Original Article

# On Slightly Ng<sup>#</sup>– Continuous Functions in Neutrosophic Topological Space

Babisha Julit R L<sup>1</sup>, Pious Missier S<sup>2</sup>

<sup>1</sup>Research Scholar (Reg.No-19212052092006), Department of Mathematics, G. Venkataswamy Naidu College, Kovilpatti, (Affiliated to Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli), Tamil Nadu, India. <sup>2</sup>Head & Associate Professor, Department of Mathematics, Don Bosco College of Arts and Science, Keela Eral, Thoothukudi,

(Affiliated to Manonmaniam Sundaranar University, Abishekapatti, Tirunelveli) Tamil Nadu, India.

Abstract — In this article, we present and study a new class of Neutrosophic functions namely, slightly Neutrosophic  $g^{\#}$ - continuous functions. Moreover, we discuss its relationship with some other related functions.

**Keywords** —  $Ng^{#}$  - closed set,  $Ng^{#}$  - open set,  $Ng^{#}$  - continuous function,  $Ng^{#}$  - contra continuous function, slightly  $Ng^{#}$  - continuous function.

### I. INTRODUCTION

In 1965, Zadeh [21] introduced fuzzy set theoryas a mathematical tool for dealing with uncertainities where each element had a degree of membership. The Intuitionistic fuzzy set was introduced by Atanassov[2] in 1983 as a generalization of fuzzy set, where besides the degree of membership and the degree of non- membership of each element. Smarandache [8] introduced the idea of Neutrosophic set and explained, neutrosophic set is a generalization of Intuitionistic fuzzyset. In 2014 Salama et.al. [17] initiated further studies into Neutrosophic closed sets and Neutrosophic continuous functions. Recently Pious Missier et.al.[11],[12], introduced the concept of  $Ng^{#-}$  closed sets, continuous and irresolute mappings, in Neutrosophic Topological Spaces. Here, the notion of  $Ng^{#-}$  closed sets is applied to introduce a new class of continuity in the consept of Neutrosophic topology called slightly  $Ng^{#-}$  continuous functions and investigate its properties.

#### II. PRELIMINARIES

#### **Definition 2.1.** [8]

A Neutrosophic set (NS)  $A_N$  is an object having the form  $A_N = \{\langle x, \mu_{AN}(x), \sigma_{AN}(x), \gamma_{AN}(x) \rangle : x \in X\}$  where  $\mu_{AN}(x), \sigma_{AN}(x)$ and  $\gamma_{AN}(x)$  represent the degree of membership, degree of indeterminacy and the degree of non-membership respectively of each element  $x \in X$  to the set  $A_N$ . A Neutrosophic set  $A_N = \{\langle x, \mu_{AN}(x), \sigma_{AN}(x), \gamma_{AN}(x) \rangle : x \in X\}$  can be identified as an ordered triple  $\langle \mu_{AN}(x), \sigma_{AN}(x), \gamma_{AN}(x) \rangle$  in ]–0,1+[ on X.

# **Definition 2.2.** [17]

For any two Neutrosophic sets  $A_N = \{ \langle x, \mu_{AN}(x), \sigma_{AN}(x), \gamma_{AN}(x) \rangle : x \in X \}$  and  $B_N = \{ \langle x, \mu_{BN}(x), \sigma_{BN}(x), \gamma_{BN}(x) \rangle : x \in X \}$  we have

- 1.  $A_N \subseteq B_N \iff \mu_{AN}(x) \le \mu_{BN}(x), \sigma_{AN}(x) \le \sigma_{BN}(x) \text{ and } \gamma_{AN}(x) \ge \gamma_{BN}(x).$
- 2.  $A_N \cap B_N = \langle x, \mu_{AN}(x) \land \mu_{BN}(x), \sigma_{AN}(x) \land \sigma_{BN}(x) \text{ and } \gamma_{AN}(x) \lor \gamma_{BN}(x) \rangle$ .
- 3.  $A_N \cup B_N = \langle x, \mu_{AN}(x) \lor \mu_{BN}(x), \sigma_{AN}(x) \lor \sigma_{BN}(x) \text{ and } \gamma_{AN}(x) \land \gamma_{BN}(x) \rangle$ .

**Definition 2.3.** [17] Let  $A_N = \langle \mu_{AN}(x), \sigma_{AN}(x), \gamma_{AN}(x) \rangle$  be a NS on X, then the complement

 $A_N^c$  defined as

 $A_{N}^{c} = \{ \langle x, \gamma_{AN}(x), 1 - \sigma_{AN}(x), \mu_{AN}(x) \rangle : x \in \mathbf{X} \}$ 

Note that for any two Neutrosophic sets  $A_N$  and  $B_N$ ,

- $(\mathbf{A}_{\mathbf{N}} \cup \mathbf{B}_{\mathbf{N}})^c = \mathbf{A}_{\mathbf{N}}^c \cap \mathbf{B}_{\mathbf{N}}^c$
- $(A_N \cap B_N)^c = A_N^c \cup B_N^c$

**Definition 2.4.** [17] A Neutrosophic topology (NT ) on a non-empty set X is a family  $\tau$  of Neutrosophic subsets in X satisfies the following axioms:

- **1.**  $0_N, 1_N \in \tau$
- 2.  $R_{N1} \cap R_{N2} \in \tau$  for any  $R_{N1}, R_{N2} \in \tau$

3.  $\cup R_{Ni} \in \tau \forall R_{Ni} : i \in I \subseteq \tau$ 

Here the empty set  $\mathbf{0}_{N}$  and the whole set  $\mathbf{1}_{N}$  may be defined as follows:

- **1.**  $\mathbf{0}_{N} = \{ \langle x, 0, 0, 1 \rangle : x \in X \}$
- 2.  $\mathbf{1}_{N} = \{ \langle x, 1, 1, 0 \rangle : x \in X \}$

# **Definition 2.5.** [17] Let $A_N$ be a NS in NTS $X_N$ . Then

- **1.** Nint(A<sub>N</sub>) =  $\bigcup$  {*G* : *G* is a NOS in *X*<sub>N</sub> and *G*  $\subseteq$  A<sub>N</sub>} is called a Neutrosophic interior of A<sub>N</sub>.
- 2.  $Ncl(A_N) = \bigcap \{K : K \text{ is a NCS in } X_N \text{ and } A_N \subseteq K\}$  is called Neutrosophic closure of  $A_N$ .

**Definition 2.6.** [9] A Neutrosophic set  $A_N$  of a NTS  $(X, \tau)$  is called a neutrosophic NagCS if Nacl $(A_N) \subseteq U_N$ , whenever  $A_N \subseteq U_N$  and  $U_N$  is a NOS in X. The complement of NagCS is NagOS.

**Definition 2.7.** [11] A Neutrosophic set  $A_N$  of a NTS  $(X, \tau)$  is called a Neutrosophic  $g^{\#}$ -closed  $(Ng^{\#}CS)$  if  $Ncl(A_N) \subseteq Q_N$  whenever  $A_N \subseteq Q_N$  and  $Q_N$  is  $N\alpha gOS$  in X. The complement of  $Ng^{\#}CS$  is  $Ng^{\#}OS$ .

# **Definition 2.8.** [16] Let $A_N$ be a NS in NTS X. Then

- 1.  $Ng^{\#}int(A_N) = \bigcup \{G : G \text{ is a } Ng^{\#}OS \text{ in } X \text{ and } G \subseteq A_N\}$  is called a Neutrosophic  $g^{\#}$  interior of  $A_N$ .
- 2.  $Ng^{\#}cl(A_N) = \bigcap \{K : K \text{ is a } Ng^{\#}CS \text{ in } X \text{ and } A_N \subseteq K\}$  is called Neutrosophic  $g^{\#}$  closure of  $A_N$ .

**Definition 2.9.** [12] A function  $f_N : (X, \tau) \to (Y, \zeta)$  is said to be  $Ng^{\#-}$  continuous function if  $f_N^{-1}(V_N)$  is a  $Ng^{\#-}$  closed set of  $(X, \tau)$  for every neutrosophic closed set  $V_N$  of  $(Y, \zeta)$ .

**Definition 2.10.** [12] A function  $f_N : (X, \tau) \to (Y, \zeta)$  is said to be Neutrosophic  $g^{\#-}$  irresolute function if  $f_N^{-1}(V_N)$  is a  $Ng^{\#}CS$  of  $(X, \tau)$  for every  $Ng^{\#}CS V_N$  of  $(Y, \zeta)$ .

**Definition 2.11.** [16] A Neutrosophic Topological space  $(X, \tau)$  is called a  $T_N g^{\#}$ - space if every  $N g^{\#} CS$  in  $(X, \tau)$  is NCS in  $(X, \tau)$ .

**Definition 2.12.** [5] A function  $f_N : (X, \tau) \to (Y, \zeta)$  is said to be neutrosophic contra continuous if  $f_N^{-1}(V_N)$  is a neutrosophic closed set of  $(X, \tau)$  for every neutrosophic open set  $(Y, \zeta)$ .

**Definition 2.13.** [13] A function  $f_N: (X,\tau) \to (Y,\zeta)$  is said to be  $Ng^{\#-}$  contra continuous if  $f_N^{-1}(V_N)$  is a  $Ng^{\#-}$  closed set of  $(X,\tau)$  for every neutrosophic open set  $(Y,\zeta)$ .

**Definition 2.14.** [14] A function  $f_N: (X,\tau) \to (Y,\zeta)$  is said to be perfectly  $Ng^{\#-}$  continuous if the inverse image of every  $Ng^{\#-}$  closed set in  $(Y,\zeta)$  is both NOS and NCS (ie, Neutrosophic clopen set) in  $(X,\tau)$ .

**Definition 2.15.** [15] A function  $f_N: (X,\tau) \to (Y,\zeta)$  is said to be totally  $Ng^{\#-}$  continuous if the inverse image of every Neutrosophic closed set in  $(Y,\zeta)$  is both  $Ng^{\#}CS$  and  $Ng^{\#}OS$  (ie,  $Ng^{\#-}$  clopen set) in  $(X,\tau)$ .

# III. SLIGHTLY Ng<sup>#</sup>– CONTINUOUS FUNCTIONS

**Definition 3.1.** A function  $f_N: (X,\tau) \longrightarrow (Y,\zeta)$  is said to be slightly  $Ng^{\#}$  continuous if the inverse image of every Neutrosophic clopen set in  $(Y,\zeta)$  is  $Ng^{\#}CS$  in  $(X,\tau)$ .

**Example 3.2.** Let  $X = \{l, m\} = Y$  Consider the Neutrosophic sets

$$\begin{split} \mathbf{M}_{N1} &= \{ \langle l, (0.6, 0.5, 0.3) \rangle, \langle m, (0.5, 0.6, 0.4) \rangle \}, \quad \mathbf{M}_{N2} = \{ \langle l, (0.3, 0.5, 0.6) \rangle, \langle m, (0.4, 0.4, 0.5) \rangle \}, \\ \mathbf{M}_{N3} &= \{ \langle l, (0.5, 0.6, 0.4) \rangle, \langle m, (0.6, 0.5, 0.3) \rangle \}, \quad \mathbf{M}_{N4} = \{ \langle l, (0.4, 0.4, 0.5) \rangle, \langle m, (0.3, 0.5, 0.6) \rangle \}. \\ \text{Now Then } \tau &= \{ \mathbf{0}_{N}, \mathbf{M}_{N1}, \mathbf{M}_{N2}, \mathbf{1}_{N} \} \text{ and } \zeta = \{ \mathbf{0}_{N}, \mathbf{M}_{N3}, \mathbf{M}_{N4}, \mathbf{1}_{N} \} \text{ are NT } s \text{ on X and Y respectively. Define } f_{N} : (X, \tau) \to (Y, \zeta) \text{ by } \\ f_{N}(l) &= m \text{ and } f_{N}(m) = l. \text{ Here } Ng^{\#}CS(X) = \{ \mathbf{0}_{N}, \mathbf{M}_{N1}, \mathbf{M}_{N2}, \mathbf{1}_{N} \}, \text{NCOS}(Y) = \{ \mathbf{0}_{N}, \mathbf{M}_{N3}, \mathbf{M}_{N4}, \mathbf{1}_{N} \}. \text{ Now } f_{N}^{-1}(\mathbf{M}_{N3}) = \mathbf{M}_{N1} \text{ and } \\ f_{N}^{-1}(\mathbf{M}_{N4}) &= \mathbf{M}_{N2} \text{ are } Ng^{\#}CS \text{ in } (X, \tau). \text{ Therefore, } f_{N} \text{ is slightly } Ng^{\#} - \text{ continuous.} \end{split}$$

**Theorem 3.3.** Every  $Ng^{\#-}$  continuous function is slightly  $Ng^{\#-}$  continuous function. **Proof.** Let  $f_N: (X,\tau) \to (Y,\zeta)$  be any neutrosophic function. Let  $A_N$  be a N- clopen in  $(Y,\zeta)$ . Then  $A_N$  is NCS in  $(Y,\zeta)$ . Since  $f_N$  is a  $Ng^{\#-}$  continuous function,  $f_N^{-1}(A_N)$  is  $Ng^{\#}CS$  in  $(X,\tau)$ . Hence,  $f_N$  is totally  $Ng^{\#-}$  continuous function.

**Remark 3.4.** Reverse implication of above theorem need not be true as seen in the following example.

**Example 3.5.** Let  $X = \{l, m\} = Y$  Consider the Neutrosophic sets  $M_{N1} = \{\langle l, (0.6, 0.5, 0.3) \rangle, \langle m, (0.5, 0.6, 0.4) \rangle\}, M_{N2} = \{\langle l, (0.3, 0.5, 0.6) \rangle, \langle m, (0.4, 0.4, 0.5) \rangle\},$   $M_{N3} = \{\langle l, (0.5, 0.6, 0.4) \rangle, \langle m, (0.6, 0.5, 0.3) \rangle\}, M_{N4} = \{\langle l, (0.4, 0.4, 0.5) \rangle, \langle m, (0.3, 0.5, 0.6) \rangle\},$   $M_{N5} = \{\langle l, (0.7, 0.6, 0.2) \rangle, \langle m, (0.6, 0.7, 0.3) \rangle\}, M_{N6} = \{\langle l, (0.2, 0.4, 0.7) \rangle, \langle m, (0.3, 0.3, 0.6) \rangle\}.$ Now Then  $\tau = \{\mathbf{0}_N, M_{N1}, M_{N2}, \mathbf{1}_N\}$  and  $\zeta = \{\mathbf{0}_N, M_{N3}, M_{N4}, M_{N5}, \mathbf{1}_N\}$  are NT *s* on X and Y respectively. Define  $f_N : (X, \tau) \rightarrow$   $(Y, \zeta)$  by  $f_N(l) = m$  and  $f_N(m) = l$ . Here  $Ng^{\#}CS(X) = \{\mathbf{0}_N, M_{N1}, M_{N2}, \mathbf{1}_N\}, NCOS(Y) = \{\mathbf{0}_N, M_{N3}, M_{N4}, \mathbf{1}_N\}.$  Now  $f_N^{-1}(M_{N3}) = M_{N1}$ and  $f_N^{-1}(M_{N4}) = M_{N2}$  are  $Ng^{\#}CS$  in  $(X, \tau)$ . Therefore,  $f_N$  is slightly  $Ng^{\#}$ - continuous. But  $M_{N6}$  is NCS in Y but  $f_N^{-1}(M_{N6})$  is not  $Ng^{\#}CS$  in  $(X, \tau)$ . Therefore,  $f_N$  is not  $Ng^{\#}$ - continuous.

**Theorem 3.6.** Every  $Ng^{\#-}$  contra continuous function is slightly  $Ng^{\#-}$  continuous function. **Proof.** Let  $f_N : (X, \tau) \to (Y, \zeta)$  be any neutrosophic function. Let  $A_N$  be a N- clopen in  $(Y, \zeta)$ . Then  $A_N$  is NOS in  $(Y, \zeta)$ . Since  $f_N$  is a  $Ng^{\#-}$  contra continuous function,  $f_N^{-1}(A_N)$  is  $Ng^{\#}CS$  in  $(X, \tau)$ . Hence,  $f_N$  is totally  $Ng^{\#-}$  continuous function.

**Remark 3.7.** Converse of above theorem need not be true as seen in the following example.

**Example 3.8.** Let  $X = \{l, m\} = Y$  Consider the Neutrosophic sets

 $\mathbf{M}_{\mathrm{N1}} = \{ \langle l, (0.7, 0.5, 0.3) \rangle, \langle m, (0.6, 0.6, 0.4) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N1}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle m, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle l, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.3, 0.5, 0.7) \rangle, \langle l, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.4, 0.4, 0.6) \rangle, \langle l, (0.4, 0.4, 0.6) \rangle \}, \ \mathbf{M}_{\mathrm{N2}} = \{ \langle l, (0.4, 0.4, 0.6) \rangle, \langle$ 

 $\mathbf{M}_{N3} = \{ \langle l, (0.6, 0.6, 0.4) \rangle, \langle m, (0.7, 0.5, 0.3) \rangle \}, \ \mathbf{M}_{N4} = \{ \langle l, (0.4, 0.4, 0.6) \rangle, \langle m, (0.3, 0.5, 0.7) \rangle \}, \$ 

 $M_{N5} = \{ \langle l, (0.7, 0.8, 0.2) \rangle, \langle m, (0.7, 0.8, 0.3) \rangle \}, M_{N6} = \{ \langle l, (0.2, 0.2, 0.7) \rangle, \langle m, (0.3, 0.2, 0.7) \rangle \}.$ 

Now Then  $\tau = \{\mathbf{0}_N, \mathbf{M}_{N1}, \mathbf{M}_{N2}, \mathbf{1}_N\}$  and  $\zeta = \{\mathbf{0}_N, \mathbf{M}_{N3}, \mathbf{M}_{N4}, \mathbf{M}_{N6}, \mathbf{1}_N\}$  are NT *s* on X and Y respectively. Define  $f_N : (X, \tau) \rightarrow (Y, \zeta)$  by  $f_N(l) = m$  and  $f_N(m) = l$ . Here  $Ng^{\#}CS(X) = \{\mathbf{0}_N, \mathbf{M}_{N1}, \mathbf{M}_{N2}, \mathbf{1}_N\}$ , NCOS(Y) =  $\{\mathbf{0}_N, \mathbf{M}_{N3}, \mathbf{M}_{N4}, \mathbf{1}_N\}$ . Now  $f_N^{-1}(\mathbf{M}_{N3}) = \mathbf{M}_{N1}$  and  $f_N^{-1}(\mathbf{M}_{N4}) = \mathbf{M}_{N2}$  are  $Ng^{\#}CS$  in  $(X, \tau)$ . Therefore,  $f_N$  is slightly  $Ng^{\#}$ - continuous. But  $\mathbf{M}_{N6}$  is NOS in Y but  $f_N^{-1}(\mathbf{M}_{N6})$  is not  $Ng^{\#}CS$  in  $(X, \tau)$ . Therefore,  $f_N$  is not  $Ng^{\#}$ - contra continuous.

**Remark 3.9.** Composition of two slightly  $Ng^{\#-}$  continuous functions need not be a slightly  $Ng^{\#-}$  continuous function. **Example 3.10.** Let  $X = \{p,q\} = Y = Z$   $M_{N1} = \{\langle p, (0.7, 0.5, 0.3) \rangle, \langle m, (0.6, 0.6, 0.4) \rangle\}, M_{N2} = \{\langle p, (0.3, 0.5, 0.7) \rangle, \langle q, (0.4, 0.4, 0.6) \rangle\},$   $M_{N3} = \{\langle p, (0.6, 0.6, 0.4) \rangle, \langle q, (0.7, 0.5, 0.3) \rangle\}, M_{N4} = \{\langle p, (0.4, 0.4, 0.6) \rangle, \langle q, (0.3, 0.5, 0.7) \rangle\},$   $M_{N5} = \{\langle p, (0.2, 0.3, 0.8) \rangle, \langle q, (0.3, 0.2, 0.7) \rangle\}, M_{N6} = \{\langle p, (0.8, 0.7, 0.2) \rangle, \langle q, (0.7, 0.8, 0.3) \rangle\}.$ Now  $(X, \tau) = \{\mathbf{0}_N, M_{N1}, M_{N2}, \mathbf{1}_N\}, (Y, \zeta) = \{\mathbf{0}_N, M_{N3}, M_{N4}, M_{N5}, M_{N6}, \mathbf{1}_N\} = (Z, \eta)$  are Neutrosophic topological spaces. Then  $\tau = \{\mathbf{0}_N, M_{N1}, M_{N2}, \mathbf{1}_N\}, \zeta = \{\mathbf{0}_N, M_{N3}, M_{N4}, M_{N6}, \mathbf{1}_N\}$  and  $\eta = \{\mathbf{0}_N, M_{N5}, M_{N6}, \mathbf{1}_N\}$  are Neutrosophic topologies on X, Y and Z respectively. Define a function  $f_N: (X,\tau) \to (Y,\zeta)$  by  $f_N(p) = q$  and  $f_N(q) = p$  and define a function  $g_N: (Y,\zeta) \to (Z,\eta)$  by  $g_N(p) = p$  and  $g_N(q) = q$ . Then  $f_N$  and  $g_N$  are slightly  $Ng^{\#-}$  continuous functions. Now define a function  $g_N \circ f_N: (X,\tau) \to (Z,\eta)$  by  $g_N \circ f_N(p) = p$  and  $g_N \circ f_N(q) = q$ . Here  $M_{N5}$  and  $M_{N6}$  are NCOS in  $(Z,\eta)$ . But  $(g_N \circ f_N)^{-1}(M_{N5})$  is not a  $Ng^{\#}CS$  in  $(X,\tau)$ . Hence  $(g_N \circ f_N)$  is not a slightly  $Ng^{\#-}$  continuous function.

**Theorem 3.11.** Let  $f_N: (X,\tau) \to (Y,\zeta)$  and  $g_N: (Y,\zeta) \to (Z,\eta)$  be any two Neutrosophic mappings. Then

1.  $(g_N \circ f_N) : (X,\tau) \to (Z,\eta)$  is slightly  $Ng^{\#-}$  continuous if  $g_N$  is slightly  $Ng^{\#-}$  continuous and  $f_N$  is  $Ng^{\#-}$  irresolute.

2.  $(g_N \circ f_N) : (X,\tau) \to (Z,\eta)$  is slightly  $Ng^{\#-}$  continuous if  $g_N$  is  $Ng^{\#-}$  continuous and  $f_N$  is  $Ng^{\#-}$  irresolute.

3.  $(g_N \circ f_N) : (X, \tau) \to (Z, \eta)$  is  $Ng^{\#}$ - irresolute if  $g_N$  is perfectly  $Ng^{\#}$ - continuous and  $f_N$  is slightly  $Ng^{\#}$ - continuous.

4.  $(g_{N^{\circ}}f_{N})$ :  $(X,\tau) \rightarrow (Z,\eta)$  is slightly Ng<sup>#</sup>- continuous if  $g_{N}$  is Ng<sup>#</sup>- contra continuous and  $f_{N}$  is Ng<sup>#</sup>- irresolute. **Proof.** :

(1) Let  $W_N$  be a Neutrosophic clopen set in  $(Z, \eta)$ . By hypothesis,  $g_N^{-1}(W_N)$  is a  $Ng^{\#}CS$  in  $(Y, \zeta)$ . Since  $f_N$  is a  $Ng^{\#}-$  irresolute function,  $f_N^{-1}(g_N^{-1}(W_N))$  is a  $Ng^{\#}CS$  in  $(X, \tau)$ . Hence  $g_N \circ f_N$  is a slightly  $Ng^{\#}-$  continuous function.

(2) Let  $W_N$  be a Neutrosophic clopen set in  $(Z,\eta)$ . Then  $W_N$  is NCS  $(Z,\eta)$ . By hypothesis,  $g_N^{-1}(W_N)$  is a  $Ng^{\#}CS$  in  $(Y,\zeta)$ . Since  $f_N$  is a  $Ng^{\#-}$  irresolute function,  $f_N^{-1}(g_N^{-1}(W_N))$  is a  $Ng^{\#}CS$  in  $(X,\tau)$ . Hence  $g_N \circ f_N$  is a slightly  $Ng^{\#-}$  continuous function.

(3) Let  $W_N$  be a  $Ng^{\#}CS$  in  $(Z,\eta)$ . Since  $f_N$  is perfectly  $Ng^{\#-}$  continuous,  $g_N^{-1}(W_N)$  is Neutrosophic clopen set in  $(Y,\zeta)$ . Since  $f_N$  is slightly  $Ng^{\#-}$  continuous,  $f_N^{-1}(g_N^{-1}(W_N))$  is  $Ng^{\#}CS$  in  $(X,\tau)$ . Therefore  $g_N \circ f_N$  is  $Ng^{\#-}$  irresolute.

(4) Let  $W_N$  be a Neutrosophic clopen set in  $(Z,\eta)$ . Then  $W_N$  is NOS  $(Z,\eta)$ . By hypothesis,  $g_N^{-1}(W_N)$  is a  $Ng^{\#}CS$  in  $(Y,\zeta)$ . Since  $f_N$  is  $Ng^{\#}$ - irresolute function,  $f_N^{-1}(g_N^{-1}(W_N))$  is a  $Ng^{\#}CS$  in  $(X,\tau)$ . Hence  $g_N \circ f_N$  is a slightly  $Ng^{\#}$ - continuous function.

#### VI. CONCLUSION

In this article we introduced a new class of continuous function in Neutrosophic Topological space called slightly  $Ng^{\#-}$  continuous function. Further, characterizations of totally  $Ng^{\#-}$  continuous functions are analyzed and studied their properties.

#### REFERENCES

- S. Anitha, K. Mohana, Florentin Samarandache, On Ngsr Closed Sets in Neutrosophic Topological Spaces, Neutrosophic Sets and Systems, 28. (2019) 171-177.
- [2] K. T. Atanassov, Intuitionistic Fuzzy Sets, Fuzzy Sets and Systems, 20 (1986) 87-96.
- [3] C. L. Chang, Fuzzy Topological Spaces, J.Math.Anal.Appl., 24 (1968) 182-190.
- [4] R. Dhavaseelan and S. Jafari, Generalized Neutrosophic Closed Sets, New Trends in Neutrosophic Theory and Applications, 2 (2018) 261-273.
- [5] R. Dhavaseelan And S. Jafari, C. Ozel and M. A. Al-Shumrani Generalized Neutrosophic Contracontinuous, New Trends in Neutrosophic Theory and Applications, 2 (2017) 355-370.
- [6] R.Dhavaseelan, S. Jafari and Md. Hanif Page, Neutrosophic Generalized A- Contracontinuity, Creat. Math. Inform. 20(2) (2011) 1-6.
- [7] Dogan Coker, An Introduction to Intuitionistic Fuzzy Topological Spaces, Fuzzy Sets and Systems, 88 (1) (1997) 81-89.
- [8] Floretin Smarandache, Neutrosophic Set:- A Generalization of Intuitionistiic Fuzzy Set, Journal of Defense Resourses Management, 1 (2010) 107–116.
- D. Jayanthi, On a Generalized Closed Sets in Neutrosophic Topological Spaces, International Conference on Recent Trends in Mathematics And Information Technology, (2018) 88-91.
- [10] N.Levine, Generalized Closed Set In Topology, Rend.Circ.Mat Palermo, 19 (1970) 89-96.
- [11] S. Pious Missier, R.L. Babisha Julit, On Neutrosophic Generalized Closed Sets, Punjab University Journal of Mathematics (Submited)
- [12] S. Pious Missier, R.L. Babisha Julit, On Neurosophic G<sup>#</sup> Continuous Functions and Neurosophic G<sup>#</sup>- Irresolute Functions, Abstract Proceedings of 24th Fai-Icdbsmd. 6(1) (2021) 49.
- S. Pious Missier, R.L. Babisha Julit, On Ng<sup>#</sup>- Contra Continuous Functions in Neutrosophic Topological Space, Design Engineering, 6 (2021) 8606-8614.
- [14] S. Pious Missier, R.L. Babisha Julit, New Type of Continuous Functions on Neutrosophic Topological Space. (Submitted)
- [15] S. Pious Missier, R.L. Babisha Julit, J. Martina Jency, Ng<sup>#</sup>- Homeomorphism in Neutrosophic Topological Space, International Journal of Mechanical Engineering, 6(3) (2021) 2801- 2805.
- [16] S. Pious Missier, R.L. Babisha Julit, J. Martina Jency, on Totally Ng<sup>#</sup>- Continuous Functions in Neutrosophic Topological Space, Iosr-Jm, 18(1) (2022) 64-68.
- [17] S. Pious Missier, R.L. Babisha Julit ,On Ng<sup>#</sup>– Interior And Ng<sup>#</sup>– Closure in Neutrosophic Topological Space, Proc. Ncagt, (2021)122-133.
- [18] Salama A. A. and Alblowi S. A., Neutrosophic Set and Neutrosophic Topological Spaces, Iosr Jour. Of Mathematics, (2012) 31-35.
- [19] Salama A. A., Florentin Smarandache and Valeri Kroumov, Neutrosophic Closed Set and Neutrosophic Continuous Function, Neutrosophic Sets and Systems, 4 (2014) 4–8.

- [20] Wadei Al-Omeri and Saeid Jafari, On Generalized Closed Sets and Generalized Pre-Closed in Neutrosophic Topological Spaces, Mathematics Mdpi, 7 (2018)01-12.
- [21] Zadeh L. A., Fuzzy Sets, Information and Control, 8 (1965) 338-353.