

Strongly $(1,2)(\hat{g})^*$ Closed Sets In Bitopological Space

¹Ms. A. Kulandhai Therese, M.Sc., M.Phil., PGDOR., ²Ms. B. Dilshad, M.Sc.,

³Rev. Sr. Dr. Pauline Mary Helen M

¹ Assistant Professor, Department of Mathematics, St. Joseph's College of Arts and Science for Women, Periyar University,

²Department of Mathematics, St. Joseph's College of Arts and Science for Women, Periyar University,

³Principal, Nirmala College, Coimbatore, India.

ABSTRACT

In this paper, we study the concept of strongly $(1,2)(\hat{g})^*$ -closed sets and check how they deal with the bitopological spaces and their sub-sets. We also read out how the strongly $(1,2)(\hat{g})^*$ -closed sets and maps inter-relate with other sets with a change or transformation in their properties.

Key words: $\text{cl}(A)$, $\text{int}(A)$, strongly $(1,2)(\hat{g})^*$ -closed set, $(1,2)g$ -closed set, $(1,2)gs$ -closed set, $(1,2)g^*$ -closed set, $(1,2)g^{**}$ -closed set, $(1,2)sg^*$ -closed set, $(1,2)sg^{**}$ -closed set, $(1,2)(\hat{g})^*$ -closed set.

1. INTRODUCTION

A triple (X, τ_1, τ_2) , where X is a non-empty set and τ_1 and τ_2 are topologies on X is called a bitopological space. A.S. Mashhour [1] defined pro-open and pre-closed sets in 1982. N. Levine [4] introduced the class of (generalized closed sets) g -closed sets in 1970. S. P. Arya and Tour [3] defined gs -closed sets (generalized semi-closed sets) in 1990. M.K.R.S. Veerakumar [9] introduced g^* -closed sets in 1996. N. Levine [2] defined semi-open and semi-closed sets in 1963. D. Andrijevic [3] defined semi-pre open sets and semi-pre closed sets in 1986. Pauline Mary Helen. M, Veronica Vijayan, and Ponnuthai Selvarani .S [13] introduced g^{**} -closed sets in 2012. Pauline Mary Helen .M and Monica .P [12] introduced sg^{**} -closed sets in 2013. Veerakumar [14] introduced \hat{g} -closed sets in 1991. Pauline Mary Helen .M and A. Gayathri [15] introduced the class of $(\hat{g})^*$ sets in 2014. The intention of this paper is to give the basic properties of strongly $(1,2)(\hat{g})^*$ -closed set and how it works in relation with other sets.

2. PRELIMINARIES

We see the non-empty bitopological space (X, τ_1, τ_2) , a subset A of X and an open set U of X . We also see the terms, closure of A i.e. $\text{cl}(A)$ and interior of A i.e. $\text{int}(A)$.

Definition 2.1: Let A be a subset of a bitopological space (X, τ_1, τ_2) . The interior of A is defined as the union of all open sets contained in A . It is denoted by $\text{int}(A)$.

Definition 2.2: Let A be a subset of a bitopological space (X, τ_1, τ_2) . The closure of A is defined as the intersection of all closed sets containing A . It is denoted by $\text{cl}(A)$.

Clearly, $\text{int}(A)$ is open and $\text{cl}(A)$ is closed.

$$\text{int}(A) \subseteq A \subseteq \text{cl}(A)$$

If A is open, $A = \text{int}(A)$.

If A is closed, $A = \text{cl}(A)$.

Definition 2.3: A subset 'A' of the bitopological space (X, τ_1, τ_2) is called

1. a pre-open set [1] if $A \subseteq \text{int}(\text{cl}(A))$
2. a pre-closed set [1] if $\text{cl}(\text{int}(A)) \subseteq A$
3. a semi-open set [2] if $A \subseteq \text{cl}(\text{int}(A))$
4. a semi-closed set [2] if $\text{int}(\text{cl}(A)) \subseteq A$
5. a semi-pre open set [3] if $A \subseteq \text{cl}(\text{int}(\text{cl}(A)))$
6. a semi-pre closed set [3] if $\text{int}(\text{cl}(\text{int}(A))) \subseteq A$

Definition 2.4: A subset 'A' of a bitopological space (X, τ_1, τ_2) is called

1. (1,2)g-closed or generalized closed set [4] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **open** in (X, τ) .
2. (1,2)gs-closed or generalized semi-closed set [9] if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **open** in (X, τ) .
3. (1,2)g*-closed set [9] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **g-open** in (X, τ) .
4. (1,2)g** -closed set [13] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **g*-open** in (X, τ) .
5. (1,2)sg*-closed set [10] if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **g*-open** in (X, τ) .
6. (1,2)sg** -closed set [12] if $\text{scl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **g** -open** in (X, τ) .
7. (1,2) \hat{g} -closed set [14] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **semi-open** in (X, τ) .
8. (1,2) (\hat{g})* -closed set [15] if $\text{cl}(A) \subseteq U$ whenever $A \subseteq U$ and U is **\hat{g} -open** in (X, τ) .

3. BASIC PROPERTIES OF STRONGLY (\hat{g})*-CLOSED SET IN BITOPOLOGICAL SPACES

Definition 3.1:

A subset 'A' of a bitopological space (X, τ_1, τ_2) is said to be a strongly (1,2)(\hat{g})*-closed set, if $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in X.

Theorem 3.2:

Every τ_2 -closed set is strongly (1,2)(\hat{g})* -closed.

Proof:

Let (X, τ_1, τ_2) be a bitopological space.

And $A \subseteq (X, \tau_1, \tau_2)$ is a τ_2 -closed set.

i.e. $\tau_2\text{-Cl}(A) = A$.

To prove: A is strongly (1,2)(\hat{g})*-closed.

Let $A \subseteq U$ and U be $\tau_1\text{-}\hat{g}$ -open.

Then $\tau_2\text{-cl}(A) \subseteq U$.

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

We get, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

Theorem 3.3:

Every $(1,2)g$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)g$ -closed set.

By the definition 2.4.1,

$\tau_2\text{-Cl}(A) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

We've, $\tau_2\text{-cl}(A) \subseteq U$

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

Then, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in (X, τ) .

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.4:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)g$ -closed sets are $\{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

Now, $A = \{a\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)g$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)g$ -closed.

Theorem 3.5:

Every $(1,2)gs$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)gs$ -closed set.

By the definition 2.4.2,

$\tau_2\text{-scl}(A) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

We've, $\tau_2\text{-scl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(A) \subseteq U$

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

Then, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in X .

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.6:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)g_s$ -closed sets are $\{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

Now, $A = \{a\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)g_s$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)g_s$ -closed.

Theorem 3.7:

Every $(1,2)g^*$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)g^*$ -closed set.

By the definition 2.4.3,

$\tau_2\text{-cl}(A) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 - g -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

We've, $\tau_2\text{-scl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(A) \subseteq U$

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

Then, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in X .

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.8:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)g^*$ - closed sets are $\{c\}, \{b, c\}, \phi, X$.

Now, $A = \{b\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)g^*$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)g^*$ -closed.

Theorem 3.9:

Every $(1,2)g^{**}$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)g^{**}$ -closed set.

By the definition 2.4.4,

$\tau_2\text{-cl}(A) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 - g^* -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is τ_1 - \hat{g} -open.

We've, $\tau_2\text{-cl}(A) \subseteq U$

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

Then, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 - \hat{g} -open in X .

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.10:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)g^{**}$ - closed sets are $\{c\}, \{b, c\}, \{a, c\}, \phi, X$.

Now, $A = \{b\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)g^{**}$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)g^{**}$ -closed.

Theorem 3.11:

Every $(1,2)sg^*$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)sg^*$ -closed set.

By the definition 2.4.5,

$\tau_2\text{-scl}(A) \subseteq U$, whenever $A \subseteq U$ and U is τ_1 - g -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is τ_1 - \hat{g} -open.

We've, τ_2 -scl(A) $\subseteq U$

i.e. τ_2 -cl(A) $\subseteq U$

Also, τ_2 -cl(int(A)) $\subseteq \tau_2$ -cl(A)

Then, τ_2 -cl(int(A)) $\subseteq \tau_2$ -cl(A) $\subseteq U$

i.e. τ_2 -cl(int(A)) $\subseteq U$, whenever $A \subseteq U$ and U is τ_1 - \hat{g} -open in X .

$\therefore A$ is strongly (1,2)(\hat{g})*-closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.12:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly (1,2)(\hat{g})*-closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

(1,2)sg*-closed sets are $\{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

Now, $A = \{a\}$ is a strongly (1,2)(\hat{g})*-closed set but not (1,2)sg*-closed.

Hence, every strongly (1,2)(\hat{g})*-closed set need not be (1,2)sg*-closed.

Theorem 3.13:

Every (1,2)sg***-closed set is strongly (1,2)(\hat{g})*-closed.

Proof:

Let A be a (1,2)sg***-closed set.

By the definition 2.4.6,

τ_2 -scl(A) $\subseteq U$, whenever $A \subseteq U$ and U is τ_1 - g^* -open in (X, τ_1, τ_2) .

To prove: A is strongly (1,2)(\hat{g})*-closed.

Let $A \subseteq U$ and U is τ_1 - \hat{g} -open.

We've, τ_2 -scl(A) $\subseteq U$

i.e. τ_2 -cl(A) $\subseteq U$

Also, τ_2 -cl(int(A)) $\subseteq \tau_2$ -cl(A)

Then, τ_2 -cl(int(A)) $\subseteq \tau_2$ -cl(A) $\subseteq U$

i.e. τ_2 -cl(int(A)) $\subseteq U$, whenever $A \subseteq U$ and U is τ_1 - \hat{g} -open in X .

$\therefore A$ is strongly (1,2)(\hat{g})*-closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.14:

Let $X = \{a, b, c\}$

$$\tau_1 = \{\phi, X, \{a\}\}$$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$$\tau_2 = \{\phi, X, \{a, b\}\}$$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)sg^{**}$ -closed sets are $\{c\}, \{b, c\}, \phi, X$.

Now, $A = \{b\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)sg^{**}$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)sg^{**}$ -closed.

Theorem 3.15:

Every $(1,2)(\hat{g})$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)(\hat{g})$ -closed set.

By the definition 2.4.7,

$$\tau_2\text{-cl}(A) \subseteq U, \text{ whenever } A \subseteq U \text{ and } U \text{ is } \tau_1\text{-semi-open in } (X, \tau_1, \tau_2).$$

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

$$\text{We've, } \tau_2\text{-cl}(A) \subseteq U$$

$$\text{Also, } \tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$$

$$\text{Then, } \tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$$

$$\text{i.e. } \tau_2\text{-cl}(\text{int}(A)) \subseteq U, \text{ whenever } A \subseteq U \text{ and } U \text{ is } \tau_1\text{-}\hat{g}\text{-open in } X.$$

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.16:

Let $X = \{a, b, c\}$

$$\tau_1 = \{\phi, X, \{a\}\}$$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$$\tau_2 = \{\phi, X, \{a, b\}\}$$

τ_2 -closed sets are $X, \phi, \{c\}$

Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)(\hat{g})$ -closed sets are $\{c\}, \{b, c\}, \phi, X$.

Now, $A = \{b\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)(\hat{g})$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)(\hat{g})$ -closed.

Theorem 3.17:

Every $(1,2)(\hat{g})^*$ -closed set is strongly $(1,2)(\hat{g})^*$ -closed.

Proof:

Let A be a $(1,2)(\hat{g})^*$ -closed set.

By the definition 2.4.8,

$\tau_2\text{-cl}(A) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in (X, τ_1, τ_2) .

To prove: A is strongly $(1,2)(\hat{g})^*$ -closed.

Let $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open.

We've, $\tau_2\text{-cl}(A) \subseteq U$

Also, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A)$

Then, $\tau_2\text{-cl}(\text{int}(A)) \subseteq \tau_2\text{-cl}(A) \subseteq U$

i.e. $\tau_2\text{-cl}(\text{int}(A)) \subseteq U$, whenever $A \subseteq U$ and U is $\tau_1\text{-}\hat{g}$ -open in X .

$\therefore A$ is strongly $(1,2)(\hat{g})^*$ -closed.

The converse of the above theorem need not be true as shown in the following example.

Example 3.18:

Let $X = \{a, b, c\}$

$\tau_1 = \{\phi, X, \{a\}\}$

τ_1 -closed sets are $X, \phi, \{b, c\}$

$\tau_2 = \{\phi, X, \{a, b\}\}$

τ_2 -closed sets are $X, \phi, \{c\}$

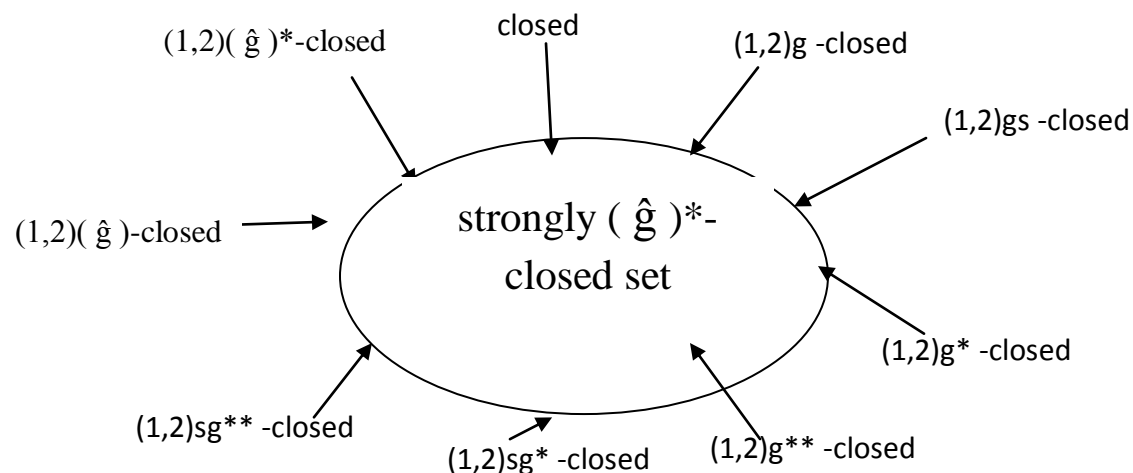
Strongly $(1,2)(\hat{g})^*$ -closed sets are $\{a\}, \{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

$(1,2)(\hat{g})^*$ -closed sets are $\{b\}, \{c\}, \{a, b\}, \{b, c\}, \{a, c\}, \phi, X$.

Now, $A = \{a\}$ is a strongly $(1,2)(\hat{g})^*$ -closed set but not $(1,2)(\hat{g})^*$ -closed.

Hence, every strongly $(1,2)(\hat{g})^*$ -closed set need not be $(1,2)(\hat{g})^*$ -closed.

The above results can be represented in the following figure:



Where $A \rightarrow B$ represents A implies B and B need not imply A .

CONCLUSION

Hence, I would like to conclude my paper by giving the properties of strongly $(1,2)(\hat{g})^*$ -closed set. And also with further results and solutions we can bring in the comparison of strongly $(1,2)(\hat{g})^*$ -closed set and function with other sets and functions as well in a given bitopological space.

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