# Finite integral involving the spheroidal function, a class of 

# polynomials and multivariable Aleph-functions IV 

F.Y. AY ANT ${ }^{1}$

1 Teacher in High School, France

## ABSTRACT

In the present paper we evaluate a generalized finite integral involving the product of the spheroidal function, multivariable Aleph-functions and general class of polynomials of several variables with general arguments. The importance of the result established in this paper lies in the fact they involve the Aleph-function of several variables which is sufficiently general in nature and capable to yielding a large of results merely by specializating the parameters their in.

Keywords:Multivariable Aleph-function, general class of polynomials, spheroidal function, multivariable I-function, Aleph-function of two variable, I-function of two variables

2010 Mathematics Subject Classification. 33C99, 33C60, 44A20

## 1.Introduction and preliminaries.

The function Aleph of several variables generalize the multivariable I-function recently study by C.K. Sharma and Ahmad [3], itself is an a generalisation of G and H -functions of multiple variables. The multiple Mellin-Barnes integral occuring in this paper will be referred to as the multivariables Aleph-function throughout our present study and will be defined and represented as follows.

We define $: \aleph\left(z_{1}, \cdots, z_{r}\right)=\aleph_{p_{i}, q_{i}, \tau_{i} ; R: p_{i}(1), q_{i}(1), \tau_{i}(1) ; R^{(1)} ; \cdots ; p_{i}(r), q_{i}(r) ; \tau_{i}(r) ; R^{(r)}}^{0, \mathfrak{m}, m_{1}, \cdots, m_{r}, n_{r}}$

$$
\left(\begin{array}{c}
\mathrm{Z}_{1} \\
\cdot \\
\cdot \\
\cdot \\
\mathrm{Z}_{r}
\end{array}\right)
$$

$$
\begin{array}{cl}
{\left[\left(\mathrm{a}_{j} ; \alpha_{j}^{(1)}, \cdots, \alpha_{j}^{(r)}\right)_{1, \mathfrak{n}}\right]} & ,\left[\tau_{i}\left(a_{j i} ; \alpha_{j i}^{(1)}, \cdots, \alpha_{j i}^{(r)}\right)_{\mathfrak{n}+1, p_{i}}\right]: \\
\ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots & ,\left[\tau_{i}\left(b_{j i} ; \beta_{j i}^{(1)}, \cdots, \beta_{j i}^{(r)}\right)_{m+1, q_{i}}\right]:
\end{array}
$$

$$
\left.\begin{array}{l}
\left.\left.\left[\left(\mathrm{c}_{j}^{(1)}\right) ; \gamma_{j}^{(1)}\right)_{1, n_{1}}\right],\left[\tau_{i(1)}\left(c_{j i^{(1)}}^{(1)} ; \gamma_{j i(1)}^{(1)}\right)_{n_{1}+1, p_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{c}_{j}^{(r)}\right) ; \gamma_{j}^{(r)}\right)_{1, n_{r}}\right],\left[\tau_{i(r)}\left(c_{j i(r)}^{(r)} ; \gamma_{j i(r)}^{(r)}\right)_{n_{r}+1, p_{i}^{(r)}}\right] \\
\left.\left.\left[\left(\mathrm{d}_{j}^{(1)}\right) ; \delta_{j}^{(1)}\right)_{1, m_{1}}\right],\left[\tau_{i^{(1)}}\left(d_{j i^{(1)}}^{(1)} ; \delta_{j i(1)}^{(1)}\right)_{m_{1}+1, q_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{d}_{j}^{(r)}\right) ; \delta_{j}^{(r)}\right)_{1, m_{r}}\right],\left[\tau_{i^{(r)}}\left(d_{j i(r)}^{(r)} ; \delta_{j i(r)}^{(r)}\right)_{m_{r}+1, q_{i}^{(r)}}\right]
\end{array}\right)
$$

$$
\begin{equation*}
=\frac{1}{(2 \pi \omega)^{r}} \int_{L_{1}} \cdots \int_{L_{r}} \psi\left(s_{1}, \cdots, s_{r}\right) \prod_{k=1}^{r} \theta_{k}\left(s_{k}\right) y_{k}^{s_{k}} \mathrm{~d} s_{1} \cdots \mathrm{~d} s_{r} \tag{1.1}
\end{equation*}
$$

with $\omega=\sqrt{-1}$
$\psi\left(s_{1}, \cdots, s_{r}\right)=\frac{\prod_{j=1}^{\mathfrak{n}} \Gamma\left(1-a_{j}+\sum_{k=1}^{r} \alpha_{j}^{(k)} s_{k}\right)}{\sum_{i=1}^{R}\left[\tau_{i} \prod_{j=\mathfrak{n}+1}^{p_{i}} \Gamma\left(a_{j i}-\sum_{k=1}^{r} \alpha_{j i}^{(k)} s_{k}\right) \prod_{j=1}^{q_{i}} \Gamma\left(1-b_{j i}+\sum_{k=1}^{r} \beta_{j i}^{(k)} s_{k}\right)\right]}$
and $\theta_{k}\left(s_{k}\right)=\frac{\prod_{j=1}^{m_{k}} \Gamma\left(d_{j}^{(k)}-\delta_{j}^{(k)} s_{k}\right) \prod_{j=1}^{n_{k}} \Gamma\left(1-c_{j}^{(k)}+\gamma_{j}^{(k)} s_{k}\right)}{\sum_{i^{(k)}=1}^{R^{(k)}}\left[\tau_{i^{(k)}} \prod_{j=m_{k}+1}^{q_{i}(k)} \Gamma\left(1-d_{j i(k)}^{(k)}+\delta_{j i(k)}^{(k)} s_{k}\right) \prod_{j=n_{k}+1}^{p_{i(k)}} \Gamma\left(c_{j i(k)}^{(k)}-\gamma_{j i(k)}^{(k)} s_{k}\right)\right]}$

Suppose, as usual, that the parameters
$a_{j}, j=1, \cdots, p ; b_{j}, j=1, \cdots, q ;$
$c_{j}^{(k)}, j=1, \cdots, n_{k} ; c_{j i(k)}^{(k)}, j=n_{k}+1, \cdots, p_{i(k)} ;$
$d_{j}^{(k)}, j=1, \cdots, m_{k} ; d_{j i(k)}^{(k)}, j=m_{k}+1, \cdots, q_{i(k)} ;$
with $k=1 \cdots, r, i=1, \cdots, R, i^{(k)}=1, \cdots, R^{(k)}$
are complex numbers, and the $\alpha^{\prime} s, \beta^{\prime} s, \gamma^{\prime} s$ and $\delta^{\prime} s$ are assumed to be positive real numbers for standardization purpose such that

$$
\begin{align*}
& U_{i}^{(k)}=\sum_{j=1}^{\mathfrak{n}} \alpha_{j}^{(k)}+\tau_{i} \sum_{j=\mathfrak{n}+1}^{p_{i}} \alpha_{j i}^{(k)}+\sum_{j=1}^{n_{k}} \gamma_{j}^{(k)}+\tau_{i(k)} \sum_{j=n_{k}+1}^{p_{i}(k)} \gamma_{j i(k)}^{(k)}-\tau_{i} \sum_{j=1}^{q_{i}} \beta_{j i}^{(k)}-\sum_{j=1}^{m_{k}} \delta_{j}^{(k)} \\
& -\tau_{i(k)} \sum_{j=m_{k}+1}^{q_{i(k)}} \delta_{j i^{(k)}}^{(k)} \leqslant 0 \tag{1.4}
\end{align*}
$$

The reals numbers $\tau_{i}$ are positives for $i=1$ to $R, \tau_{i(k)}$ are positives for $i^{(k)}=1$ to $R^{(k)}$
The contour $L_{k}$ is in the $s_{k}$-p lane and run from $\sigma-i \infty$ to $\sigma+i \infty$ where $\sigma$ is a real number with loop, if necessary ,ensure that the poles of $\Gamma\left(d_{j}^{(k)}-\delta_{j}^{(k)} s_{k}\right)$ with $j=1$ to $m_{k}$ are separated from those of $\Gamma\left(1-a_{j}+\sum_{i=1}^{r} \alpha_{j}^{(k)} s_{k}\right)$ with $j=1$ to $n$ and $\Gamma\left(1-c_{j}^{(k)}+\gamma_{j}^{(k)} s_{k}\right)$ with $j=1$ to $n_{k}$ to the left of the contour $L_{k}$. The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H -function given by as :
$\left|\arg z_{k}\right|<\frac{1}{2} A_{i}^{(k)} \pi$, where

$$
\begin{align*}
& A_{i}^{(k)}=\sum_{j=1}^{\mathfrak{n}} \alpha_{j}^{(k)}-\tau_{i} \sum_{j=\mathfrak{n}+1}^{p_{i}} \alpha_{j i}^{(k)}-\tau_{i} \sum_{j=1}^{q_{i}} \beta_{j i}^{(k)}+\sum_{j=1}^{n_{k}} \gamma_{j}^{(k)}-\tau_{i(k)} \sum_{j=n_{k}+1}^{p_{i}(k)} \gamma_{j i}^{(k)} \\
& +\sum_{j=1}^{m_{k}} \delta_{j}^{(k)}-\tau_{i^{(k)}} \sum_{j=m_{k}+1}^{q_{i}(k)} \delta_{j i(k)}^{(k)}>0, \text { with } k=1, \cdots, r, i=1, \cdots, R, i^{(k)}=1, \cdots, R^{(k)} \tag{1.5}
\end{align*}
$$

The complex numbers $z_{i}$ are not zero.Throughout this document, we assume the existence and absolute convergence conditions of the multivariable Aleph-function.

We may establish the the asymptotic expansion in the following convenient form :
$\aleph\left(z_{1}, \cdots, z_{r}\right)=0\left(\left|z_{1}\right|^{\alpha_{1}}, \cdots,\left|z_{r}\right|^{\alpha_{r}}\right), \max \left(\left|z_{1}\right|, \cdots,\left|z_{r}\right|\right) \rightarrow 0$
$\aleph\left(z_{1}, \cdots, z_{r}\right)=0\left(\left|z_{1}\right|^{\beta_{1}}, \cdots,\left|z_{r}\right|^{\beta_{r}}\right), \min \left(\left|z_{1}\right|, \cdots,\left|z_{r}\right|\right) \rightarrow \infty$
where, with $k=1, \cdots, r: \alpha_{k}=\min \left[\operatorname{Re}\left(d_{j}^{(k)} / \delta_{j}^{(k)}\right)\right], j=1, \cdots, m_{k}$ and

$$
\beta_{k}=\max \left[\operatorname{Re}\left(\left(c_{j}^{(k)}-1\right) / \gamma_{j}^{(k)}\right)\right], j=1, \cdots, n_{k}
$$

Serie representation of Aleph-function of several variables is given by

$$
\begin{align*}
& \aleph\left(y_{1}, \cdots, y_{r}\right)=\sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} \psi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) \\
& \times \theta_{1}\left(\eta_{G_{1}, g_{1}}\right) \cdots \theta_{r}\left(\eta_{G_{r}, g_{r}}\right) y_{1}^{-\eta_{G_{1}, g_{1}}} \cdots y_{r}^{-\eta_{G_{r}, g_{r}}} \tag{1.6}
\end{align*}
$$

Where $\psi(., \cdots,),. \theta_{i}(),. i=1, \cdots, r$ are given respectively in (1.2), (1.3) and

$$
\begin{equation*}
\eta_{G_{1}, g_{1}}=\frac{d_{g_{1}}^{(1)}+G_{1}}{\delta_{g_{1}}^{(1)}}, \cdots, \eta_{G_{r}, g_{r}}=\frac{d_{g_{r}}^{(r)}+G_{r}}{\delta_{g_{r}}^{(r)}} \tag{1.7}
\end{equation*}
$$

which is valid under the conditions $\delta_{g_{i}}^{(i)}\left[d_{j}^{i}+p_{i}\right] \neq \delta_{j}^{(i)}\left[d_{g_{i}}^{i}+G_{i}\right]$
for $j \neq m_{i}, m_{i}=1, \cdots \eta_{G_{i}, g_{i}} ; p_{i}, n_{i}=0,1,2, \cdots, ; y_{i} \neq 0, i=1, \cdots, r$

Consider the Aleph-function of s variables
$\aleph\left(z_{1}, \cdots, z_{s}\right)=\aleph_{P_{i}, Q_{i}, \iota_{i} ; r^{\prime}: P_{i(1)}, Q_{i(1)}, \iota_{i}(1) ; r^{(1)} ; \cdots ; P_{i(s)}, Q_{i(s)} ; \iota_{i}(s) ; r^{(s)}}^{0, N: M_{1}, N_{1}, \cdots, M_{s} N_{s}}\left(\begin{array}{c}\mathrm{z}_{1} \\ \cdot \\ \cdot \\ \cdot \\ \mathrm{Z}_{s}\end{array}\right)$

$$
\begin{array}{cl}
{\left[\left(u_{j} ; \mu_{j}^{(1)}, \cdots, \mu_{j}^{\left(r^{\prime}\right)}\right)_{1, N}\right]} & ,\left[\iota_{i}\left(u_{j i} ; \mu_{j i}^{(1)}, \cdots, \mu_{j i}^{\left(r^{\prime}\right)}\right)_{\left.N+1, P_{i}\right]}\right]: \\
\cdots \cdots \cdots \cdots \cdots \cdots \cdots \cdots \cdots & ,\left[\iota_{i}\left(v_{j i} ; v_{j i}^{(1)}, \cdots, v_{j i}^{\left(r^{\prime}\right)}\right)_{M+1, Q_{i}}\right]:
\end{array}
$$

$\left.\left.\left.\left[\left(\mathrm{a}_{j}^{(1)}\right) ; \alpha_{j}^{(1)}\right)_{1, N_{1}}\right],\left[\iota_{i(1)}\left(a_{j i(1)}^{(1)} ; \alpha_{j i(1)}^{(1)}\right)_{N_{1}+1, P_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{a}_{j}^{(s)}\right) ; \alpha_{j}^{(s)}\right)_{1, N_{s}}\right],\left[\iota_{i^{(s)}}\left(a_{j i(s)}^{(s)} ; \alpha_{j i(s)}^{(s)}\right)_{N_{s}+1, P_{i}^{(s)}}\right]\right)$ $\left.\left.\left.\left[\left(\mathrm{b}_{j}^{(1)}\right) ; \beta_{j}^{(1)}\right)_{1, M_{1}}\right],\left[\iota_{i^{(1)}}\left(b_{j i(1)}^{(1)} ; \beta_{j i^{(1)}}^{(1)}\right)_{M_{1}+1, Q_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{b}_{j}^{(s)}\right) ; \beta_{j}^{(s)}\right)_{1, M_{s}}\right],\left[\iota_{i(s)}\left(b_{j i^{(s)}}^{(s)} ; \beta_{j i^{(s)}}^{(s)}\right)_{M_{s}+1, Q_{i}^{(s)}}\right]\right)$
$=\frac{1}{(2 \pi \omega)^{s}} \int_{L_{1}} \cdots \int_{L_{s}} \zeta\left(t_{1}, \cdots, t_{s}\right) \prod_{k=1}^{s} \phi_{k}\left(t_{k}\right) z_{k}^{t_{k}} \mathrm{~d} t_{1} \cdots \mathrm{~d} t_{s}$
with $\omega=\sqrt{-1}$
$\zeta\left(t_{1}, \cdots, t_{s}\right)=\frac{\prod_{j=1}^{N} \Gamma\left(1-u_{j}+\sum_{k=1}^{s} \mu_{j}^{(k)} t_{k}\right)}{\sum_{i=1}^{r^{\prime}}\left[\iota_{i} \prod_{j=N+1}^{P_{i}} \Gamma\left(u_{j i}-\sum_{k=1}^{s} \mu_{j i}^{(k)} t_{k}\right) \prod_{j=1}^{Q_{i}} \Gamma\left(1-v_{j i}+\sum_{k=1}^{s} v_{j i}^{(k)} t_{k}\right)\right]}$
and $\phi_{k}\left(t_{k}\right)=\frac{\prod_{j=1}^{M_{k}} \Gamma\left(b_{j}^{(k)}-\beta_{j}^{(k)} t_{k}\right) \prod_{j=1}^{N_{k}} \Gamma\left(1-a_{j}^{(k)}+\alpha_{j}^{(k)} s_{k}\right)}{\left.\sum_{i^{(k)}=1}^{r^{(k)}\left[\iota_{i(k)}\right.} \prod_{j=M_{k}+1}^{Q_{i(k)}^{(k)}} \Gamma\left(1-b_{j i(k)}^{(k)}+\beta_{j i(k)}^{(k)} t_{k}\right) \prod_{j=N_{k}+1}^{P_{i(k)}} \Gamma\left(a_{j i(k)}^{(k)}-\alpha_{j i(k)}^{(k)} s_{k}\right)\right]}(1.1$

Suppose, as usual , that the parameters
$u_{j}, j=1, \cdots, P ; v_{j}, j=1, \cdots, Q ;$
$a_{j}^{(k)}, j=1, \cdots, N_{k} ; a_{j i(k)}^{(k)}, j=n_{k}+1, \cdots, P_{i^{(k)}} ;$
$b_{j i(k)}^{(k)}, j=m_{k}+1, \cdots, Q_{i^{(k)}} ; b_{j}^{(k)}, j=1, \cdots, M_{k} ;$
with $k=1 \cdots, s, i=1, \cdots, r^{\prime}, i^{(k)}=1, \cdots, r^{(k)}$
are complex numbers, and the $\alpha^{\prime} s, \beta^{\prime} s, \gamma^{\prime} s$ and $\delta^{\prime} s$ are assumed to be positive real numbers for standardization purpose such that

$$
\begin{align*}
& U_{i}^{(k)}=\sum_{j=1}^{N} \mu_{j}^{(k)}+\iota_{i} \sum_{j=N+1}^{P_{i}} \mu_{j i}^{(k)}+\sum_{j=1}^{N_{k}} \alpha_{j}^{(k)}+\iota_{i}(k) \sum_{j=N_{k}+1}^{P_{i(k)}} \alpha_{j i(k)}^{(k)}-\iota_{i} \sum_{j=1}^{Q_{i}} v_{j i}^{(k)}-\sum_{j=1}^{M_{k}} \beta_{j}^{(k)} \\
& -\iota_{i(k)} \sum_{j=M_{k}+1}^{Q_{i}(k)} \beta_{j i(k)}^{(k)} \leqslant 0 \tag{1.12}
\end{align*}
$$

The reals numbers $\tau_{i}$ are positives for $i=1, \cdots, r, \iota_{i}(k)$ are positives for $i^{(k)}=1 \cdots r^{(k)}$
The contour $L_{k}$ is in the $t_{k}$-p lane and run from $\sigma-i \infty$ to $\sigma+i \infty$ where $\sigma$ is a real number with loop, if necessary ,ensure that the poles of $\Gamma\left(b_{j}^{(k)}-\beta_{j}^{(k)} t_{k}\right)$ with $j=1$ to $M_{k}$ are separated from those of $\Gamma\left(1-u_{j}+\sum_{i=1}^{s} \mu_{j}^{(k)} t_{k}\right)$ with $j=1$ to $N$ and $\Gamma\left(1-a_{j}^{(k)}+\alpha_{j}^{(k)} t_{k}\right)$ with $j=1$ to $N_{k}$ to the left of the contour $L_{k}$. The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H -function given by as :

$$
\begin{align*}
& \left|\arg z_{k}\right|<\frac{1}{2} B_{i}^{(k)} \pi, \text { where } \\
& B_{i}^{(k)}=\sum_{j=1}^{N} \mu_{j}^{(k)}-\iota_{i} \sum_{j=N+1}^{P_{i}} \mu_{j i}^{(k)}-\iota_{i} \sum_{j=1}^{Q_{i}} v_{j i}^{(k)}+\sum_{j=1}^{N_{k}} \alpha_{j}^{(k)}-\iota_{i(k)} \sum_{j=N_{k}+1}^{P_{i(k)}} \alpha_{j i(k)}^{(k)} \\
& +\sum_{j=1}^{M_{k}} \beta_{j}^{(k)}-\iota_{i(k)}^{q_{i}(k)} \sum_{j=M_{k}+1}^{(k)} \beta_{j i(k)}^{(k)}>0, \text { with } k=1, \cdots, s, i=1, \cdots, r, i^{(k)}=1, \cdots, r^{(k)} \tag{1.13}
\end{align*}
$$

The complex numbers $z_{i}$ are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable Aleph-function.

We may establish the the asymptotic expansion in the following convenient form :
$\aleph\left(z_{1}, \cdots, z_{s}\right)=0\left(\left|z_{1}\right|^{\alpha_{1}^{\prime}}, \cdots,\left|z_{s}\right|^{\alpha_{s}^{\prime}}\right), \max \left(\left|z_{1}\right|, \cdots,\left|z_{s}\right|\right) \rightarrow 0$
$\aleph\left(z_{1}, \cdots, z_{s}\right)=0\left(\left|z_{1}\right|^{\beta_{1}^{\prime}}, \cdots,\left|z_{s}\right|^{\beta_{s}^{\prime}}\right), \min \left(\left|z_{1}\right|, \cdots,\left|z_{s}\right|\right) \rightarrow \infty$
where, with $k=1, \cdots, z: \alpha_{k}^{\prime}=\min \left[\operatorname{Re}\left(b_{j}^{(k)} / \beta_{j}^{(k)}\right)\right], j=1, \cdots, M_{k}$ and

$$
\beta_{k}^{\prime}=\max \left[\operatorname{Re}\left(\left(a_{j}^{(k)}-1\right) / \alpha_{j}^{(k)}\right)\right], j=1, \cdots, N_{k}
$$

We will use these following notations in this paper
$U=P_{i}, Q_{i}, \iota_{i} ; r^{\prime} ; V=M_{1}, N_{1} ; \cdots ; M_{s}, N_{s}$
$\mathrm{W}=P_{i^{(1)}}, Q_{i^{(1)}}, \iota_{i^{(1)}} ; r^{(1)}, \cdots, P_{i^{(r)}}, Q_{i^{(r)}}, \iota_{i^{(s)}} ; r^{(s)}$
$A=\left\{\left(u_{j} ; \mu_{j}^{(1)}, \cdots, \mu_{j}^{(s)}\right)_{1, N}\right\},\left\{\iota_{i}\left(u_{j i} ; \mu_{j i}^{(1)}, \cdots, \mu_{j i}^{(s)}\right)_{N+1, P_{i}}\right\}$
$B=\left\{\iota_{i}\left(v_{j i} ; v_{j i}^{(1)}, \cdots, v_{j i}^{(s)}\right)_{M+1, Q_{i}}\right\}$
$C=\left(a_{j}^{(1)} ; \alpha_{j}^{(1)}\right)_{1, N_{1}}, \iota_{i(1)}\left(a_{j i(1)}^{(1)} ; \alpha_{j i(1)}^{(1)}\right) N_{1}+1, P_{i(1)}, \cdots,\left(a_{j}^{(s)} ; \alpha_{j}^{(s)}\right)_{1, N_{s}}, \iota_{i(s)}\left(a_{j i(s)}^{(s)} ; \alpha_{j i(s)}^{(s)}\right) N_{s}+1, P_{i(s)}^{(1}$
$D=\left(b_{j}^{(1)} ; \beta_{j}^{(1)}\right)_{1, M_{1}, \iota_{i(1)}}\left(b_{j i^{(1)}}^{(1)} ; \beta_{j i(1)}^{(1)}\right)_{M_{1}+1, Q_{i}(1)}, \cdots,\left(b_{j}^{(s)} ; \beta_{j}^{(s)}\right)_{1, M_{s},} \iota_{i^{(s)}}\left(\beta_{j i^{(s)}}^{(s)} ; \beta_{j i^{(s)}}^{(s)}\right)_{M_{s}+1, Q_{i}(s)}$

The multivariable Aleph-function write :
$\aleph\left(z_{1}, \cdots, z_{s}\right)=\aleph_{U: W}^{0, N: V}\left(\begin{array}{c|c}\mathrm{z}_{1} & \mathrm{~A}: \mathrm{C} \\ \cdot & \\ \cdot & \cdot \\ \mathrm{z}_{s} & \mathrm{~B}: \mathrm{D}\end{array}\right)$

The generalized polynomials defined by Srivastava [6], is given in the following manner :
$S_{N_{1}, \cdots, N_{t}}^{M_{1}, \cdots, M_{t}}\left[y_{1}, \cdots, y_{t}\right]=\sum_{K_{1}=0}^{\left[N_{1} / M_{1}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M_{t}\right]} \frac{\left(-N_{1}\right)_{M_{1} K_{1}}}{K_{1}!} \cdots \frac{\left(-N_{t}\right)_{M_{t} K_{t}}}{K_{t}!}$
$A\left[N_{1}, K_{1} ; \cdots ; N_{t}, K_{t}\right] y_{1}^{K_{1}} \cdots y_{t}^{K_{t}}$

Where $M_{1}, \cdots, M_{s}$ are arbitrary positive integers and the coefficients $A\left[N_{1}, K_{1} ; \cdots ; N_{t}, K_{t}\right]$ are arbitrary constants, real or complex. In the present paper, we use the following notation
$a_{1}=\frac{\left(-N_{1}\right)_{M_{1} K_{1}}}{K_{1}!} \cdots \frac{\left(-N_{t}\right)_{M_{t} K_{t}}}{K_{t}!} A\left[N_{1}, K_{1} ; \cdots ; N_{t}, K_{t}\right]$
In the document, we note :
$G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)=\phi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) \theta_{1}\left(\eta_{G_{1}, g_{1}}\right) \cdots \theta_{r}\left(\eta_{G_{r}, g_{r}}\right)$
where $\phi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right), \theta_{1}\left(\eta_{G_{1}, g_{1}}\right), \cdots, \theta_{r}\left(\eta_{G_{r}, g_{r}}\right)$ are given respectively in (1.2) and (1.3)

The spheroidal function $\psi_{\alpha n}(c, \eta)$ of general order $\alpha>-1$ can be expansed as ([2] an [7].
$\psi_{\alpha n}(c, \eta)=\frac{i^{n} \sqrt{2 \pi}}{V_{\alpha n(c)}} \sum_{k=0, o r 1}^{\infty_{*}} a_{k}(c \mid \alpha n)(c \eta)^{-\alpha-\frac{1}{2}} J_{k+\alpha+\frac{1}{2}}(c \eta)$
which represents the function uniformly on $(\infty, \infty)$, where the coefficients $a_{k}(c \mid \alpha n)$ satisfy the recursion formula [14, eq.67] and the asterisk over the summation sign indicates that the sum is taken over only even or odd values of $k$ according as $n$ is even or odd. As $c \rightarrow 0, a_{k}(c \mid \alpha n) \rightarrow 0, k \neq n$

## 2.Required integral

We have the following result , see Brychkow ([1], 4.1.5, eq. 68 page 140)

$$
\begin{align*}
& \int_{0}^{a} x^{s+\frac{1}{2}}(a-s)^{s} \ln \left[\frac{1+b \sqrt[4]{x(a-x)}}{1-b \sqrt[4]{x(a-x)}}\right] \mathrm{d} x=2^{-2 s-\frac{1}{2}} \sqrt{\pi} a^{2 s+2} b \frac{\Gamma\left(2 s+\frac{5}{2}\right)}{\Gamma(2 s+3)} \\
& \times{ }_{3} F_{2}\left[\frac{1}{2}, 1,2 s+\frac{5}{2} ; \frac{3}{2}, 2 s+3 ; \frac{a b^{2}}{2}\right]  \tag{2.1}\\
& \text { where }: a>0, \text { Res }>-\frac{5}{4},\left|\arg \left(2-a b^{2}\right)\right|<\pi
\end{align*}
$$

## 3. main integral

Let $X^{c}=x^{c}(a-x)^{c}$, we have the following general finite integral.

$$
\begin{aligned}
& \int_{0}^{a} x^{\alpha+\frac{1}{2}}(a-x)^{\alpha} l n\left[\frac{1+b \sqrt[4]{x(a-x)}}{1-b \sqrt[4]{x(a-x)}}\right] \psi_{\alpha n}\left(c^{\sigma}, X_{\beta}\right) S_{N_{1}, \cdots, N_{t}}^{M_{1}, \cdots, M_{t}}\left(\begin{array}{c}
\mathrm{y}_{1} X_{\gamma_{1}} \\
\vdots \\
\mathrm{y}_{t} X_{\gamma_{t}}
\end{array}\right) \aleph_{u: w}^{0, \mathrm{n}: v}\left(\begin{array}{c}
\mathrm{z}_{1} X_{\alpha_{1}} \\
\cdots \\
\mathrm{z}_{r} X_{\alpha_{r}}
\end{array}\right) \\
& \aleph_{U: W}^{0, N: V}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\eta_{1}} \\
\cdots \\
\mathrm{Z}_{s} X_{\eta_{s}}
\end{array}\right) \mathrm{d} x=2^{-2 \alpha-\frac{1}{2}} \sqrt{\pi} a^{2 \alpha+2} b \frac{i^{n} \sqrt{2 \pi}}{V_{\alpha n}\left(c^{\sigma}\right)} \sum_{k=0, o r 1}^{\infty} \sum_{m=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{n^{\prime}=0}^{\infty}
\end{aligned}
$$

$$
\sum_{K_{1}=0}^{\left[N_{1} / M_{1}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M_{t}\right]} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} a_{1} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)
$$

$$
\frac{(-)^{m} a_{k}\left(c^{\sigma} \mid \alpha n\right)}{m!\Gamma\left(m+k+\alpha+\frac{3}{2}\right)} y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}} C^{\sigma(2 m+k)} \frac{\left(\frac{1}{2}\right)_{n^{\prime}}}{\left(\frac{3}{2}\right)_{n^{\prime}}}\left(\frac{a^{2} b}{2}\right)^{n^{\prime}}
$$

$$
4^{-\left(\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i}\right)} a^{\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i}} \aleph_{U_{11}: W}^{0, N+1: V}\left(\begin{array}{c}
\left(\frac{a}{4}\right)^{\eta_{1}} Z_{1} \\
\cdots \\
\cdots \\
\left(\frac{a}{4}\right)^{\eta_{s}} Z_{s}
\end{array}\right)
$$

$$
\left.\begin{array}{l}
\left(-\frac{3}{2}-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, \cdots, 2 \eta_{s}\right), A: C \\
\left(-2-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, \cdots, 2 \eta_{s}\right), B: D \tag{3.1}
\end{array}\right)
$$

Provided that
a) $\min \left\{\gamma_{i}, \mu_{i}, \alpha_{j}, \beta_{j}, \eta_{k}, \epsilon_{k}\right\}>0, i=1, \cdots, t, j=1, \cdots, r, k=1, \cdots, s$
b) $a>0,\left|\arg \left(2-a b^{2}\right)\right|<\pi$
c) $R e\left[\alpha+\beta(2 m+k)+\sum_{i=1}^{r} \alpha_{i} \min _{1 \leqslant j \leqslant m_{i}} \frac{d_{j}^{(i)}}{\delta_{j}^{(i)}}+\sum_{i=1}^{s} \eta_{i} \min _{1 \leqslant j \leqslant M_{i}} \frac{b_{j}^{(i)}}{\beta_{j}^{(i)}}\right]>-\frac{5}{4}$
d) $\left|\arg z_{k}\right|<\frac{1}{2} A_{i}^{(k)} \pi$, where $A_{i}^{(k)}$ is defined by (1.5); $i=1, \cdots, r$
e) $\left|\arg Z_{k}\right|<\frac{1}{2} B_{i}^{(k)} \pi$, where $B_{i}^{(k)}$ is defined by (1.13); $i=1, \cdots, s$
f) The series occuring on the right-hand side of (3.1) is absolutely and uniformly convergent.

## Proof

Expressing the spheroidal function involved in the integrand in its expression form with the help of (1.25) and the Bessel serie, the Aleph-function of r variables in series with the help of equation (1.6), the general class of polynomial of several variables $S_{N_{1}, \cdots, N_{t}}^{M_{1}, \cdots, M_{t}}$ with the help of equation (1.22)and the Aleph-function of s variables in Mellin-Barnes contour integral with the help of equation (1.9), changing the order of integration ans summation (which is easily seen to be justified due to the absolute convergence of the integral and the summations involved in the process) and then evaluating the resulting integral with the help of equation (2.1) and expressing the generalized hypergeometric function ${ }_{3} F_{2}$ in serie, use the relation $\Gamma(a)(a)_{n}=\Gamma(a+n)$ with Rea $>0$. Finally interpreting the result thus obtained with the Mellin-barnes contour integral, we arrive at the desired result.

## 4. Multivariable I-function

If $\iota_{i}, \iota_{i(1)}, \cdots, \iota_{i(s)} \rightarrow 1$, the Aleph-function of several variables degenere to the I-function of several variables. The generalized simple integral have been derived in this section for multivariable I-functions defined by Sharma et al [3].

## Corollary 1

$\int_{0}^{a} x^{\alpha+\frac{1}{2}}(a-x)^{\alpha} \ln \left[\frac{1+b \sqrt[4]{x(a-x)}}{1-b \sqrt[4]{x(a-x)}}\right] \psi_{\alpha n}\left(c^{\sigma}, X_{\beta}\right) S_{N_{1}, \cdots, N_{t}}^{M_{1}, \ldots, M_{t}}\left(\begin{array}{c}\mathrm{y}_{1} X_{\gamma_{1}} \\ \vdots \\ \mathrm{y}_{t} X_{\gamma_{t}}\end{array}\right) \aleph_{u: w}^{0, \mathfrak{n}: v}\left(\begin{array}{c}\mathrm{z}_{1} X_{\alpha_{1}} \\ \cdots \\ \mathrm{z}_{r} X_{\alpha_{r}}\end{array}\right)$
$I_{U: W}^{0, N: V}\binom{\mathrm{Z}_{1} X_{\eta_{1}}}{\dot{Z_{s}} X_{\eta_{s}}} \mathrm{~d} x=2^{-2 \alpha-\frac{1}{2}} \sqrt{\pi} a^{2 \alpha+2} b \frac{i^{n} \sqrt{2 \pi}}{V_{\alpha n}\left(c^{\sigma}\right)} \sum_{k=0, o r}^{\infty} \sum_{m=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{n^{\prime}=0}^{\infty}$
$\sum_{K_{1}=0}^{\left[N_{1} / M_{1}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M_{t}\right]} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} a_{1} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)$
$\frac{(-)^{m} a_{k}\left(c^{\sigma} \mid \alpha n\right)}{m!\Gamma\left(m+k+\alpha+\frac{3}{2}\right)} y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}} c^{\sigma(2 m+k)} \frac{\left(\frac{1}{2}\right)_{n^{\prime}}}{\left(\frac{3}{2}\right)_{n^{\prime}}}\left(\frac{a^{2} b}{2}\right)^{n^{\prime}}$

$$
\left.\begin{array}{l}
4^{-\left(\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i}\right)} a^{\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i}} I_{U_{11}: W}^{0, N+1: V}\left(\begin{array}{c}
\left(\frac{a}{4}\right)^{\eta_{1}} Z_{1} \\
\cdots \\
\cdots \\
\left(\frac{a}{4}\right)^{\eta_{s}} Z_{s}
\end{array}\right) \\
\left(-\frac{3}{2}-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, \cdots, 2 \eta_{s}\right), A: C  \tag{4.1}\\
\cdots \\
\left(-2-\mathrm{n} '-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, \cdots, 2 \eta_{s}\right), B: D
\end{array}\right) \quad(4)
$$

under the same conditions and notations that (3.1) with $\iota_{i}, \iota_{i(1)}, \cdots, \iota_{i(s)} \rightarrow 1$

## 5. Aleph-function of two variables

If $s=2$, we obtain the Aleph-function of two variables defined by K.Sharma [5], and we have the following simple integrals.

## Corollary 2

$\int_{0}^{a} x^{\alpha+\frac{1}{2}}(a-x)^{\alpha} \ln \left[\frac{1+b \sqrt[4]{x(a-x)}}{1-b \sqrt[4]{x(a-x)}}\right] \psi_{\alpha n}\left(c^{\sigma}, X_{\beta}\right) S_{N_{1}, \cdots, N_{t}}^{M_{1}, \ldots, M_{t}}\left(\begin{array}{c}\mathrm{y}_{1} X_{\gamma_{1}} \\ \vdots \\ \mathrm{y}_{t} X_{\gamma_{t}}\end{array}\right) \aleph_{u: w}^{0, \mathrm{n}: v}\binom{\mathrm{z}_{1} X_{\alpha_{1}}}{\mathrm{z}_{r} X_{\alpha_{r}}}$
$\aleph_{U: W}^{0, N: V}\left(\begin{array}{c}\mathrm{Z}_{1} X_{\eta_{1}} \\ \dot{-} \cdot \dot{U}_{1} \\ \mathrm{Z}_{2} X_{\eta_{2}}\end{array}\right) \mathrm{d} x=2^{-2 \alpha-\frac{1}{2}} \sqrt{\pi} a^{2 \alpha+2} b \frac{i^{n} \sqrt{2 \pi}}{V_{\alpha n}\left(c^{\sigma}\right)} \sum_{k=0, o r 1}^{\infty} \sum_{m=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{n^{\prime}=0}^{\infty}$

$$
\sum_{K_{1}=0}^{\left[N_{1} / M_{1}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M_{t}\right]} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} a_{1} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)
$$

$\frac{(-)^{m} a_{k}\left(c^{\sigma} \mid \alpha n\right)}{m!\Gamma\left(m+k+\alpha+\frac{3}{2}\right)} y_{1}^{K_{1}} \cdots y_{t}^{K_{t} z_{1} z_{1}, g_{1}} \ldots z_{r}^{\eta_{G}, g_{r}} c^{\sigma(2 m+k)} \frac{\left(\frac{1}{2}\right)_{n^{\prime}}}{\left(\frac{3}{2}\right)_{n^{\prime}}}\left(\frac{a^{2} b}{2}\right)^{n^{\prime}}$
$4^{-\left(\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i}\right)} a^{\beta(2 m+k)+\sum_{i=1}^{t} K_{i} \gamma_{i}+\sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} \aleph_{U_{11}: W}^{0, N+1: V}\left(\begin{array}{c}\left(\frac{a}{4}\right)^{\eta_{1}} Z_{1} \\ \cdots \\ \cdots \\ \cdots \\ \left(\frac{a}{4}\right)^{\eta_{2}} Z_{2}\end{array}\right) . . . . .}$

$$
\left.\begin{array}{c}
\left(-\frac{3}{2}-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, 2 \eta_{2}\right), A: C \\
\left(-2-\mathrm{n}^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} \cdot K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, 2 \eta_{2}\right), B: D \tag{5.1}
\end{array}\right)
$$

under the same conditions and notations that (3.1) with $s=2$

## 6. I-function of two variables

If $\iota_{i}, \iota_{i}^{\prime}, \iota_{i}^{\prime \prime} \rightarrow 1$, then the Aleph-function of two variables degenere in the I-function of two variables defined by sharma et $\mathrm{al}[4]$ and we obtain the same formula with the I-function of two variables.

## Corollary 3

$$
\left.\begin{array}{c}
\left(-\frac{3}{2}-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, 2 \eta_{2}\right), A: C  \tag{6.1}\\
\left(-2-n^{\prime}-2 \alpha-2 \beta(2 m+k)-2 \sum_{i=1}^{t} K_{i} \gamma_{i}-2 \sum_{i=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{i} ; 2 \eta_{1}, 2 \eta_{2}\right), B: D
\end{array}\right)
$$

under the same conditions and notations that (3.1) with $s=2$ and $\iota_{i}, \iota_{i}^{\prime}, \iota_{i}^{\prime \prime} \rightarrow 1$

## 7. Conclusion

In this paper we have evaluated a generalized finite integral involving the multivariable Aleph-functions, a class of polynomials of several variables and the spheroidal function.The integral established in this paper is of very general nature as it contains Multivariable Aleph-function, which is a general function of several variables studied so far. Thus, the integral established in this research work would serve as a key formula from which, upon specializing the parameters, as many as desired results involving the special functions of one and several variables can be obtained.

$$
\begin{aligned}
& \int_{0}^{a} x^{\alpha+\frac{1}{2}}(a-x)^{\alpha} \ln \left[\frac{1+b \sqrt[4]{x(a-x)}}{1-b \sqrt[4]{x(a-x)}}\right] \psi_{\alpha n}\left(c^{\sigma}, X_{\beta}\right) S_{N_{1}, \cdots, N_{t}}^{M_{1}, \cdots, M_{t}}\left(\begin{array}{c}
\mathrm{y}_{1} X_{\gamma_{1}} \\
\cdot \\
\mathrm{y}_{t} X_{\gamma_{t}}
\end{array}\right) \underset{\sim}{X_{u: w}}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\alpha_{1}} \\
\cdot \\
\mathrm{Z}_{r} X_{\alpha_{r}}
\end{array}\right) \\
& I_{U: W}^{0, N: V}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\eta_{1}} \\
\cdot . \cdot \\
\mathrm{Z}_{2} X_{\eta_{2}}
\end{array}\right) \mathrm{d} x=2^{-2 \alpha-\frac{1}{2}} \sqrt{\pi} a^{2 \alpha+2} b \frac{i^{n} \sqrt{2 \pi}}{V_{\alpha n}\left(c^{\sigma}\right)} \sum_{k=0, o r 1}^{\infty_{*}} \sum_{m=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{n^{\prime}=0}^{\infty} \\
& \sum_{K_{1}=0}^{\left[N_{1} / M_{1}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M_{t}\right]} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} a_{1} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) \\
& \frac{(-)^{m} a_{k}\left(c^{\sigma} \mid \alpha n\right)}{m!\Gamma\left(m+k+\alpha+\frac{3}{2}\right)} y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}} c^{\sigma(2 m+k)} \frac{\left(\frac{1}{2}\right)_{n^{\prime}}}{\left(\frac{3}{2}\right)_{n^{\prime}}}\left(\frac{a^{2} b}{2}\right)^{n^{\prime}}
\end{aligned}
$$

## REFERENCES

[1] Brychkow Y.A. Handbook of Special Functions. Derivatives. Integrals, Series and Other Formulas. CRC. Press. Taykor and Francis Group. Boca. Raton. London. New York. 2008.
[2] Rhodes D.R. On the spheroidal functions. J. Res. Nat. Bur. Standards. Sect. B 74(1970), page187-209.
[3] Sharma C.K.and Ahmad S.S.: On the multivariable I-function. Acta ciencia Indica Math , 1994 vol 20,no2, p 113116.
[4] C.K. Sharma and P.L. mishra : On the I-function of two variables and its properties. Acta Ciencia Indica Math , 1991 Vol 17 page 667-672.
[5] Sharma K. On the integral representation and applications of the generalized function of two variables , International Journal of Mathematical Engineering and Sciences, Vol 3 , issue1 ( 2014 ), page1-13.
[6] Srivastava H.M. A multilinear generating function for the Konhauser set of biorthogonal polynomials suggested by Laguerre polynomial, Pacific. J. Math. 177(1985), page183-191.
[7] Stratton J.A. And Chu L.J. Elliptic and spheroidal wave function J. Math. And Phys. 20 (1941), page 259-309.

[^0]
[^0]:    Personal adress : 411 Avenue Joseph Raynaud
    Le parc Fleuri , Bat B
    83140 , Six-Fours les plages
    Tel : 06-83-12-49-68
    Department : VAR
    Country : FRANCE

