# Multiple integrals transformation about the generalized incomplete hypergeometric 

# function, a general class of polynomials and the multivariable Aleph-functions 

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## ABSTRACT

In the present paper we evaluate a generalized multiple integrals transformation involving the product of rhe generalized incomplete hypergeometric function, the multivariable Aleph-functions, and general class of polynomials of several variables. The importance of the result established in this paper lies in the fact they involve the Aleph-function of several variables which is sufficiently general in nature and capable to yielding a large of results merely by specializating the parameters their in.. We shall the case concerning the multivariable I-function defined by Sharma and Sharma [2].

Keywords:Multivariable Aleph-function, general class of polynomials, multiple integrals, generalized incomplete hypergeometric function, multivariable I -function, multivariable H -function

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## 1.Introduction and preliminaries.

The function Aleph of several variables is an extension the multivariable I-function recently studied by C.K. Sharma and Ahmad [6], itself is a generalisation of G and H -functions of multiple variables. The multiple Mellin-Barnes integral occurring in this paper will be referred to as the multivariables Aleph-function throughout our present study and will be defined and represented as follows.

We define : $\aleph\left(z_{1}, \cdots, z_{r}\right)=\underset{p_{i}, q_{i}, \tau_{i} ; R: p_{i(1)}, q_{i(1)}, \tau_{i(1)} ; R^{(1)} ; \cdots ; p_{i(r)}, q_{i(r)} ; \tau_{i(r)} ; R^{(r)}}{\mathfrak{n}^{2} m_{1}, n_{1}, \cdots, m_{2}, n_{r}}\left(\begin{array}{c}\mathrm{z}_{1} \\ \cdot \\ \cdot \\ \cdot \\ \mathrm{Z}_{r}\end{array}\right)$

$$
\begin{array}{cc}
{\left[\left(\mathrm{a}_{j} ; \alpha_{j}^{(1)}, \cdots, \alpha_{j}^{(r)}\right)_{1, \mathfrak{n}}\right]} & ,\left[\tau_{i}\left(a_{j i} ; \alpha_{j i}^{(1)}, \cdots, \alpha_{j i}^{(r)}\right)_{\mathfrak{n}+1, p_{i}}\right]: \\
\quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots & ,\left[\tau_{i}\left(b_{j i} ; \beta_{j i}^{(1)}, \cdots, \beta_{j i}^{(r)}\right)_{1, q_{i}}\right]:
\end{array}
$$

$\left.\begin{array}{l}\left.\left.\left[\left(\mathrm{c}_{j}^{(1)}\right) ; \gamma_{j}^{(1)}\right)_{1, n_{1}}\right],\left[\tau_{i(1)}\left(c_{j i(1)}^{(1)} ; \gamma_{j i(1)}^{(1)}\right)_{n_{1}+1, p_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{c}_{j}^{(r)}\right) ; \gamma_{j}^{(r)}\right)_{1, n_{r}}\right],\left[\tau_{i^{(r)}}\left(c_{j i(r)}^{(r)} ; \gamma_{j i}^{(r)}\right)_{n_{r}+1, p_{i}^{(r)}}\right] \\ \left.\left.\left[\left(\mathrm{d}_{j}^{(1)}\right) ; \delta_{j}^{(1)}\right)_{1, m_{1}}\right],\left[\tau_{i^{(1)}}\left(d_{j i^{(1)}}^{(1)} ; \delta_{j i(1)}^{(1)}\right)_{m_{1}+1, q_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{d}_{j}^{(r)}\right) ; \delta_{j}^{(r)}\right)_{1, m_{r}}\right],\left[\tau_{i(r)}\left(d_{j i(r)}^{(r)} ; \delta_{j i(r)}^{(r)}\right)_{m_{r}+1, q_{i}}^{(r)}\right]\end{array}\right)$
$=\frac{1}{(2 \pi \omega)^{r}} \int_{L_{1}} \cdots \int_{L_{r}} \psi\left(s_{1}, \cdots, s_{r}\right) \prod_{k=1}^{r} \theta_{k}\left(s_{k}\right) y_{k}^{s_{k}} \mathrm{~d} s_{1} \cdots \mathrm{~d} s_{r}$
with $\omega=\sqrt{-1}$
$\psi\left(s_{1}, \cdots, s_{r}\right)=\frac{\prod_{j=1}^{\mathfrak{n}} \Gamma\left(1-a_{j}+\sum_{k=1}^{r} \alpha_{j}^{(k)} s_{k}\right)}{\sum_{i=1}^{R}\left[\tau_{i} \prod_{j=\mathfrak{n}+1}^{p_{i}} \Gamma\left(a_{j i}-\sum_{k=1}^{r} \alpha_{j i}^{(k)} s_{k}\right) \prod_{j=1}^{q_{i}} \Gamma\left(1-b_{j i}+\sum_{k=1}^{r} \beta_{j i}^{(k)} s_{k}\right)\right]}$

Suppose, as usual, that the parameters
$a_{j}, j=1, \cdots, p ; b_{j}, j=1, \cdots, q ;$
$c_{j}^{(k)}, j=1, \cdots, n_{k} ; c_{j i(k)}^{(k)}, j=n_{k}+1, \cdots, p_{i(k)} ;$
$d_{j}^{(k)}, j=1, \cdots, m_{k} ; d_{j i^{(k)}}^{(k)}, j=m_{k}+1, \cdots, q_{i(k)} ;$
with $k=1 \cdots, r, i=1, \cdots, R, i^{(k)}=1, \cdots, R^{(k)}$
are complex numbers, and the $\alpha^{\prime} s, \beta^{\prime} s, \gamma^{\prime} s$ and $\delta^{\prime} s$ are assumed to be positive real numbers for standardization purpose such that
$U_{i}^{(k)}=+\tau_{i} \sum_{j=\mathfrak{n}+1}^{p_{i}} \alpha_{j i}^{(k)}-\tau_{i^{(k)}} \sum_{j=n_{k}+1}^{p_{i}(k)} \gamma_{j i^{(k)}}^{(k)}+\tau_{i} \sum_{j=1}^{q_{i}} \beta_{j i}^{(k)}-\tau_{i^{(k)}} \sum_{j=m_{k}+1}^{q_{i}(k)} \delta_{j i^{(k)}}^{(k)} \leqslant 0$

The reals numbers $\tau_{i}$ are positives for $i=1$ to $R, \tau_{i(k)}$ are positives for $i^{(k)}=1$ to $R^{(k)}$
The contour $L_{k}$ is in the $s_{k}$-p lane and run from $\sigma-i \infty$ to $\sigma+i \infty$ where $\sigma$ is a real number with loop, if necessary ,ensure that the poles of $\Gamma\left(d_{j}^{(k)}-\delta_{j}^{(k)} s_{k}\right)$ with $j=1$ to $m_{k}$ are separated from those of $\Gamma\left(1-a_{j}+\sum_{i=1}^{r} \alpha_{j}^{(k)} s_{k}\right)$ with $j=1$ to $n$ and $\Gamma\left(1-c_{j}^{(k)}+\gamma_{j}^{(k)} s_{k}\right)$ with $j=1$ to $n_{k}$ to the left of the contour $L_{k}$. The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H -function given by as :
$\left|\arg z_{k}\right|<\frac{1}{2} A_{i}^{(k)} \pi$, where

$$
\begin{align*}
& A_{i}^{(k)}=\sum_{j=1}^{\mathfrak{n}} \alpha_{j}^{(k)}-\tau_{i} \sum_{j=\mathfrak{n}+1}^{p_{i}} \alpha_{j i}^{(k)}-\tau_{i} \sum_{j=1}^{q_{i}} \beta_{j i}^{(k)}+\sum_{j=1}^{n_{k}} \gamma_{j}^{(k)}-\tau_{i(k)} \sum_{j=n_{k}+1}^{p_{i}(k)} \gamma_{j i}^{(k)} \\
& +\sum_{j=1}^{m_{k}} \delta_{j}^{(k)}-\tau_{i(k)} \sum_{j=m_{k}+1}^{q_{i}(k)} \delta_{j i(k)}^{(k)}>0, \quad \text { with } k=1 \cdots, r, i=1, \cdots, R, i^{(k)}=1, \cdots, R^{(k)} \tag{1.4}
\end{align*}
$$

The complex numbers $z_{i}$ are not zero.Throughout this document, we assume the existence and absolute convergence conditions of the multivariable Aleph-function.

We may establish the the asymptotic expansion in the following convenient form :
$\aleph\left(z_{1}, \cdots, z_{r}\right)=0\left(\left|z_{1}\right|^{\alpha_{1}}, \cdots,\left|z_{r}\right|^{\alpha_{r}}\right), \max \left(\left|z_{1}\right|, \cdots,\left|z_{r}\right|\right) \rightarrow 0$
$\aleph\left(z_{1}, \cdots, z_{r}\right)=0\left(\left|z_{1}\right|^{\beta_{1}}, \cdots,\left|z_{r}\right|^{\beta_{r}}\right), \min \left(\left|z_{1}\right|, \cdots,\left|z_{r}\right|\right) \rightarrow \infty$
where $k=1, \cdots, r: \alpha_{k}=\min \left[\operatorname{Re}\left(d_{j}^{(k)} / \delta_{j}^{(k)}\right)\right], j=1, \cdots, m_{k}$ and

$$
\beta_{k}=\max \left[\operatorname{Re}\left(\left(c_{j}^{(k)}-1\right) / \gamma_{j}^{(k)}\right)\right], j=1, \cdots, n_{k}
$$

Series representation of Aleph-function of several variables is given by

$$
\aleph\left(y_{1}, \cdots, y_{r}\right)=\sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} \psi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)
$$

$\times \theta_{1}\left(\eta_{G_{1}, g_{1}}\right) \cdots \theta_{r}\left(\eta_{G_{r}, g_{r}}\right) y_{1}^{-\eta_{G_{1}, g_{1}}} \cdots y_{r}^{-\eta_{G_{r}, g_{r}}}$

Where $\psi(., \cdots,),. \theta_{i}(),. i=1, \cdots, r$ are given respectively in (1.2), (1.3) and
$\eta_{G_{1}, g_{1}}=\frac{d_{g_{1}}^{(1)}+G_{1}}{\delta_{g_{1}}^{(1)}}, \cdots, \eta_{G_{r}, g_{r}}=\frac{d_{g_{r}}^{(r)}+G_{r}}{\delta_{g_{r}}^{(r)}}$
which is valid under the conditions $\delta_{g_{i}}^{(i)}\left[d_{j}^{i}+p_{i}\right] \neq \delta_{j}^{(i)}\left[d_{g_{i}}^{i}+G_{i}\right]$
for $j \neq m_{i}, m_{i}=1, \cdots \eta_{G_{i}, g_{i}} ; p_{i}, n_{i}=0,1,2, \cdots, ; y_{i} \neq 0, i=1, \cdots, r$

Consider the Aleph-function of s variables
$\aleph\left(z_{1}, \cdots, z_{s}\right)=\aleph_{P_{i}, Q_{i}, \iota_{i} ; r^{\prime}: P_{i}(1), Q_{i}(1), \iota_{i}(1) ; r^{(1)} ; \cdots ; P_{i}(s), Q_{i}(s) ; \iota_{i}(s) ; r^{(s)}}^{0, N: M_{1}, N_{1}, \cdots, M_{s}, N_{s}}\left(\begin{array}{c}\mathrm{z}_{1} \\ \cdot \\ \cdot \\ \cdot \\ \mathrm{z}_{s}\end{array}\right)$

$$
\left[\left(u_{j} ; \mu_{j}^{(1)}, \cdots, \mu_{j}^{\left(r^{\prime}\right)}\right)_{1, N}\right] \quad,\left[\iota_{i}\left(u_{j i} ; \mu_{j i}^{(1)}, \cdots, \mu_{j i}^{\left(r^{\prime}\right)}\right)_{N+1, P_{i}}\right]:
$$

$\left.\left.\left[\left(\mathrm{a}_{j}^{(1)}\right) ; \alpha_{j}^{(1)}\right)_{1, N_{1}}\right],\left[\iota_{i^{(1)}}\left(a_{j i(1)}^{(1)} ; \alpha_{j i^{(1)}}^{(1)}\right)_{N_{1}+1, P_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{a}_{j}^{(s)}\right) ; \alpha_{j}^{(s)}\right)_{1, N_{s}}\right],\left[\iota_{i^{(s)}}\left(a_{j i^{(s)}}^{(s)} ; \alpha_{j i^{(s)}}^{(s)}\right)_{\left.N_{s}+1, P_{i}^{(s)}\right]}\right]$ $\left.\left.\left[\left(\mathrm{b}_{j}^{(1)}\right) ; \beta_{j}^{(1)}\right)_{1, M_{1}}\right],\left[\iota_{i^{(1)}}\left(b_{j i^{(1)}}^{(1)} ; \beta_{j i^{(1)}}^{(1)}\right)_{M_{1}+1, Q_{i}^{(1)}}\right] ; \cdots ;\left[\left(\mathrm{b}_{j}^{(s)}\right) ; \beta_{j}^{(s)}\right)_{1, M_{s}}\right],\left[\iota_{i(s)}^{(s)}\left(b_{j i^{(s)}}^{(s)} ; \beta_{j i^{(s)}}^{(s)}\right)_{M_{s}+1, Q_{i}^{(s)}}\right]$
$=\frac{1}{(2 \pi \omega)^{s}} \int_{L_{1}^{\prime}} \cdots \int_{L_{s}^{\prime}} \zeta\left(t_{1}, \cdots, t_{s}\right) \prod_{k=1}^{s} \phi_{k}\left(t_{k}\right) z_{k}^{t_{k}} \mathrm{~d} t_{1} \cdots \mathrm{~d} t_{s}$
with $\omega=\sqrt{-1}$
$\zeta\left(t_{1}, \cdots, t_{s}\right)=\frac{\prod_{j=1}^{N} \Gamma\left(1-u_{j}+\sum_{k=1}^{s} \mu_{j}^{(k)} t_{k}\right)}{\sum_{i=1}^{r^{\prime}}\left[\iota_{i} \prod_{j=N+1}^{P_{i}} \Gamma\left(u_{j i}-\sum_{k=1}^{s} \mu_{j i}^{(k)} t_{k}\right) \prod_{j=1}^{Q_{i}} \Gamma\left(1-v_{j i}+\sum_{k=1}^{s} v_{j i}^{(k)} t_{k}\right)\right]}$
and $\phi_{k}\left(t_{k}\right)=\frac{\prod_{j=1}^{M_{k}} \Gamma\left(b_{j}^{(k)}-\beta_{j}^{(k)} t_{k}\right) \prod_{j=1}^{N_{k}} \Gamma\left(1-a_{j}^{(k)}+\alpha_{j}^{(k)} s_{k}\right)}{\sum_{i^{(k)}=1}^{r^{(k)}}\left[\iota_{i}(k) \prod_{j=M_{k}+1}^{Q_{i}(k)} \Gamma\left(1-b_{j i}^{(k)}+\beta_{j i(k)}^{(k)} t_{k}\right) \prod_{j=N_{k}+1}^{P_{i}(k)} \Gamma\left(a_{j i(k)}^{(k)}-\alpha_{j i(k)}^{(k)} s_{k}\right)\right]}(1$,

Suppose, as usual , that the parameters
$u_{j}, j=1, \cdots, P ; v_{j}, j=1, \cdots, Q ;$
$a_{j}^{(k)}, j=1, \cdots, N_{k} ; a_{j i(k)}^{(k)}, j=n_{k}+1, \cdots, P_{i(k)} ;$
$b_{j i(k)}^{(k)}, j=m_{k}+1, \cdots, Q_{i^{(k)}} ; b_{j}^{(k)}, j=1, \cdots, M_{k} ;$
with $k=1 \cdots, s, i=1, \cdots, r^{\prime}, i^{(k)}=1, \cdots, r^{(k)}$
are complex numbers, and the $\alpha^{\prime} s, \beta^{\prime} s, \gamma^{\prime} s$ and $\delta^{\prime} s$ are assumed to be positive real numbers for standardization purpose such that

$$
\begin{equation*}
U_{i}^{(k)}=\iota_{i} \sum_{j=N+1}^{P_{i}} \mu_{j i}^{(k)}-\iota_{i(k)} \sum_{j=N_{k}+1}^{P_{i(k)}} \alpha_{j i^{(k)}}^{(k)}+\iota_{i} \sum_{j=1}^{Q_{i}} v_{j i}^{(k)}-\iota_{i(k)} \sum_{j=M_{k}+1}^{Q_{i}(k)} \beta_{j i^{(k)}}^{(k)} \leqslant 0 \tag{1.11}
\end{equation*}
$$

The reals numbers $\tau_{i}$ are positives for $i=1, \cdots, r, \iota_{i(k)}$ are positives for $i^{(k)}=1 \cdots r^{(k)}$
The contour $L_{k}$ is in the $t_{k}$-p lane and run from $\sigma-i \infty$ to $\sigma+i \infty$ where $\sigma$ is a real number with loop, if necessary ,ensure that the poles of $\Gamma\left(b_{j}^{(k)}-\beta_{j}^{(k)} t_{k}\right)$ with $j=1$ to $M_{k}$ are separated from those of $\Gamma\left(1-u_{j}+\sum_{i=1}^{s} \mu_{j}^{(k)} t_{k}\right)$ with $j=1$ to $N$ and $\Gamma\left(1-a_{j}^{(k)}+\alpha_{j}^{(k)} t_{k}\right)$ with $j=1$ to $N_{k}$ to the left of the contour $L_{k}$. The condition for absolute convergence of multiple Mellin-Barnes type contour (1.9) can be obtained by extension of the corresponding conditions for multivariable H -function given by as :
$\left|\arg z_{k}\right|<\frac{1}{2} B_{i}^{(k)} \pi$, where

$$
\begin{align*}
& B_{i}^{(k)}=\sum_{j=1}^{N} \mu_{j}^{(k)}-\iota_{i} \sum_{j=N+1}^{P_{i}} \mu_{j i}^{(k)}-\iota_{i} \sum_{j=1}^{Q_{i}} v_{j i}^{(k)}+\sum_{j=1}^{N_{k}} \alpha_{j}^{(k)}-\iota_{i(k)} \sum_{j=N_{k}+1}^{P_{i(k)}} \alpha_{j i(k)}^{(k)} \\
& +\sum_{j=1}^{M_{k}} \beta_{j}^{(k)}-\iota_{i(k)} \sum_{j=M_{k}+1}^{q_{i}(k)} \beta_{j i^{(k)}}^{(k)}>0, \quad \text { with } k=1 \cdots, s, i=1, \cdots, r, i^{(k)}=1, \cdots, r^{(k)} \tag{1.12}
\end{align*}
$$

The complex numbers $z_{i}$ are not zero. Throughout this document, we assume the existence and absolute convergence conditions of the multivariable Aleph-function.

We may establish the the asymptotic expansion in the following convenient form :
$\aleph\left(z_{1}, \cdots, z_{s}\right)=0\left(\left|z_{1}\right|^{\alpha_{1}^{\prime}}, \cdots,\left|z_{s}\right|^{\alpha_{s}^{\prime}}\right), \max \left(\left|z_{1}\right|, \cdots,\left|z_{s}\right|\right) \rightarrow 0$
$\aleph\left(z_{1}, \cdots, z_{s}\right)=0\left(\left|z_{1}\right|^{\beta_{1}^{\prime}}, \cdots,\left|z_{s}\right|^{\beta_{s}^{\prime}}\right), \min \left(\left|z_{1}\right|, \cdots,\left|z_{s}\right|\right) \rightarrow \infty$
where, $k=1, \cdots, z: \alpha_{k}^{\prime}=\min \left[\operatorname{Re}\left(b_{j}^{(k)} / \beta_{j}^{(k)}\right)\right], j=1, \cdots, M_{k}$ and

$$
\begin{equation*}
\beta_{k}^{\prime}=\max \left[\operatorname{Re}\left(\left(a_{j}^{(k)}-1\right) / \alpha_{j}^{(k)}\right)\right], j=1, \cdots, N_{k} \tag{1.13}
\end{equation*}
$$

We will use these following notations in this paper

$$
\begin{align*}
& U=P_{i}, Q_{i}, \iota_{i} ; r^{\prime} ; V=M_{1}, N_{1} ; \cdots ; M_{s}, N_{s}  \tag{1.14}\\
& \mathrm{~W}=P_{i^{(1)}}, Q_{i^{(1)}}, \iota_{i(1)} ; r^{(1)}, \cdots, P_{i^{(r)}}, Q_{i^{(r)}}, \iota_{i(s)} ; r^{(s)}  \tag{1.15}\\
& A=\left\{\left(u_{j} ; \mu_{j}^{(1)}, \cdots, \mu_{j}^{(s)}\right)_{1, N}\right\},\left\{\iota_{i}\left(u_{j i} ; \mu_{j i}^{(1)}, \cdots, \mu_{j i}^{(s)}\right)_{N+1, P_{i}}\right\}  \tag{1.16}\\
& B=\left\{\iota_{i}\left(v_{j i} ; v_{j i}^{(1)}, \cdots, v_{j i}^{(s)}\right)_{M+1, Q_{i}}\right\}  \tag{1.17}\\
& C=\left(a_{j}^{(1)} ; \alpha_{j}^{(1)}\right)_{1, N_{1}}, \iota_{i^{(1)}}\left(a_{j i^{(1)}}^{(1)} ; \alpha_{j i^{(1)}}^{(1)}\right)_{N_{1}+1, P_{i(1)}}, \cdots,\left(a_{j}^{(s)} ; \alpha_{j}^{(s)}\right)_{1, N_{s}}, \iota_{i^{(s)}}\left(a_{j i^{(s)}}^{(s)} ; \alpha_{j i^{(s)}}^{(s)}\right)_{N_{s}+1, P_{i}(s)}  \tag{1.18}\\
& D=\left(b_{j}^{(1)} ; \beta_{j}^{(1)}\right)_{1, M_{1}, \iota_{i(1)}\left(b_{j i(1)}^{(1)} ; \beta_{\left.j i^{(1)}\right)}^{(1)}\right)_{M_{1}+1, Q_{i}(1)}, \cdots,\left(b_{j}^{(s)} ; \beta_{j}^{(s)}\right)_{1, M_{s}}, \iota_{i(s)}\left(\beta_{j i^{(s)}}^{(s)} ; \beta_{j i(s)}^{(s)}\right)_{M_{s}+1, Q_{i}(s)}, 1 .} \tag{1.19}
\end{align*}
$$

The multivariable Aleph-function writes :
$\aleph\left(z_{1}, \cdots, z_{s}\right)=\aleph_{U: W}^{0, N: V}\left(\begin{array}{c|c}\mathrm{z}_{1} & \mathrm{~A}: \mathrm{C} \\ \cdot & \cdots \\ \cdot & \mathrm{B}: \mathrm{D} \\ \mathrm{z}_{s} & \end{array}\right)$

The generalized polynomials defined by Srivastava [5], is given in the following manner :
$S_{N_{1}^{\prime}, \cdots, N_{t}^{\prime}}^{M_{1}^{\prime}, \cdots, M_{t}^{\prime}}\left[y_{1}, \cdots, y_{t}\right]=\sum_{K_{1}=0}^{\left[N_{1}^{\prime} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t}^{\prime} / M_{t}^{\prime}\right]} \frac{\left(-N_{1}^{\prime}\right)_{M_{1}^{\prime} K_{1}}}{K_{1}!} \cdots \frac{\left(-N_{t}^{\prime}\right)_{M_{t}^{\prime} K_{t}}}{K_{t}!}$
$A\left[N_{1}^{\prime}, K_{1} ; \cdots ; N_{t}^{\prime}, K_{t}\right] y_{1}^{K_{1}} \cdots y_{t}^{K_{t}}$

Where $M_{1}^{\prime}, \cdots, M_{t}^{\prime}$ are arbitrary positive integers and the coefficients $A\left[N_{1}^{\prime}, K_{1} ; \cdots ; N_{t}^{\prime}, K_{t}\right]$ are arbitrary constants, real or complex. In the present paper, we use the following notation
$a_{1}=\frac{\left(-N_{1}^{\prime}\right)_{M_{1}^{\prime} K_{1}}}{K_{1}!} \cdots \frac{\left(-N_{t}^{\prime}\right)_{M_{t}^{\prime} K_{t}}}{K_{t}!} A\left[N_{1}^{\prime}, K_{1} ; \cdots ; N_{t}^{\prime}, K_{t}\right]$
In the document, we note :
$G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right)=\phi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) \theta_{1}\left(\eta_{G_{1}, g_{1}}\right) \cdots \theta_{r}\left(\eta_{G_{r}, g_{r}}\right)$
where $\phi\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right), \theta_{1}\left(\eta_{G_{1}, g_{1}}\right), \cdots, \theta_{r}\left(\eta_{G_{r}, g_{r}}\right)$ are given respectively in (1.2) and (1.3)

## 2. Generalized incomplete hypergeometric function.

The generalized incomplete hypergeometric function introduced by Srivastava et al [6 page 675, Eq.(4.1) is represented in the following manner.
${ }_{p} \gamma_{q}\left[\begin{array}{c}\left(\mathrm{e}_{1} ; \sigma\right),\left(e_{2}\right), \cdots,\left(e_{p}\right) \\ \cdots \\ \left(\mathrm{f}_{1}\right), \cdots,\left(f_{q}\right)\end{array} \quad ; z\right]=\sum_{n=0}^{\infty} \frac{\left(e_{1} ; \sigma\right)_{n}\left(e_{2}\right)_{n} \cdots\left(e_{p}\right)_{n}}{\left(f_{1}\right)_{n} \cdots\left(f_{q}\right)_{n}} \frac{z^{n}}{n!}$
where the incomplete Pochhammer symbols are defined as follows :

$$
\begin{align*}
& (a ; \sigma)_{n}=\frac{\gamma(a+n ; \sigma)}{\Gamma(a)} \quad(a, n \in \mathbb{C} ; x \geqslant 0)  \tag{2.2}\\
& \gamma(s, x)=\int_{0}^{x} t^{s-1} e^{-t} \mathrm{~d} t \quad(\operatorname{Re}(s)>0, x \geqslant 0) \tag{2.3}
\end{align*}
$$

## 3.Required formul.a

We have the following multiple integrals transformation, see Marichev et al. ([1], 33.416 page 590).
$\int_{x_{1} \geqslant 0} \cdots \int_{x_{n} \geqslant 0} e^{-p\left(x_{1}+\cdots+x_{n}\right)} \prod_{i=1}^{n} x_{i}^{v_{i}-1} \mathrm{~d} x_{1} \cdots \mathrm{~d} x_{n}=\frac{\Gamma\left(v_{1}\right) \cdots \Gamma\left(v_{n}\right)}{\Gamma\left(v_{1}+\cdots+v_{n}\right)} \times$
$\int_{0}^{1} x^{v_{1}+\cdots+v_{n}-1} e^{-p x} \mathrm{~d} x$
where $x_{1}+\cdots+x_{n} \leqslant 1, \operatorname{Re}(p)>0, v_{i}>0, i=1, \cdots, n$

## 4. Main integral

We note $X_{v_{1}, \cdots, v_{n}}=x_{1}^{v_{1}} \cdots x_{n}^{v_{n}} \quad$ and $A_{n^{\prime}}=\frac{\left(e_{1} ; \sigma\right)_{n}\left(e_{2}\right)_{n} \cdots\left(e_{p}\right)_{n}}{\left(f_{1}\right)_{n} \cdots\left(f_{q}\right)_{n}}$
we have the following formula

## Theorem

$$
\begin{aligned}
& \int_{x_{1} \geqslant 0} \cdots \int_{x_{n} \geqslant 0}{ }^{p \gamma_{q}}\left[\begin{array}{c}
\left(\mathrm{e}_{1} ; \sigma\right),\left(e_{2}\right), \cdots,\left(e_{p}\right) \\
\cdots \\
\left(\mathrm{f}_{1}\right), \cdots,\left(f_{q}\right)
\end{array} ; z X_{\xi_{1}, \cdots, \xi_{n}}\right] S_{N_{1}, \cdots, N_{t}}^{M_{1}^{\prime}, \cdots, M_{t}^{\prime}}\left(\begin{array}{c}
\mathrm{y}_{1} X_{\gamma_{1}^{(1)}, \cdots \gamma_{1}^{(n)}} \\
\cdots \\
\mathrm{y}_{t} X_{\gamma_{t}^{(1)} \ldots \gamma_{t}^{(n)}}
\end{array}\right) e^{-p\left(x_{1}+\cdots+x_{n}\right)} \\
& \aleph_{u: w}^{0, \mathfrak{n}: v}\left(\begin{array}{c}
\mathrm{z}_{1} X_{\alpha_{1}^{(1)}, \ldots \alpha_{1}^{(n)}} \\
\cdots \\
\mathrm{z}_{r} X_{\alpha_{r}^{(1)} \ldots \alpha_{r}^{(n)}}
\end{array}\right) \aleph_{U: W}^{0, N: V}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\eta_{1}^{(1)} \ldots \eta_{1}^{(n)}} \\
\cdots \cdots \\
\mathrm{Z}_{s} X_{\eta_{s}^{(1)} \ldots \eta_{s}^{(n)}}
\end{array}\right) \prod_{i=1}^{n} x_{i}^{v_{i}-1} \mathrm{~d} x_{1} \cdots \mathrm{~d} x_{n}=\sum_{K_{1}=0}^{\left[N_{1}^{\prime} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t}^{\prime} / M_{t}^{\prime}\right]} \\
& \sum_{n^{\prime}=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{M_{1}} \cdots \sum_{g_{r}=0}^{M_{r}} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots \eta_{G_{r}, g_{r}}\right) a_{1} \frac{A_{n^{\prime}} z^{n^{\prime}}}{n^{\prime}!} z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}}
\end{aligned}
$$

$$
\left.\begin{array}{c}
y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} \int_{0}^{1} x^{\sum_{i=1}^{n}\left(n^{\prime} \xi_{i}+\sum_{j=1}^{t} K_{j} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{j}, g_{j}} \alpha_{j}^{(i)}\right)-1} e^{-p x} \aleph_{U_{n, 1}: W}^{0, N+n: V}\left(\begin{array}{c}
\mathrm{Z}_{1} x_{1}^{\eta_{1}^{(1)}+\cdots+\eta_{1}^{(n)}} \\
\cdots \\
\mathrm{Z}_{s} x^{\eta_{s}^{(1)}+\cdots+\eta_{s}^{(n)}}
\end{array}\right. \\
{\left[1-\left(v_{i}+n^{\prime} \xi_{i}+\sum_{j=1}^{t} K_{i} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{j}^{(i)}\right) ; \eta_{1}^{(i)}, \cdots, \eta_{s}^{(i)}\right]_{1, n}, B: D}  \tag{4.1}\\
\cdots \\
\mathrm{~B}_{1}, C: D
\end{array}\right) \mathrm{d} x \quad .
$$

where : $B_{1}=\left\{1-\sum_{i=1}^{n}\left[v_{i}+n^{\prime} \xi_{i}+\sum_{j=1}^{t} K_{j} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{j}, g_{j}} \alpha_{j}^{(i)}\right] \quad ; \eta_{1}^{(1)}+\cdots+\eta_{1}^{(n)}\right.$,
$\left.\cdots, \eta_{s}^{(1)}+\cdots+\eta_{s}^{(n)}\right\}$

Provided that
a) $\min \left\{\xi_{i}, v_{i}, \gamma_{j}^{(i)}, \alpha_{k}^{(i)}, \eta_{l}^{(i)},\right\}>0, i=1, \cdots, n, j=1, \cdots, t, k=1, \cdots, r, l=1, \cdots, s$
b) $\operatorname{Re}\left(v_{i}+n^{\prime} \xi_{i}\right)+\sum_{j=1}^{r} \alpha_{j}^{(i)} \min _{1 \leqslant k \leqslant m_{i}} \operatorname{Re}\left(\frac{d_{k}^{(j)}}{\delta_{k}^{(j)}}\right)+\sum_{j=1}^{s} \eta_{j}^{(i)} \min _{1 \leqslant k \leqslant M_{i}}\left(\frac{b_{k}^{(j)}}{\beta_{k}^{(j)}}\right)>0, i=1, \cdots, n$
c) $\left|\arg z_{k}\right|<\frac{1}{2} A_{i}^{(k)} \pi$, where $A_{i}^{(k)}$ is defined by (1.5) ; $i=1, \cdots, r$
c) $\left|\arg Z_{k}\right|<\frac{1}{2} B_{i}^{(k)} \pi$, where $B_{i}^{(k)}$ is defined by (1.13); $i=1, \cdots, s$
d) The series occurring on the right-hand side of (4.1) is absolutely and uniformly convergent.

The quantities $U, V, W, A, B, C$ and $D$ are defined by the equations (1.14) to (1;19) respectively.

Proof of (4.1) : Let $M\left\}=\frac{1}{(2 \pi \omega)^{s}} \int_{L_{1}^{\prime}} \cdots \int_{L_{s}^{\prime}} \zeta\left(t_{1}, \cdots, t_{s}\right) \prod_{k=1}^{s} \phi_{k}\left(t_{k}\right)\{ \}\right.$. We have :
${ }_{p} \gamma_{q}\left[\begin{array}{c}\left(\mathrm{e}_{1} ; \sigma\right),\left(e_{2}\right), \cdots,\left(e_{p}\right) \\ \left(\mathrm{f}_{1}\right), \cdots,\left(f_{q}\right)\end{array} \quad ; y X_{\xi_{1}, \cdots, \xi_{n} ; \xi}\right] S_{N_{1}, \cdots, N_{t}}^{M_{1}^{\prime}, \cdots, M_{t}^{\prime}}\left(\begin{array}{c}\mathrm{y}_{1} X_{\gamma_{1}^{(1)}, \cdots, \gamma_{1}^{(n)}, \gamma_{1}} \\ \cdots \\ \mathrm{y}_{t} X_{\gamma_{t}^{(1)} \ldots, \gamma_{t}^{(n)}, \gamma_{t}}\end{array}\right)$
$\aleph_{u: w}^{0, \mathfrak{n}: v}\left(\begin{array}{c}\mathrm{z}_{1} X_{\alpha_{1}^{(1)}, \ldots \alpha_{1}^{(n)}, \alpha_{1}} \\ \cdots \\ \mathrm{z}_{r} X_{\alpha_{r}^{(1)} \ldots \alpha_{r}^{(n)}, \alpha_{r}}\end{array}\right) \aleph_{U: W}^{0, N: V}\left(\begin{array}{c}\mathrm{Z}_{1} X_{\eta_{1}^{(1)} \ldots \eta_{1}^{(n)}, \eta_{1}} \\ \cdots \\ \mathrm{Z}_{s} X_{\eta_{s}^{(1)} \ldots \eta_{s}^{(n)}, \eta_{s}}\end{array}\right)=\sum_{g_{1}=0}^{m_{1}} \cdots \sum_{g_{r}=0}^{m_{r}} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty}$

$$
\begin{align*}
& \sum_{K_{1}=0}^{\left[N_{1} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t} / M^{\prime}\right]} \sum_{n^{\prime}=0}^{\infty} A_{n^{\prime}} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) a_{1} \frac{y^{n^{\prime}}}{n^{\prime}!} z_{1}^{\eta_{G_{1}, g_{1}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}} y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} A_{n^{\prime}}} \\
& \prod_{j=1}^{t} X_{\gamma_{j}^{(1)}, \ldots, \gamma_{j}^{(n)}}^{K_{j}} X_{\xi_{(1)}^{\prime}, \cdots, \xi_{(n)} \prod_{j=1}^{n^{\prime}} X_{\alpha_{j}^{(1),,_{j}, \alpha_{j}^{(n)}}}^{\eta_{G_{j},}^{(1)}} M\left[\prod_{j=1}^{s} Z_{j}^{t_{j}} X_{\eta_{j}^{(1)}, \cdots, \eta_{j}^{(n)}}^{t_{j}}\right] \mathrm{d} t_{1} \cdots \mathrm{~d} t_{s}} . \tag{4.2}
\end{align*}
$$

Multiplying both sides of (4.3) by $f(t) e^{-p\left(x_{1}+\cdots+x_{n}\right)} \prod_{i=1}^{n} x_{i}^{v_{i}-1}$ and integrating with respect to $x_{1}, \cdots, x_{s}$ verifying the conditions e), changing the order of integrations and summations (which is easily seen to be justified due to the absolute convergence of the integrals and the summations involved in the process), we obtain :

$$
\sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{M_{1}} \cdots \sum_{g_{r}=0}^{M_{r}} \sum_{K_{1}=0}^{\left[N_{1}^{\prime} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t}^{\prime} / M_{t}^{\prime}\right]} \sum_{n^{\prime}=0}^{\infty} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) a_{1} \frac{A_{n^{\prime}} z^{n^{\prime}}}{n^{\prime}!}
$$

$$
\begin{align*}
& z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}} y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} \int_{x_{1} \geqslant 0} \cdots \int_{x_{n} \geqslant 0} \prod_{j=1}^{t} X_{\gamma_{j}^{(1)}, \ldots, \gamma_{j}^{(n)}}^{K_{j}} X_{\xi_{1}, \cdots, \xi_{n}}^{n_{j}^{\prime}} \prod_{j=1}^{r} X_{\alpha_{j}^{(1),}, \cdots, \alpha_{j}^{(n)}}^{\eta_{G_{j}, g_{j}}} \\
& \left\{M\left[\prod_{j=1}^{s} Z_{j}^{t_{j}} X_{\eta_{j}^{(1)}, \cdots, \eta_{j}^{(n)}}^{t_{j}}\right] \mathrm{d} t_{1} \cdots \mathrm{~d} t_{s}\right\} f(t) e^{-p\left(x_{1}+\cdots+x_{n}\right)} \prod_{i=1}^{n} x_{i}^{v_{i}-1} \mathrm{~d} x_{1} \cdots \mathrm{~d} x_{n} \tag{4.3}
\end{align*}
$$

Change the order of the $\left(x_{1}, \cdots, x_{n}\right)$-integrals and $\left(t_{1}, \cdots, t_{s}\right)$-integrals , we get :
$\sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{M_{1}} \cdots \sum_{g_{r}=0}^{M_{r}} \sum_{K_{1}=0}^{\left[N_{1}^{\prime} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t}^{\prime} / M_{t}^{\prime}\right]} \sum_{n^{\prime}=0}^{\infty} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots, \eta_{G_{r}, g_{r}}\right) a_{1} \frac{A_{n^{\prime}} z^{n^{\prime}}}{n^{\prime}!}$

$\left.\left.\prod_{i=1}^{n} x^{\xi_{i} n^{\prime}+\sum_{j=1}^{t} K_{j} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{j}, g_{j}} \alpha_{j}^{(i)}+\sum_{j=1}^{s} t_{j} \eta_{j}^{(i)}+v_{i}-1} \mathrm{~d} x_{1} \cdots \mathrm{~d} x_{n}\right] \mathrm{d} t_{1} \cdots \mathrm{~d} t_{s}\right\}$

Now, we transform the inner $\left(x_{1}, \cdots, x_{n}\right)$-integrals by using the equation (3.1) and interpreting the result thus obtained with the Mellin-barnes contour integrals (1.8), we arrive at the desired result.

## 5. Multivariable I-function

If $\iota_{i}, \iota_{i(1)}, \cdots, \iota_{i(s)} \rightarrow 1$, the Aleph-function of several variables reduces in the I-function of several variables. The multiple integrals have been derived in this section about the multivariable I-functions defined by Sharma and Ahmad [2].

## Corollary

$$
\begin{aligned}
& \left.\int_{x_{1} \geqslant 0} \cdots \int_{x_{n} \geqslant 0}{ }_{p \gamma_{q}}\left[\begin{array}{c}
\left(\mathrm{e}_{1} ; \sigma\right),\left(e_{2}\right), \cdots,\left(e_{p}\right) \\
\cdots \cdots X_{\xi_{1}, \cdots, \xi_{n}, \xi} \\
\left(\mathrm{f}_{1}\right), \cdots,\left(f_{q}\right)
\end{array}\right] S_{N_{1}, \cdots, N_{t}}^{M_{1}^{\prime}, \cdots, M_{t}^{\prime}} \begin{array}{c}
\mathrm{y}_{1} X_{\gamma_{1}^{(1)}, \cdots \gamma_{1}^{(n)}}^{\cdots} \\
\cdots \\
\mathrm{y}_{t} X_{\gamma_{t}^{(1)} \cdots \gamma_{t}^{(n)}}
\end{array}\right) e^{-p\left(x_{1}+\cdots+x_{n}\right)} \\
& \aleph_{u: w}^{0, \mathfrak{n}: v}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\alpha_{1}^{(1)}, \cdots \alpha_{1}^{(n)}} \\
\cdots \cdot \\
\mathrm{Z}_{r} X_{\alpha_{r}^{(1)} \cdots \alpha_{r}^{(n)}}
\end{array}\right) I_{U: W}^{0, N: V}\left(\begin{array}{c}
\mathrm{Z}_{1} X_{\eta_{1}^{(1)} \cdots \eta_{1}^{(n)}} \\
\cdots \cdot \cdot \\
\mathrm{Z}_{s} X_{\eta_{s}^{(1)} \cdots \eta_{s}^{(n)}}
\end{array}\right) \prod_{i=1}^{n} x_{i}^{v_{i}-1} \mathrm{~d} x_{1} \cdots \mathrm{~d} x_{n}=\sum_{K_{1}=0}^{\left[N_{1}^{\prime} / M_{1}^{\prime}\right]} \cdots \sum_{K_{t}=0}^{\left[N_{t}^{\prime} / M_{t}^{\prime}\right]} \\
& \sum_{n^{\prime}=0}^{\infty} \sum_{G_{1}, \cdots, G_{r}=0}^{\infty} \sum_{g_{1}=0}^{M_{1}} \cdots \sum_{g_{r}=0}^{M_{r}} \frac{(-)^{G_{1}+\cdots+G_{r}}}{\delta_{g_{1}} G_{1}!\cdots \delta_{g_{r}} G_{r}!} G\left(\eta_{G_{1}, g_{1}}, \cdots \eta_{G_{r}, g_{r}}\right) a_{1} \frac{A_{n^{\prime}} z^{n^{\prime}}}{n^{\prime}!} z_{1}^{\eta_{G_{1}, g_{1}}} \cdots z_{r}^{\eta_{G_{r}, g_{r}}}
\end{aligned}
$$

$$
\left.\begin{array}{l}
y_{1}^{K_{1}} \cdots y_{t}^{K_{t}} \int_{0}^{1} x^{\sum_{i=1}^{n}\left(n^{\prime} \xi_{i}+\sum_{j=1}^{t} K_{j} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{j}, g_{j}} \alpha_{j}^{(i)}\right)-1} e^{-p x} I_{U_{n, 1}: W}^{0, N+n: V}\left(\left.\begin{array}{c}
\mathrm{Z}_{1} x^{\eta_{1}^{(1)}+\cdots+\eta_{1}^{(n)}} \\
\cdots \\
\mathrm{Z}_{s} x^{(1)}+\cdots+\eta_{s}^{(n)}
\end{array} \right\rvert\,\right. \\
{\left[1-\left(v_{i}+n^{\prime} \xi_{i}+\sum_{j=1}^{t} K_{i} \gamma_{j}^{(i)}+\sum_{j=1}^{r} \eta_{G_{i}, g_{i}} \alpha_{j}^{(i)}\right) ; \eta_{1}^{(i)}, \cdots, \eta_{s}^{(i)}\right]_{1, n}, B: D}  \tag{5.1}\\
\cdots \\
\mathrm{~B}_{1}, C: D
\end{array}\right) \mathrm{d} x \quad .
$$

under the same existence conditions and notations that (4.1) with $\iota_{i}, \iota_{i(1)}, \cdots, \iota_{i}(s) \rightarrow 1$

## Remarks :

If $s=2$, we obtain the similar relation with the Aleph-function of two variables defined by Sharma [4].
If $\mathrm{s}=2$ and $\iota_{i}, \iota_{i}^{\prime}, \iota_{i}^{\prime \prime} \rightarrow 1$, the multivariable Aleph-function reduces to the I -function of two variables defined by Sharma and Mishra [3].

## 6. Conclusion

In this paper we have evaluated multiple integrals transformation involving the multivariable Aleph-functions, class of polynomials of several variables and generalized incomplete hypergeometric function. This relation established in this paper is of very general nature as it contains multivariable Aleph-function, which is a general function of several variables studied so far. Thus, the integral established in this research work would serve as a key formula from which, upon specializing the parameters, as many as desired results involving the special functions of one and several variables can be obtained.

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