

# Eulerian integral associated with product of two multivariable I-functions, a class of polynomials and the multivariable A-function

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**ABSTRACT**

The present paper is evaluated a new Eulerian integral associated with the product of two multivariable I-functions defined by Prasad [2] a generalized Lauricella function , a class of multivariable polynomials and multivariable A-function with general arguments . We will study the case concerning the multivariable H-function defined by Srivastava et al [8] and Srivastava-Daoust polynomial [5].

Keywords: Eulerian integral, multivariable I-function, generalized Lauricella function of several variables, multivariable A-function, generalized hypergeometric function, class of polynomials

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## 1. Introduction

In this paper, we evaluate a new Eulerian integral of most general characters associated with the products of two multivariable I-functions defined by Prasad [2], the A-function of several variables and a class of polynomials with general arguments. The A-function of several variables is an extension of multivariable H-function defined by Srivastava et al [8].

The serie representation of the multivariable A-function is given by Gautam [1] as

$$A[u_1, \dots, u_v] = A_{A,C:(M',N');\dots;(M^{(v)},N^{(v)})}^{0,\lambda:(\alpha',\beta');\dots;(\alpha^{(v)},\beta^{(v)})} \left( \begin{matrix} u_1 \\ \cdot \\ \cdot \\ u_v \end{matrix} \middle| \begin{matrix} [(g_j); \gamma', \dots, \gamma^{(v)}]_{1,A} : \\ \cdot \\ \cdot \\ [(f_j); \xi', \dots, \xi^{(v)}]_{1,C} : \end{matrix} \right)$$

$$\left( \begin{matrix} (q^{(1)}, \eta^{(1)})_{1,M^{(1)}}; \dots; (q^{(v)}, \eta^{(v)})_{1,M^{(v)}} \\ \cdot \\ \cdot \\ (p^{(1)}, \epsilon^{(1)})_{1,N^{(1)}}; \dots; (p^{(v)}, \epsilon^{(v)})_{1,N^{(v)}} \end{matrix} \right) = \sum_{G_i=1}^{\alpha^{(i)}} \sum_{g_i=1}^{\infty} \phi_1 \frac{\prod_{i=1}^v \phi_i u_i^{\eta_{G_i, g_i}} (-)^{\sum_{i=1}^v g_i}}{\prod_{i=1}^v \epsilon_{G_i}^{(i)} g_i!} \tag{1.1}$$

where

$$\phi_1 = \frac{\prod_{j=1}^{\lambda} \Gamma(1 - g_j + \sum_{i=1}^v \gamma_j^{(i)} \eta_{G_i, g_i})}{\prod_{j=\lambda'+1}^A \Gamma(g_j - \sum_{i=1}^v \gamma_j^{(i)} U_i) \prod_{j=1}^C \Gamma(1 - f_j + \sum_{i=1}^v \xi_j^{(i)} \eta_{G_i, g_i})} \tag{1.2}$$

$$\phi_i = \frac{\prod_{j=1, j \neq m_i}^{\alpha^{(i)}} \Gamma(p_j^{(i)} - \epsilon_j^{(i)} \eta_{G_i, g_i}) \prod_{j=1}^{\beta^{(i)}} \Gamma(1 - q_j^{(i)} + \eta_j^{(i)} \eta_{G_i, g_i})}{\prod_{j=\alpha^{(i)}+1}^{N^{(i)}} \Gamma(1 - p_j^{(i)} + \epsilon_j^{(i)} \eta_{G_i, g_i}) \prod_{j=\beta^{(i)}+1}^{M^{(i)}} \Gamma(q_j^{(i)} - \eta_j^{(i)} \eta_{G_i, g_i})}, i = 1, \dots, v \tag{1.3}$$

and  $\eta_{G_i, g_i} = \frac{p_{G_i}^{(i)} + g_i}{\epsilon_{G_i}^{(i)}}, i = 1, \dots, v$  (1.4)

which is valid under the following conditions :  $\epsilon_{m_i}^{(i)} [p_j^{(i)} + p'_i] \neq \epsilon_j^{(i)} [p_{m_i} + g_i]$  (1.5)  
and

$$u_i \neq 0, \sum_{j=1}^A \gamma_j^{(i)} - \sum_{j=1}^C \xi_j^{(i)} + \sum_{j=1}^{M^{(i)}} \eta_j^{(i)} - \sum_{j=1}^{N^{(i)}} \epsilon_j^{(i)} < 0, i = 1, \dots, v \tag{1.6}$$

Here  $\lambda, A, C, \alpha_i, \beta_i, M_i, N_i \in \mathbb{N}^*$ ;  $i = 1, \dots, v$ ;  $f_j, g_j, p_j^{(i)}, q_j^{(i)}, \gamma_j^{(i)}, \xi_j^{(i)}, \eta_j^{(i)}, \epsilon_j^{(i)} \in \mathbb{C}$

The multivariable I-function of r-variables is defined in term of multiple Mellin-Barnes type integral :

$$I(z_1, \dots, z_r) = I_{p_2, q_2, p_3, q_3; \dots; p_r, q_r; p^{(1)}, q^{(1)}; \dots; p^{(r)}, q^{(r)}}^{0, n_2; 0, n_3; \dots; 0, n_r; m^{(1)}, n^{(1)}; \dots; m^{(r)}, n^{(r)}} \left( \begin{matrix} z_1 \\ \cdot \\ \cdot \\ \cdot \\ z_r \end{matrix} \middle| \begin{matrix} (a_{2j}; \alpha'_{2j}, \alpha''_{2j})_{1, p_2}; \dots; \\ \\ \\ (b_{2j}; \beta'_{2j}, \beta''_{2j})_{1, q_2}; \dots; \end{matrix} \right)$$

$$\left( \begin{matrix} (a_{rj}; \alpha_{rj}^{(1)}, \dots, \alpha_{rj}^{(r)})_{1, p_r}; (a_j^{(1)}, \alpha_j^{(1)})_{1, p^{(1)}}; \dots; (a_j^{(r)}, \alpha_j^{(r)})_{1, p^{(r)}} \\ (b_{rj}; \beta_{rj}^{(1)}, \dots, \beta_{rj}^{(r)})_{1, q_r}; (b_j^{(1)}, \beta_j^{(1)})_{1, q^{(1)}}; \dots; (b_j^{(r)}, \beta_j^{(r)})_{1, q^{(r)}} \end{matrix} \right) \tag{1.7}$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_1} \dots \int_{L_r} \phi(s_1, \dots, s_r) \prod_{i=1}^r \theta_i(s_i) z_i^{s_i} ds_1 \dots ds_r \tag{1.8}$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [2]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

$|arg z_i| < \frac{1}{2} \Omega_i \pi$ , where

$$\Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left( \sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)} \right) + \dots +$$

$$\left( \sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)} \right) - \left( \sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \dots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)} \right) \tag{1.9}$$

where  $i = 1, \dots, r$

The complex numbers  $z_i$  are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the the asymptotic expansion in the following convenient form :

$$I(z_1, \dots, z_r) = O(|z_1|^{\alpha_1}, \dots, |z_r|^{\alpha_r}), \max(|z_1|, \dots, |z_r|) \rightarrow 0$$

$$I(z_1, \dots, z_r) = 0(|z_1|^{\beta_1}, \dots, |z_r|^{\beta_r}), \min(|z_1|, \dots, |z_r|) \rightarrow \infty$$

where  $k = 1, \dots, r : \alpha'_k = \min[\operatorname{Re}(b_j^{(k)})/\beta_j^{(k)}], j = 1, \dots, m_k$  and

$$\beta'_k = \max[\operatorname{Re}((a_j^{(k)} - 1)/\alpha_j^{(k)}), j = 1, \dots, n_k$$

Consider a second multivariable I-function defined by Prasad [2]

$$I(z'_1, \dots, z'_s) = I_{\substack{0, n'_2; 0, n'_3; \dots; 0, n'_r; m'^{(1)}, n'^{(1)}; \dots; m'^{(s)}, n'^{(s)} \\ p'_2, q'_2, p'_3, q'_3; \dots; p'_s, q'_s; p'^{(1)}, q'^{(1)}; \dots; p'^{(s)}, q'^{(s)}}} \left( \begin{array}{c} z'_1 \\ \cdot \\ \cdot \\ \cdot \\ z'_s \end{array} \middle| \begin{array}{l} (a'_{2j}; \alpha'_{2j}{}^{(1)}, \alpha'_{2j}{}^{(2)})_{1, p'_2}; \dots; \\ (b'_{2j}; \beta'_{2j}{}^{(1)}, \beta'_{2j}{}^{(2)})_{1, q'_2}; \dots; \end{array} \right.$$

$$\left. \begin{array}{l} (a'_{sj}; \alpha'_{sj}{}^{(1)}, \dots, \alpha'_{sj}{}^{(s)})_{1, p'_s} : (a'_j{}^{(1)}, \alpha'_j{}^{(1)})_{1, p'^{(1)}}; \dots; (a'_j{}^{(s)}, \alpha'_j{}^{(s)})_{1, p'^{(s)}} \\ (b'_{sj}; \beta'_{sj}{}^{(1)}, \dots, \beta'_{sj}{}^{(s)})_{1, q'_s} : (b'_j{}^{(1)}, \beta'_j{}^{(1)})_{1, q'^{(1)}}; \dots; (b'_j{}^{(s)}, \beta'_j{}^{(s)})_{1, q'^{(s)}} \end{array} \right) \tag{1.10}$$

$$= \frac{1}{(2\pi\omega)^s} \int_{L_1} \dots \int_{L_s} \psi(t_1, \dots, t_s) \prod_{i=1}^s \xi_i(t_i) z_i^{t_i} dt_1 \dots dt_s \tag{1.11}$$

The defined integral of the above function, the existence and convergence conditions, see Y,N Prasad [2]. Throughout the present document, we assume that the existence and convergence conditions of the multivariable I-function.

The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H-function given by as :

where  $|\arg z'_i| < \frac{1}{2} \Omega'_i \pi$ ,

$$\begin{aligned} \Omega'_i &= \sum_{k=1}^{n'^{(i)}} \alpha'_k{}^{(i)} - \sum_{k=n'^{(i)}+1}^{p'^{(i)}} \alpha'_k{}^{(i)} + \sum_{k=1}^{m'^{(i)}} \beta'_k{}^{(i)} - \sum_{k=m'^{(i)}+1}^{q'^{(i)}} \beta'_k{}^{(i)} + \left( \sum_{k=1}^{n'_2} \alpha'_{2k}{}^{(i)} - \sum_{k=n_2+1}^{p'_2} \alpha'_{2k}{}^{(i)} \right) \\ &+ \dots + \left( \sum_{k=1}^{n'_s} \alpha'_{sk}{}^{(i)} - \sum_{k=n'_s+1}^{p'_s} \alpha'_{sk}{}^{(i)} \right) - \left( \sum_{k=1}^{q'_2} \beta'_{2k}{}^{(i)} + \sum_{k=1}^{q'_3} \beta'_{3k}{}^{(i)} + \dots + \sum_{k=1}^{q'_s} \beta'_{sk}{}^{(i)} \right) \end{aligned} \tag{1.12}$$

where  $i = 1, \dots, s$

The complex numbers  $z_i$  are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable I-function.

We may establish the the asymptotic expansion in the following convenient form :

$$I(z'_1, \dots, z'_s) = 0(|z'_1|^{\alpha'_1}, \dots, |z'_s|^{\alpha'_s}), \max(|z'_1|, \dots, |z'_s|) \rightarrow 0$$

$$I(z'_1, \dots, z'_s) = 0(|z'_1|^{\beta'_1}, \dots, |z'_s|^{\beta'_s}), \min(|z'_1|, \dots, |z'_s|) \rightarrow \infty$$

where  $k = 1, \dots, z : \alpha''_k = \min[Re(b_j^{(k)}/\beta_j^{(k)})], j = 1, \dots, m'_k$  and

$$\beta''_k = \max[Re((a_j^{(k)} - 1)/\alpha_j^{(k)})], j = 1, \dots, n'_k$$

where  $k = 1, \dots, z : \alpha''_k = \min[Re(b_j^{(k)}/\beta_j^{(k)})], j = 1, \dots, m'_k$  and

$$\beta''_k = \max[Re((a_j^{(k)} - 1)/\alpha_j^{(k)})], j = 1, \dots, n'_k$$

Srivastava and Garg [6] introduced and defined a general class of multivariable polynomials as follows

$$S_L^{h_1, \dots, h_u} [z_1, \dots, z_u] = \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} (-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u) \frac{z_1^{R_1} \dots z_u^{R_u}}{R_1! \dots R_u!} \quad (1.13)$$

The coefficients are  $B[E; R_1, \dots, R_u]$  arbitrary constants, real or complex.

## 2. Integral representation of generalized Lauricella function of several variables

The following generalized hypergeometric function in terms of multiple contour integrals is also required [7, page 39 eq.30]

$$\frac{\prod_{j=1}^P \Gamma(A_j)}{\prod_{j=1}^Q \Gamma(B_j)} {}_P F_Q [(A_P); (B_Q); -(x_1 + \dots + x_r)]$$

$$= \frac{1}{(2\pi\omega)^r} \int_{L_1} \dots \int_{L_r} \frac{\prod_{j=1}^P \Gamma(A_j + s_1 + \dots + s_r)}{\prod_{j=1}^Q \Gamma(B_j + s_1 + \dots + s_r)} \Gamma(-s_1) \dots \Gamma(-s_r) x_1^{s_1} \dots x_r^{s_r} ds_1 \dots ds_r \quad (2.1)$$

where the contours are of Barnes type with indentations, if necessary, to ensure that the poles of  $\Gamma(A_j + s_1 + \dots + s_r)$  are separated from those of  $\Gamma(-s_j), j = 1, \dots, r$ . The above result (1.23) can be easily established by an appeal to the calculus of residues by calculating the residues at the poles of  $\Gamma(-s_j), j = 1, \dots, r$

In order to evaluate a number of integrals of multivariable I-function, we first establish the formula

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1 - \tau_j (t-a)^{h_j}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j} dt = (b-a)^{\alpha+\beta-1} B(\alpha, \beta) \prod_{j=1}^k (af_j + g_j)^{\sigma_j}$$

$$F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1} \left( \begin{matrix} (\alpha : h_1, \dots, h_l, 1, \dots, 1) : (\lambda_1 : 1), \dots, (\lambda_l : 1); (-\sigma_1 : 1), \dots, (-\sigma_k : 1) \\ \dots \\ (\alpha + \beta : h_1, \dots, h_l, 1, \dots, 1) : -, \dots, -; -, \dots, - \end{matrix} \right)$$

$$; \tau_1(b-a)^{h_1}, \dots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1+g_1}, \dots, -\frac{(b-a)f_k}{af_k+g_k} \tag{2.2}$$

where  $a, b \in \mathbb{R}(a < b), \alpha, \beta, f_i, g_i, \sigma_i, \tau_j, h_j \in \mathbb{C}, \lambda_j \in \mathbb{R}^+(i = 1, \dots, k; j = 1, \dots, l)$

$$\min(\operatorname{Re}(\alpha), \operatorname{Re}(\beta)) > 0, \max_{1 \leq j \leq l} \{|\tau_j(b-a)^{h_j}|\} < 1, \max_{1 \leq j \leq k} \left\{ \left| \frac{(b-a)f_i}{af_i+g_i} \right| \right\} < 1,$$

and  $F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1}$  is a particular case of the generalized Lauricella function introduced by Srivastava-Daoust [5, page 454] given by :

$$F_{1:0, \dots, 0; 0, \dots, 0}^{1:1, \dots, 1; 1, \dots, 1} \left( \begin{matrix} (\alpha : h_1, \dots, h_l, 1, \dots, 1) : (\lambda_1 : 1), \dots, (\lambda_l : 1); (-\sigma_1 : 1), \dots, (-\sigma_k : 1) \\ \dots \\ (\alpha + \beta : h_1, \dots, h_l, 1, \dots, 1) : -, \dots, -; -, \dots, - \end{matrix} \right)$$

$$; \tau_1(b-a)^{h_1}, \dots, \tau_l(b-a)^{h_l}, -\frac{(b-a)f_1}{af_1+g_1}, \dots, -\frac{(b-a)f_k}{af_k+g_k} \Bigg) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha) \prod_{j=1}^l \Gamma(\lambda_j) \prod_{j=1}^k \Gamma(-\sigma_j)}$$

$$\frac{1}{(2\pi\omega)^{l+k}} \int_{L_1} \dots \int_{L_{l+k}} \frac{\Gamma\left(\alpha + \sum_{j=1}^l h_j s_j + \sum_{j=1}^k s_{l+j}\right)}{\Gamma\left(\alpha + \beta + \sum_{j=1}^l h_j s_j + \sum_{j=1}^k s_{l+j}\right)} \prod_{j=1}^l \Gamma(\lambda_j + s_j) \prod_{j=1}^k \Gamma(-\sigma_j + s_{l+j})$$

$$\prod_{j=1}^{l+k} \Gamma(-s_j) z_1^{s_1} \dots z_l^{s_l} z_{l+1}^{s_{l+1}} \dots, z_{l+k}^{s_{l+k}} ds_1 \dots ds_{l+k} \tag{2.3}$$

Here the contour  $L'_j s$  are defined by  $L_j = L_{w\zeta_j\infty}(\operatorname{Re}(\zeta_j) = v''_j)$  starting at the point  $v''_j - \omega\infty$  and terminating at the point  $v''_j + \omega\infty$  with  $v''_j \in \mathbb{R}(j = 1, \dots, l)$  and each of the remaining contour  $L_{l+1}, \dots, L_{l+k}$  run from  $-\omega\infty$  to  $\omega\infty$

(2.2) can be easily established by expanding  $\prod_{j=1}^l [1 - \tau_j(t-a)^{h_j}]^{-\lambda_j}$  by means of the formula :

$$(1-z)^{-\alpha} = \sum_{r=0}^{\infty} \frac{(\alpha)_r}{r!} z^r (|z| < 1) \tag{2.4}$$

integrating term by term with the help of the integral given by Saigo and Saxena [3, page 93, eq.(3.2)] and applying the definition of the generalized Lauricella function [5, page 454].

### 3. Eulerian integral

In this section , we note :

$$\theta_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_j}]^{-\zeta_j^{(i)}}, \zeta_j^{(i)} > 0 (i = 1, \dots, r); \theta'_i = \prod_{j=1}^l [1 - \tau_j(t-a)^{h_j}]^{-\zeta_j^{(i)'}}, \zeta_j^{(i)'} > 0 (i = 1, \dots, s)$$

$$\theta_i'' = \prod_{j=1}^l [1 - \tau_j(t - a)^{h_i}]^{-\zeta_j''(i)}, \zeta_j''(i) > 0 (i = 1, \dots, u)$$

$$\theta_i''' = \prod_{j=1}^l [1 - \tau_j(t - a)^{h_i}]^{-\zeta_j'''(i)}, \zeta_j'''(i) > 0 (i = 1, \dots, v) \tag{3.1}$$

$$U = p_2, q_2; p_3, q_3; \dots; p_{r-1}, q_{r-1}; p_2', q_2'; p_3', q_3'; \dots; p_{s-1}', q_{s-1}'; 0, 0; \dots; 0, 0; 0, 0; \dots; 0, 0 \tag{3.2}$$

$$V = 0, n_2; 0, n_3; \dots; 0, n_{r-1}; 0, n_2'; 0, n_3'; \dots; 0, n_{s-1}'; 0, 0; \dots; 0, 0; 0, 0; \dots; 0, 0 \tag{3.3}$$

$$X = m^{(1)}, n^{(1)}; \dots; m^{(r)}, n^{(r)}; m'^{(1)}, n'^{(1)}; \dots; m'^{(s)}, n'^{(s)}; 1, 0; \dots; 1, 0; 1, 0; \dots; 1, 0 \tag{3.4}$$

$$Y = p^{(1)}, q^{(1)}; \dots; p^{(r)}, q^{(r)}; p'^{(1)}, q'^{(1)}; \dots; p'^{(s)}, q'^{(s)}; 0, 1; \dots; 0, 1; 0, 1; \dots; 0, 1 \tag{3.5}$$

$$A = (a_{2k}; \alpha_{2k}^{(1)}, \alpha_{2k}^{(2)})_{1,p_2}; \dots; (a_{(s-1)k}; \alpha_{(s-1)k}^{(1)}, \alpha_{(s-1)k}^{(2)}, \dots, \alpha_{(s-1)k}^{(s-1)})_{1,p_{s-1}}; (a'_{2k}; \alpha'_{2k}^{(1)}, \alpha'_{2k}^{(2)})_{1,p'_2}; \dots; (a'_{(u-1)k}; \alpha'_{(u-1)k}^{(1)}, \alpha'_{(u-1)k}^{(2)}, \dots, \alpha'_{(u-1)k}^{(u-1)})_{1,p'_{u-1}} \tag{3.6}$$

$$B = (b_{2k}; \beta_{2k}^{(1)}, \beta_{2k}^{(2)})_{1,q_2}; \dots; (b_{(s-1)k}; \beta_{(s-1)k}^{(1)}, \beta_{(s-1)k}^{(2)}, \dots, \beta_{(s-1)k}^{(s-1)})_{1,q_{s-1}}; (b'_{2k}; \beta'_{2k}^{(1)}, \beta'_{2k}^{(2)})_{1,q'_2}; \dots; (b'_{(u-1)k}; \beta'_{(u-1)k}^{(1)}, \beta'_{(u-1)k}^{(2)}, \dots, \beta'_{(u-1)k}^{(u-1)})_{1,q'_{u-1}} \tag{3.7}$$

$$\mathfrak{A} = (a_{sk}; \alpha_{sk}^{(1)}, \alpha_{sk}^{(2)}, \dots, \alpha_{sk}^{(s)}, 0, \dots, 0, 0, \dots, 0, 0, \dots, 0)_{1,p_s} \tag{3.8}$$

$$\mathfrak{A}' = (a'_{uk}; 0, \dots, 0, \alpha'_{uk}^{(1)}, \alpha'_{uk}^{(2)}, \dots, \alpha'_{uk}^{(u)}, 0, \dots, 0, 0, \dots, 0)_{1,p'_u} \tag{3.9}$$

$$\mathfrak{B} = (b_{sk}; \beta_{sk}^{(1)}, \beta_{sk}^{(2)}, \dots, \beta_{sk}^{(s)}, 0, \dots, 0, 0, \dots, 0, 0, \dots, 0)_{1,q_s} \tag{3.10}$$

$$\mathfrak{B}' = (b'_{uk}; 0, \dots, 0, \beta'_{uk}^{(1)}, \beta'_{uk}^{(2)}, \dots, \beta'_{uk}^{(u)}, 0, \dots, 0, 0, \dots, 0)_{1,q'_u} \tag{3.11}$$

$$\mathfrak{A}_1 = (a_k^{(1)}, \alpha_k^{(1)})_{1,p^{(1)}}; \dots; (a_k^{(r)}, \alpha_k^{(r)})_{1,p^{(r)}}; (a_k'^{(1)}, \alpha_k'^{(1)})_{1,p'^{(1)}}; \dots; (a_k'^{(s)}, \alpha_k'^{(s)})_{1,p'^{(s)}}; (1, 0); \dots; (1, 0); (1, 0); \dots; (1, 0) \tag{3.12}$$

$$\mathfrak{B}_1 = (b_k^{(1)}, \beta_k^{(1)})_{1,q^{(1)}}; \dots; (b_k^{(r)}, \beta_k^{(r)})_{1,q^{(r)}}; (b_k'^{(1)}, \beta_k'^{(1)})_{1,q'^{(1)}}; \dots; (b_k'^{(s)}, \beta_k'^{(s)})_{1,q'^{(s)}}; (0, 1); \dots; (0, 1); (0, 1); \dots; (0, 1) \tag{3.13}$$

$$K_1 = (1 - \alpha - \sum_{i=1}^u R_i a_i - \sum_{i=1}^v \eta_{G_i, g_i} a'_i; \mu_1, \dots, \mu_r, \mu'_1, \dots, \mu'_s, h_1, \dots, h_l, 1, \dots, 1) \quad (3.14)$$

$$K_2 = (1 - \beta - \sum_{i=1}^u R_i b_i - \sum_{i=1}^v \eta_{G_i, g_i} b'_i; \rho_1, \dots, \rho_r, \rho'_1, \dots, \rho'_s, 0, \dots, 0, 0 \dots, 0) \quad (3.15)$$

$$K_j = [1 - \lambda_j - \sum_{i=1}^u R_i \zeta_j^{(i)} - \sum_{i=1}^v \eta_{G_i, g_i} \zeta_j^{(i)}; \zeta_j^{(1)}, \dots, \zeta_j^{(r)}, \zeta_j^{(1)} \dots, \zeta_j^{(s)}, 0, \dots, 1, \dots, 0, 0 \dots, 0]_{1,l} \quad (3.16)$$

$$K'_j = [1 + \sigma_j - \sum_{i=1}^u R_i \lambda_j^{(i)} - \sum_{i=1}^v \eta_{G_i, g_i} \lambda_j^{(i)}; \lambda_j^{(1)}, \dots, \lambda_j^{(r)}, \lambda_j^{(1)} \dots, \lambda_j^{(s)}, 0, \dots, 0, 0 \dots, 1, \dots, 0]_{1,k} \quad (3.17)$$

$$L_1 = (1 - \alpha - \beta - \sum_{i=1}^u R_i (a_i + b_i) - \sum_{i=1}^v (a'_i + b'_i) \eta_{G_i, g_i}; \mu_1 + \rho_1, \dots, \mu_r + \rho_r, \mu'_1 + \rho'_1, \dots, \mu'_r + \rho'_r, h_1, \dots, h_l, 1, \dots, 1) \quad (3.18)$$

$$L_j = [1 - \lambda_j - \sum_{i=1}^u R_i \zeta_j^{(i)} - \sum_{i=1}^s \zeta_j^{(i)} \eta_{G_i, g_i}; \zeta_j^{(1)}, \dots, \zeta_j^{(r)}, \zeta_j^{(1)} \dots, \zeta_j^{(s)}, 0, \dots, 0, 0 \dots, 0]_{1,l} \quad (3.19)$$

$$L'_j = [1 + \sigma_j - \sum_{i=1}^u R_i \lambda_j^{(i)} - \sum_{i=1}^v \lambda_j^{(i)} \eta_{G_i, g_i}; \lambda_j^{(1)}, \dots, \lambda_j^{(r)}, \lambda_j^{(1)} \dots, \lambda_j^{(s)}, 0, \dots, 0, 0 \dots, 0]_{1,k} \quad (3.20)$$

$$P_1 = (b - a)^{\alpha + \beta - 1} \left\{ \prod_{j=1}^h (af_j + g_j)^{\sigma_j} \right\} \quad (3.21)$$

$$B_{u,v} = (b - a)^{\sum_{i=1}^v (a'_i + b'_i) \eta_{G_i, g_i} + \sum_{i=1}^u (a_i + b_i) R_i} \left\{ \prod_{j=1}^h (af_j + g_j)^{-\sum_{i=1}^v \lambda_i^{(i)} \eta_{G_i, g_i} - \sum_{i=1}^u \lambda_i^{(i)} R_i} \right\} G_v \quad (3.22)$$

where  $G_v = \phi_1 \frac{\prod_{i=1}^v \phi_i u_i^{\eta_{G_i, g_i}} (-)^{\sum_{i=1}^v g_i}}{\prod_{i=1}^v \epsilon_{G_i}^{(i)} g_i!}$

$\phi_1, \phi_i$  for  $i = 1, \dots, v$  are defined respectively by (1.2) and (1.3)

$$B_u = \frac{(-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u)}{R_1! \dots R_u!} \tag{3.23}$$

We have the general Eulerian integral.

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1 - \tau_j (t-a)^{h_j}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$S_L^{h_1, \dots, h_u} \left( \begin{matrix} z_1'' \theta_1'' (t-a)^{a_1} (b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_u'' \theta_u'' (t-a)^{a_u} (b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(u)}} \end{matrix} \right)$$

$$A \left( \begin{matrix} z_1''' \theta_1''' (t-a)^{a'_1} (b-t)^{b'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)'}} \\ \vdots \\ z_v''' \theta_v''' (t-a)^{a'_v} (b-t)^{b'_v} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(v)'}} \end{matrix} \right)$$

$$I \left( \begin{matrix} z_1 \theta_1 (t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r (t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{matrix} \right)$$

$$I \left( \begin{matrix} z_1' \theta_1' (t-a)^{\mu'_1} (b-t)^{\rho'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)'}} \\ \vdots \\ z_s' \theta_s' (t-a)^{\mu'_s} (b-t)^{\rho'_s} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(s)'}} \end{matrix} \right) dt$$

$$= P_1 \sum_{g_1, \dots, g_v=0}^{\infty} \sum_{M_1=0}^{\alpha^{(1)}} \dots \sum_{M_v=0}^{\alpha^{(v)}} \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} \prod_{i=1}^v z_i^{\eta_{h_i, k_i}} \prod_{k=1}^u z^{\eta_{R_k}} B_u B_{u,v}$$





$$(C) \max_{1 \leq j \leq k} \left\{ \left| \frac{(b-a)f_i}{af_i + g_i} \right| \right\} < 1, \max_{1 \leq j \leq l} \{ |\tau_j(b-a)^{h_j}| \} < 1$$

$$(D) \operatorname{Re} \left[ \alpha + \sum_{j=1}^v a'_j \min_{1 \leq k \leq \alpha^{(i)}} \frac{p_k^{(j)}}{\epsilon_k^{(j)}} + \sum_{j=1}^r \mu_j \min_{1 \leq k \leq m^{(i)}} \frac{b_k^{(j)}}{\beta_k^{(j)}} + \sum_{j=1}^s \mu'_i \min_{1 \leq k \leq m'^{(i)}} \frac{b_k'^{(j)}}{\beta_k'^{(j)}} \right] > 0$$

$$\operatorname{Re} \left[ \beta + \sum_{j=1}^v b'_j \min_{1 \leq k \leq \alpha^{(i)}} \frac{p_k^{(j)}}{\epsilon_k^{(j)}} + \sum_{j=1}^r \rho_j \min_{1 \leq k \leq m^{(i)}} \frac{b_k^{(j)}}{\beta_k^{(j)}} + \sum_{j=1}^s \rho'_j \min_{1 \leq k \leq m'^{(i)}} \frac{b_k'^{(j)}}{\beta_k'^{(j)}} \right] > 0$$

$$(E) \operatorname{Re} \left( \alpha + \sum_{i=1}^v \eta_{G_i, g_i} a'_i + \sum_{i=1}^u R_i a_i + \sum_{i=1}^r \mu_i s_i + \sum_{i=1}^s t_i \mu'_i \right) > 0$$

$$\operatorname{Re} \left( \beta + \sum_{i=1}^v \eta_{G_i, g_i} b'_i + \sum_{i=1}^u R_i b_i + \sum_{i=1}^r v_i s_i + \sum_{i=1}^s t_i \rho'_i \right) > 0$$

$$\operatorname{Re} \left( \lambda_j + \sum_{i=1}^v \eta_{G_i, g_i} \lambda_j^{(i)} + \sum_{i=1}^u R_i \lambda_j^{(i)} + \sum_{i=1}^r s_i \zeta_j^{(i)} + \sum_{i=1}^s t_i \zeta_j'^{(i)} \right) > 0 (j = 1, \dots, l);$$

$$\operatorname{Re} \left( -\sigma_j + \sum_{i=1}^v \eta_{G_i, g_i} \lambda_j^{(i)} + \sum_{i=1}^u R_i \lambda_j^{(i)} + \sum_{i=1}^r s_i \lambda_j^{(i)} + \sum_{i=1}^s t_i \lambda_j'^{(i)} \right) > 0 (j = 1, \dots, k);$$

$$(F) \Omega_i = \sum_{k=1}^{n^{(i)}} \alpha_k^{(i)} - \sum_{k=n^{(i)}+1}^{p^{(i)}} \alpha_k^{(i)} + \sum_{k=1}^{m^{(i)}} \beta_k^{(i)} - \sum_{k=m^{(i)}+1}^{q^{(i)}} \beta_k^{(i)} + \left( \sum_{k=1}^{n_2} \alpha_{2k}^{(i)} - \sum_{k=n_2+1}^{p_2} \alpha_{2k}^{(i)} \right) + \dots +$$

$$\left( \sum_{k=1}^{n_s} \alpha_{sk}^{(i)} - \sum_{k=n_s+1}^{p_s} \alpha_{sk}^{(i)} \right) - \left( \sum_{k=1}^{q_2} \beta_{2k}^{(i)} + \sum_{k=1}^{q_3} \beta_{3k}^{(i)} + \dots + \sum_{k=1}^{q_s} \beta_{sk}^{(i)} \right) - \mu_i - \rho_i$$

$$- \sum_{l=1}^k \lambda_j^{(i)} - \sum_{l=1}^l \zeta_j^{(i)} > 0 \quad (i = 1, \dots, r)$$

$$\Omega'_i = \sum_{k=1}^{n'^{(i)}} \alpha'_k{}^{(i)} - \sum_{k=n'^{(i)}+1}^{p'^{(i)}} \alpha'_k{}^{(i)} + \sum_{k=1}^{m'^{(i)}} \beta'_k{}^{(i)} - \sum_{k=m'^{(i)}+1}^{q'^{(i)}} \beta'_k{}^{(i)} + \left( \sum_{k=1}^{n'_2} \alpha'_{2k}{}^{(i)} - \sum_{k=n'_2+1}^{p'_2} \alpha'_{2k}{}^{(i)} \right) +$$

$$\dots + \left( \sum_{k=1}^{n'_s} \alpha'_{sk}{}^{(i)} - \sum_{k=n'_s+1}^{p'_s} \alpha'_{sk}{}^{(i)} \right) - \left( \sum_{k=1}^{q'_2} \beta'_{2k}{}^{(i)} + \sum_{k=1}^{q'_3} \beta'_{3k}{}^{(i)} + \dots + \sum_{k=1}^{q'_s} \beta'_{sk}{}^{(i)} \right) - \mu'_i - \rho'_i$$

$$- \sum_{l=1}^k \lambda'_j{}^{(i)} - \sum_{l=1}^l \zeta'_j{}^{(i)} > 0 \quad (i = 1, \dots, s)$$

$$(G) \left| \arg \left( z_i \prod_{j=1}^l [1 - \tau_j(t-a)^{h_j}]^{-\zeta_j^{(i)}} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(i)}} \right) \right| < \frac{1}{2} \Omega_i \pi \quad (a \leq t \leq b; i = 1, \dots, r)$$

$$\left| \arg \left( z'_i \prod_{j=1}^l [1 - \tau'_j(t-a)^{h'_i}]^{-\zeta_j^{(i)}} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(i)}} \right) \right| < \frac{1}{2} \Omega'_i \pi \quad (a \leq t \leq b; i = 1, \dots, s)$$

**(H)** The multiple series occurring on the right-hand side of (3.24) is absolutely and uniformly convergent.

**Proof**

To prove (3.24), first, we express in series the multivariable A-function with the help of (1.1), a class of multivariable polynomials defined by Srivastava et al [5]  $S_L^{h_1, \dots, h_u} [.]$  in series with the help of (1.13) and we interchange the order of summations and t-integral (which is permissible under the conditions stated). Expressing the I-functions of r-variables and s-variables defined by Prasad [2] in terms of Mellin-Barnes type contour integral with the help of (1.8) and (1.11) respectively and interchange the order of integrations which is justifiable due to absolute convergence of the integral involved in the process. Now collect the power of  $[1 - \tau_j(t-a)^{h_i}]$  with  $(i = 1, \dots, r; j = 1, \dots, l)$  and collect the power of  $(f_j t + g_j)$  with  $j = 1, \dots, k$ . Use the equations (2.2) and (2.3) and express the result in Mellin-Barnes contour integral. Interpreting the  $(r + s + k + l)$  dimensional Mellin-Barnes integral in multivariable I-function defined by Prasad [2], we obtain the equation (3.24).

**Remarks**

If a)  $\rho_1 = \dots, \rho_r = \rho'_1 = \dots, \rho'_s = 0$ ; b)  $\mu_1 = \dots, \mu_r = \mu'_1 = \dots, \mu'_s = 0$ , we obtain the similar formulas that (3.24) with the corresponding simplifications.

4. Particular cases

a) If  $U = V = A = B = 0$ , the multivariable I-function defined by Prasad reduces to multivariable H-function defined by Srivastava et al [8] and we obtain :

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1 - \tau_j(t-a)^{h_i}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$S_L^{h_1, \dots, h_u} \left( \begin{matrix} z''_1 \theta''_1 (t-a)^{a_1} (b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z''_u \theta''_u (t-a)^{a_u} (b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(u)}} \end{matrix} \right)$$

$$A \left( \begin{matrix} z'''_1 \theta'''_1 (t-a)^{a'_1} (b-t)^{b'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)'}} \\ \vdots \\ z'''_v \theta'''_v (t-a)^{a'_v} (b-t)^{b'_v} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(v)'}} \end{matrix} \right)$$

$$H \left( \begin{matrix} z_1 \theta_1 (t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r (t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{matrix} \right)$$

$$\begin{aligned}
 & H \left( \begin{array}{c} z'_1 \theta'_1 (t-a)^{\mu'_1} (b-t)^{\rho'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda'_j(1)} \\ \vdots \\ z'_s \theta'_s (t-a)^{\mu'_s} (b-t)^{\rho'_s} \prod_{j=1}^k (f_j t + g_j)^{-\lambda'_j(s)} \end{array} \right) dt \\
 &= P_1 \sum_{g_1, \dots, g_u=0}^{\infty} \sum_{M_1=0}^{\alpha(1)} \dots \sum_{M_v=0}^{\alpha(v)} \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} \prod_{i=1}^v z_i^{\mu_i \eta_{i,k_j}} \prod_{k=1}^u z^{\mu R_k} B_u B_{u,v} \\
 & H_{p_r+n'_s+l+k+2; X}^{0, n_r+n'_s+l+k+2; Y} \left( \begin{array}{c} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j(1)}} \\ \dots \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j(r)}} \\ \frac{z'_1(b-a)^{\mu'_1+\rho'_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j(1)}} \\ \dots \\ \frac{z'_s(b-a)^{\mu'_s+\rho'_s}}{\prod_{j=1}^k (af_j+g_j)^{\lambda'_j(s)}} \\ \tau_1(b-a)^{h_1} \\ \dots \\ \tau_l(b-a)^{h_l} \\ \frac{(b-a)f_1}{af_1+g_1} \\ \dots \\ \frac{(b-a)f_k}{af_k+g_k} \end{array} \middle| \begin{array}{l} \mathbf{K}_1, \mathbf{K}_2, \mathbf{K}_j, \mathbf{K}'_j, \mathfrak{A} : A' \\ \vdots \\ \mathbf{L}_1, \mathbf{L}_j, \mathbf{L}'_j : D_1, \mathfrak{B} : B' \end{array} \right) \quad (4.1)
 \end{aligned}$$

under the same notations and conditions that (3.24) with  $U = V = A = B = 0$

$$\text{b) If } B(L; R_1, \dots, R_u) = \frac{\prod_{j=1}^{\bar{A}} (a_j)_{R_1 \theta'_j + \dots + R_u \theta_j^{(u)}} \prod_{j=1}^{B'} (b'_j)_{R_1 \phi'_j} \dots \prod_{j=1}^{B^{(u)}} (b_j^{(u)})_{R_u \phi_j^{(u)}}}{\prod_{j=1}^{\bar{C}} (c_j)_{R_1 \psi'_j + \dots + R_u \psi_j^{(u)}} \prod_{j=1}^{D'} (d'_j)_{R_1 \delta'_j} \dots \prod_{j=1}^{D^{(u)}} (d_j^{(u)})_{R_u \delta_j^{(u)}}} \quad (4.2)$$

then the general class of multivariable polynomial  $S_L^{h_1, \dots, h_u} [z_1, \dots, z_u]$  reduces to generalized Lauricella function

defined by Srivastava et al [5]. We have the following integral.

$$\int_a^b (t-a)^{\alpha-1} (b-t)^{\beta-1} \prod_{j=1}^l [1-\tau_j(t-a)^{h_j}]^{-\lambda_j} \prod_{j=1}^k (f_j t + g_j)^{\sigma_j}$$

$$F_{\bar{C}:D';\dots;D^{(u)}}^{1+\bar{A}:B';\dots;B^{(u)}} \left( \begin{matrix} z_1''\theta_1''(t-a)^{a_1}(b-t)^{b_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''(1)} \\ \vdots \\ z_u''\theta_u''(t-a)^{a_u}(b-t)^{b_u} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j''(u)} \end{matrix} \right)$$

$$A \left( \begin{matrix} z_1''' \theta_1''' (t-a)^{a'_1} (b-t)^{b'_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''(1)} \\ \vdots \\ z_v''' \theta_v''' (t-a)^{a'_v} (b-t)^{b'_v} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'''(v)} \end{matrix} \right)$$

$$I \left( \begin{matrix} z_1 \theta_1 (t-a)^{\mu_1} (b-t)^{\rho_1} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(1)}} \\ \vdots \\ z_r \theta_r (t-a)^{\mu_r} (b-t)^{\rho_r} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j^{(r)}} \end{matrix} \right)$$

$$I \left( \begin{matrix} z_1' \theta_1' (t-a)^{\mu_1'} (b-t)^{\rho_1'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(1)}} \\ \vdots \\ z_s' \theta_s' (t-a)^{\mu_s'} (b-t)^{\rho_s'} \prod_{j=1}^k (f_j t + g_j)^{-\lambda_j'^{(s)}} \end{matrix} \right) dt$$

$$= P_1 \sum_{g_1, \dots, g_v=0}^{\infty} \sum_{M_1=0}^{\alpha^{(1)}} \dots \sum_{M_v=0}^{\alpha^{(v)}} \sum_{R_1, \dots, R_u=0}^{h_1 R_1 + \dots + h_u R_u \leq L} \prod_{i=1}^v z_i''' \eta_{h_i, k_i} \prod_{k=1}^u z'' R_k B_u' B_{u,v}$$

$$\begin{aligned}
 & I_{U: p_r+p'_s+l+k+2, q_r+q'_s+l+k+1; Y}^{V; 0, n_r+n'_s+l+k+2; X} \left( \begin{array}{l} \frac{z_1(b-a)^{\mu_1+\rho_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(1)}}} \\ \dots \\ \frac{z_r(b-a)^{\mu_r+\rho_r}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j^{(r)}}} \\ \frac{z'_1(b-a)^{\mu'_1+\rho'_1}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j'^{(1)}}} \\ \dots \\ \frac{z'_s(b-a)^{\mu'_s+\rho'_s}}{\prod_{j=1}^k (af_j+g_j)^{\lambda_j'^{(s)}}} \\ \tau_1(b-a)^{h_1} \\ \dots \\ \tau_l(b-a)^{h_l} \\ \frac{(b-a)f_1}{af_1+g_1} \\ \dots \\ \frac{(b-a)f_k}{af_k+g_k} \end{array} \middle| \begin{array}{l} A; K_1, K_2, K_j, K'_j, \mathfrak{A} : A' \\ \dots \\ B; L_1, L_j, L'_j : D_1, \mathfrak{B} : B' \end{array} \right) \tag{4.3}
 \end{aligned}$$

under the same conditions and notations that (3.24)

where  $B'_u = \frac{(-L)_{h_1 R_1 + \dots + h_u R_u} B(E; R_1, \dots, R_u)}{R_1! \dots R_u!}$ ,  $B[E; R_1, \dots, R_u]$  is defined by (4.2)

**Remark:**

By the following similar procedure, the results of this document can be extended to product of any finite number of multivariable I-functions defined by Prasad [2] and a class of multivariable polynomials defined by Srivastava et al [6].

**5. Conclusion**

In this paper we have evaluated a generalized Eulerian integral involving the product of two multivariable I-functions defined by Prasad [1], a expansion of multivariable A-function and a class of multivariable polynomials defined by Srivastava et al [5] with general arguments. The formulae established in this paper is very general nature. Thus, the results established in this research work would serve as a key formula from which, upon specializing the parameters, as many as desired results involving the special functions of one and several variables can be obtained.

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