) = \frac{\prod_{j=1}^{\bar{A}} (a_j)_{R_1 \theta'_j + \dots + R_u \theta_j^{(u)}} \prod_{j=1}^{B'} (b'_j)_{R_1 \phi'_j} \cdots \prod_{j=1}^{B^{(u)}} (b_j^{(u)})_{R_u \phi_j^{(u)}}}{\prod_{j=1}^{\bar{C}} (c_j)_{R_1 \psi'_j + \dots + R_u \psi_j^{(u)}} \prod_{j=1}^{D'} (d'_j)_{R_1 \delta'_j} \cdots \prod_{j=1}^{D^{(u)}} (d_j^{(u)})_{R_u \delta_j^{(u)}}} \quad (4.2)$$

then the general class of multivariable polynomial $S_L^{h_1, \dots, h_u} [z_1, \dots, z_u]$ reduces to generalized Lauricella function

defined by Srivastava et al [5]. We have

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1-\tau_j(t-a)^{h_j}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$F_{\bar{C}:D';\dots;D^{(u)}}^{1+\bar{A}:B';\dots;B^{(u)}} \left(\begin{matrix} z_1''\theta_1''(t-a)^{a_1}(b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''^{(1)}} \\ \vdots \\ z_u''\theta_u''(t-a)^{a_u}(b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''^{(u)}} \end{matrix} \right)$$

$$\left[(-L); R_1, \dots, R_u \right] [(a); \theta', \dots, \theta^{(u)}] : [(b'); \phi']; \dots; [(b^{(u)}); \phi^{(u)}] \\ [(c); \psi', \dots, \psi^{(u)}] : [(d'); \delta']; \dots; [(d^{(u)}); \delta^{(u)}]$$

$$S_{N_1,\dots,N_v}^{\mathfrak{M}_1,\dots,\mathfrak{M}_v} \left(\begin{matrix} z_1''' \theta_1''' (t-a)^{a_1'} (b-t)^{b_1'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''^{(1)}} \\ \vdots \\ z_v''' \theta_v''' (t-a)^{a_v'} (b-t)^{b_v'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''^{(v)}} \end{matrix} \right)$$

$$I \left(\begin{matrix} z_1 \theta_1 (t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r (t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{matrix} \right)$$

$$I \left(\begin{matrix} z_1' \theta_1' (t-a)^{\mu_1'} (b-t)^{\rho_1'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z_s' \theta_s' (t-a)^{\mu_s'} (b-t)^{\rho_s'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(s)}} \end{matrix} \right) dt$$

$$= P_1 \sum_{K_1=0}^{[N_1/\mathfrak{M}_1]} \cdots \sum_{K_v=0}^{[N_v/\mathfrak{M}_v]} h_1 R_1 + \cdots h_u R_u \leq L \sum_{R_1, \dots, R_u=0} a_v b_u B_{u,v} \prod_{k=1}^u z''^{R_k} \prod_{k=1}^v z'''^{K_k}$$

$$I_{U;p_r+p'_s+l+k+2,q_r+q'_s+l+k+1;Y}^{V;0,n_r+n'_s+l+k+2;X} \left(\begin{array}{c|c} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} & A ; K_1, K_2, K_j, K'_j, \mathfrak{A} : A' \\ \cdot & \cdot \\ \cdot & \cdot \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(r)}}} & \cdot \\ \frac{z'_1(b-a)^{\mu'_1+\rho'_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j'^{(1)}}} & \cdot \\ \cdot & \cdot \\ \cdot & \cdot \\ \frac{z'_s(b-a)^{\mu'_s+\rho'_s}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j'^{(s)}}} & \cdot \\ \tau_1(b-a)^{h_1} & \cdot \\ \cdot & \cdot \\ \cdot & \cdot \\ \tau_l(b-a)^{h_l} & \cdot \\ \frac{(b-a)f_1}{af_1+g_1} & \cdot \\ \cdot & B ; L_1, L_j, L'_j : D_1, \mathfrak{B} : B' \\ \cdot & \cdot \\ \frac{(b-a)f_k}{af_k+g_k} & \cdot \end{array} \right) \quad (4.3)$$

under the same conditions and notations that (3.24)

$$\text{where } b'_u = \frac{(-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u)}{R_1! \dots R_u!}, B[E; R_1, \dots, R_v] \text{ is defined by (4.2)}$$

Remark:

By the following similar procedure, the results of this document can be extended a class of multivariable polynomials defined by Srivastava et al [5] and Srivastava [3].

5. Conclusion

In this paper we have evaluated a generalized Eulerian integral involving the product of two multivariable I-functions defined by Prasad [1] and classes of multivariable polynomials defined by Srivastava [3] and Srivastava et al [5] with general arguments. The formulae established in this paper is very general nature. Thus, the results established in this research work would serve as a key formula from which, upon specializing the parameters, as many as desired results involving the special functions of one and several variables can be obtained.

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Personal adress : 411 Avenue Joseph Raynaud
Le parc Fleuri , Bat B
83140 , Six-Fours les plages
Tel : 06-83-12-49-68
Department : VAR
Country : FRANCE