

Original Article

Modified Domination and Domination Banhatti Indices of Some Chemical Drugs

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Received: 12 July 2023

Revised: 17 August 2023

Accepted: 03 September 2023

Published: 22 September 2023

Abstract - Define the modified domination and domination Banhatti indices of a graph. Here we compute these indices of chloroquine and hydroxychloroquine.

Keywords - Modified domination index, Domination Banhatti index, Chloroquine, Hydroxychloroquine.

Mathematics Subject Classification - 05C10, 05C69.

1. Introduction

The graph $G = (V(G), E(G))$, where $V(G)$ vertex set and $E(G)$ edge set. We refer to [1-3], for other definitions.

Topological indices are numerical values obtained from chemical structures. It is very important to determine topological indices of chloroquine hydroxychloroquine to compare physicochemical properties using QSAR models. Some topological indices were studied in [4-13].

The domination degree $d_d(u)$ of a vertex u in a graph G is defined as the number of minimal dominating sets of G which contains u .

mDM_1 (first modified domination) index is defined as

$$mDM_1(G) = \sum_{uv \in E(G)} \frac{1}{d_d(u) + d_d(v)}$$

mDM_2 (second modified domination) index is defined as

$$mDM_2(G) = \sum_{uv \in E(G)} \frac{1}{d_d(u)d_d(v)}$$

DB_1 (first domination Banhatti) index is defined as

$$DB_1(G) = \sum_{uv \in E(G)} \frac{d_d(u) + d_d(v)}{2}$$

DB_2 (second domination Banhatti) index is defined as

$$DB_2(G) = \sum_{uv \in E(G)} \frac{d_d(u)d_d(v)}{2}$$

DB_3 (third domination Banhatti) index is defined as

$$DB_3(G) = \sum_{uv \in E(G)} \left(\frac{d_d(u) + d_d(v)}{2} \right)^2$$

Some domination indices were studied in [14- 29].

In this paper, we determine the modified domination indices and domination Banhatti indices of some standard graphs, two chemical drugs, chloroquine hydroxychloroquine.

2. Results for Some Standard Graphs

Proposition 1. If K_n it is a complete graph with n vertices, then

- (i) $mDM_1(K_n) = \frac{n(n-1)}{4}$. (ii) $mDM_2(K_n) = \frac{n(n-1)}{2}$. (iii) $DB_1(K_n) = \frac{n(n-1)}{2}$. (iv) $DB_2(K_n) = \frac{n(n-1)}{4}$.
(v) $DB_3(K_n) = \frac{n(n-1)}{2}$.

Proof: If K_n is a complete graph, then $d_d(u) = 1$. From definitions, we have

(i) $mDM_1(K_n) = \frac{n(n-1)}{2} \frac{1}{(1+1)} = \frac{n(n-1)}{4}$.



$$(ii) \quad mDM_2(K_n) = \frac{n(n-1)}{2} \frac{1}{(1 \times 1)} = \frac{n(n-1)}{2}.$$

$$(iii) \quad DB_1(K_n) = \frac{n(n-1)}{2} \left(\frac{1+1}{2}\right) = \frac{n(n-1)}{2}.$$

$$(iv) \quad DB_2(K_n) = \frac{n(n-1)}{2} \frac{(1 \times 1)}{2} = \frac{n(n-1)}{4}.$$

$$(v) \quad DB_3(K_n) = \frac{n(n-1)}{2} \left(\frac{1+1}{2}\right)^2 = \frac{n(n-1)}{2}.$$

Proposition 2. If S_{n+1} is a star graph with $d_d(u) = 1$, then

$$(i) \quad mDM_1(S_{n+1}) = \frac{n}{2}. \quad (ii) \quad mDM_2(S_{n+1}) = n. \quad (iii) \quad DB_1(S_{n+1}) = n. \quad (iv) \quad DB_2(S_{n+1}) = \frac{n}{2}.$$

$$(v) \quad DB_1(S_{n+1}) = n.$$

Proposition 3. If $S_{p+1,q+1}$ is a double star graph with $d_d(u) = 2$, then

$$(i) \quad mDM_1(S_{p+1,q+1}) = \frac{p+q+1}{4}. \quad (ii) \quad mDM_2(S_{p+1,q+1}) = \frac{p+q+1}{4}. \quad (iii) \quad DB_1(S_{p+1,q+1}) = 2(p+q+1).$$

$$(iv) \quad DB_2(S_{p+1,q+1}) = 2(p+q+1). \quad (v) \quad DB_3(S_{p+1,q+1}) = 4(p+q+1).$$

Proposition 4. Let $K_{m,n}$ be a complete bipartite graph with $2 \leq m \leq n$. Then

$$(i) \quad mDM_1(K_{m,n}) = \frac{mn}{m+n+2}, \quad (ii) \quad mDM_2(K_{m,n}) = \frac{mn}{(m+1)(n+1)}$$

$$(iii) \quad DB_1(K_{m,n}) = \frac{mn(m+n+2)}{2}, \quad (iv) \quad DB_2(K_{m,n}) = \frac{mn(m+1)(n+1)}{2}.$$

$$(v) \quad DB_3(K_{m,n}) = \frac{mn(m+n+2)^2}{4}.$$

Proof: Let $G = K_{m,n}$, $m, n \geq 2$ with $d_d(u) = m+1$
 $= n+1$, for all $u \in V(G)$.

From the definition, we have

$$(i) \quad mDM_1(K_{m,n}) = \frac{mn}{m+1+n+1} = \frac{mn}{m+n+2}$$

$$(ii) \quad mDM_2(K_{m,n}) = \frac{mn}{(m+1)(n+1)}$$

$$(iii) \quad DB_1(K_{m,n}) = \frac{mn(m+1+n+1)}{2} = \frac{mn(m+n+2)}{2}.$$

$$(iv) \quad DB_2(K_{m,n}) = \frac{mn(m+1)(n+1)}{2}.$$

$$(v) \quad DB_3(K_{m,n}) = \frac{mn(m+1+n+1)^2}{2^2} = \frac{mn(m+n+2)^2}{4}.$$

3. Results for Chloroquine

Chloroquine is a drug used to prevent and treat malaria. The graph G of chloroquine has 21 atoms and 23 bonds; see Figure 1.

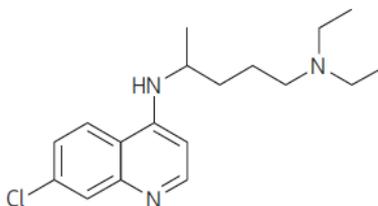


Fig. 1 Chemical structure of chloroquine

From Figure 1, we obtain that $\{(d_d(u), d_d(v)) \mid uv \in E(G)\}$ has 16 bond set partitions.

Table 1. Bond set partitions of chloroquine

$d_d(u), d_d(v) \mid uv \in E(G)$	(216,288)	(216,264)	(216,216)	(324,324)	(297,324)
Number of bonds	2	2	2	4	2
	(240,408)	(240,264)	(144,204)	(246,288)	(144,384)
	1	1	1	1	1
	(288,384)	(216,384)	(216,240)	(240,324)	(216,324)
	1	1	1	1	1
	(216,297)				
	1				

Theorem 1. mDM_1 index of chloroquine is

$$mDM_1(G) = 0.04324746393$$

Proof: From definition,

$$\begin{aligned}
 mDM_1(G) &= \sum_{uv \in E(G)} \frac{1}{d_d(u)+d_d(v)} \\
 &= \frac{2}{216+288} + \frac{2}{216+264} + \frac{2}{216+216} + \frac{4}{324+324} + \frac{2}{297+324} + \frac{1}{240+408} \\
 &+ \frac{1}{240+264} + \frac{1}{144+204} + \frac{1}{246+288} + \frac{1}{144+384} + \frac{1}{288+384} + \frac{1}{216+384} \\
 &+ \frac{1}{216+240} + \frac{1}{240+324} + \frac{1}{216+324} + \frac{1}{216+297} \\
 &= \frac{2}{504} + \frac{2}{480} + \frac{2}{432} + \frac{4}{648} + \frac{2}{621} + \frac{1}{648} + \frac{1}{504} + \frac{1}{348} + \frac{1}{534} + \frac{1}{528} + \frac{1}{672} + \frac{1}{600} \\
 &+ \frac{1}{456} + \frac{1}{564} + \frac{1}{540} + \frac{1}{513} \\
 &= 0.04324746393
 \end{aligned}$$

Theorem 2. mDM_2 index of chloroquine is

$$mDM_2(G) = 0.00034430832$$

Proof: From definition,

$$\begin{aligned}
 mDM_2(G) &= \sum_{uv \in E(G)} \frac{1}{d_d(u)d_d(v)} \\
 &= \frac{2}{216 \times 288} + \frac{2}{216 \times 264} + \frac{2}{216 \times 216} + \frac{4}{324 \times 324} + \frac{2}{297 \times 324} + \frac{1}{240 \times 408} \\
 &+ \frac{1}{240 \times 264} + \frac{1}{144 \times 204} + \frac{1}{246 \times 288} + \frac{1}{144 \times 384} + \frac{1}{288 \times 384} + \frac{1}{216 \times 384} \\
 &+ \frac{1}{216 \times 240} + \frac{1}{240 \times 324} + \frac{1}{216 \times 324} + \frac{1}{216 \times 297} \\
 &= \frac{2}{62208} + \frac{2}{57024} + \frac{2}{46656} + \frac{4}{104976} + \frac{2}{96228} + \frac{1}{97920} + \frac{1}{63360} + \frac{1}{29376} \\
 &+ \frac{1}{70848} + \frac{1}{55296} + \frac{1}{110076} + \frac{1}{82944} + \frac{1}{51840} + \frac{1}{77760} + \frac{1}{69984} + \frac{1}{64152} \\
 &= 0.00034430832
 \end{aligned}$$

Theorem 3. DB_1 index of chloroquine is

$$DB_1(G) = 6283.5$$

Proof: From definition,

$$\begin{aligned}
 DB_1(G) &= \sum_{uv \in E(G)} \frac{d_d(u)+d_d(v)}{2} \\
 &= \frac{2(216+288)}{2} + \frac{2(216+264)}{2} + \frac{2(216+216)}{2} + \frac{4(324+324)}{2} + \frac{2(297+324)}{2} + \frac{1(240+408)}{2} \\
 &+ \frac{1(240+264)}{2} + \frac{1(144+204)}{2} + \frac{1(246+288)}{2} + \frac{1(144+384)}{2} + \frac{1(288+384)}{2} + \frac{1(216+384)}{2} \\
 &+ \frac{1(216+240)}{2} + \frac{1(240+324)}{2} + \frac{1(216+324)}{2} + \frac{1(216+297)}{2} \\
 &= \frac{2(504)}{2} + \frac{2(480)}{2} + \frac{2(432)}{2} + \frac{4(648)}{2} + \frac{2(621)}{2} + \frac{648}{2} + \frac{504}{2} + \frac{348}{2} + \frac{534}{2} + \frac{528}{2} + \frac{672}{2} + \frac{600}{2} \\
 &+ \frac{456}{2} + \frac{564}{2} + \frac{540}{2} + \frac{513}{2} \\
 &= 6283.5
 \end{aligned}$$

Theorem 4. DB_2 index of chloroquine is
 $DB_2(G) = 859296$

Proof: From definition,

$$\begin{aligned}
 DB_2(G) &= \sum_{uv \in E(G)} \frac{d_d(u)d_d(v)}{2} \\
 &= \frac{2(216 \times 288)}{2} + \frac{2(216 \times 264)}{2} + \frac{2(216 \times 216)}{2} + \frac{4(324 \times 324)}{2} + \frac{2(297 \times 324)}{2} + \frac{1(240 \times 408)}{2} \\
 &+ \frac{1(240 \times 264)}{2} + \frac{1(144 \times 204)}{2} + \frac{1(246 \times 288)}{2} + \frac{1(144 \times 384)}{2} + \frac{1(288 \times 384)}{2} + \frac{1(216 \times 384)}{2} \\
 &+ \frac{1(216 \times 240)}{2} + \frac{1(240 \times 324)}{2} + \frac{1(216 \times 324)}{2} + \frac{1(216 \times 297)}{2} \\
 &= \frac{2(62208)}{2} + \frac{2(57024)}{2} + \frac{2(46656)}{2} + \frac{4(104976)}{2} + \frac{2(96228)}{2} + \frac{1(97920)}{2} + \frac{1(63360)}{2} + \frac{1(29376)}{2} \\
 &+ \frac{1(70848)}{2} + \frac{1(55296)}{2} + \frac{1(110076)}{2} + \frac{1(82944)}{2} + \frac{1(51840)}{2} + \frac{1(77760)}{2} + \frac{1(69984)}{2} + \frac{1(64152)}{2} \\
 &= 859206
 \end{aligned}$$

Theorem 5. DB_3 index of chloroquine is
 $DB_3(G) = 1761081.75$

Proof: From definition,

$$\begin{aligned}
 DB_3(G) &= \sum_{uv \in E(G)} \left(\frac{d_d(u)+d_d(v)}{2} \right)^2 = \frac{2(216+288)^2}{4} + \frac{2(216+264)^2}{4} + \frac{2(216+216)^2}{4} + \frac{4(324+324)^2}{4} + \frac{2(297+324)^2}{4} + \\
 &\frac{1(240+408)^2}{4} + \frac{1(240+264)^2}{4} + \frac{1(144+204)^2}{4} + \frac{1(246+288)^2}{4} + \frac{1(144+384)^2}{4} + \frac{1(288+384)^2}{4} + \frac{1(216+384)^2}{4} + \\
 &\frac{1(216+240)^2}{4} + \frac{1(240+324)^2}{4} + \frac{1(216+324)^2}{4} + \frac{1(216+297)^2}{4} \\
 &= \frac{2(504)^2}{4} + \frac{2(480)^2}{4} + \frac{2(432)^2}{4} + \frac{4(648)^2}{4} + \frac{2(621)^2}{4} + \frac{(648)^2}{4} + \frac{(504)^2}{4} + \frac{(348)^2}{4} \\
 &+ \frac{(534)^2}{4} + \frac{(528)^2}{4} + \frac{(672)^2}{4} + \frac{(600)^2}{4} + \frac{(456)^2}{4} + \frac{(564)^2}{4} + \frac{(540)^2}{4} + \frac{(513)^2}{4} \\
 &= 1761081.75
 \end{aligned}$$

4. Results for Hydroxychloroquine

Hydroxychloroquine is another drug which has antiviral activity very similar to that of chloroquine. The graph H of hydroxychloroquine has 22 atoms and 24 bonds, see Figure 2.

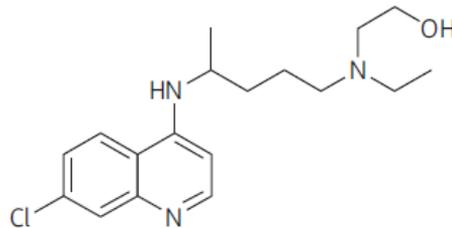


Fig. 2 Chemical structure of hydroxychloroquine

From Figure 2, we obtain that $\{(d_d(u), d_d(v)) \mid uv \in E(H)\}$ has 21 bond set partitions,

Table 2. Edge partition based on the domination degree of end atoms of each bond of hydroxychloroquine

$d_d(u), d_d(v) \mid uv \in E(H)$	(210,350)	(210,425)	(207,324)	(207,567)	(315,317)
Number of bonds	1	1	1	1	1
	(315,385)	(315,420)	(315,425)	(317,340)	(317,385)
	1	2	1	1	1
	(324,324)	(324,459)	(324,567)	(324,621)	(340,486)
	1	1	1	1	1
	(350,385)	(350,595)	(385,420)	(420,425)	(459,486)
	1	1	1	1	3
	(486,567)				
	1				

Theorem 6. mDM_1 index of hydroxychloroquine is
 $mDM_1(H) = 0.03163257708$

Proof: From definition,

$$\begin{aligned}
 mDM_1(H) &= \sum_{uv \in E(H)} \frac{1}{d_d(u)+d_d(v)} \\
 &= \frac{1}{210+350} + \frac{1}{210+425} + \frac{1}{207+324} + \frac{1}{207+567} + \frac{1}{315+317} + \frac{1}{315+385} \\
 &+ \frac{1}{315+420} + \frac{1}{315+425} + \frac{1}{317+340} + \frac{1}{317+385} + \frac{1}{324+324} + \frac{1}{324+459} \\
 &+ \frac{1}{324+567} + \frac{1}{324+621} + \frac{1}{340+486} + \frac{1}{350+385} + \frac{1}{350+595} + \frac{1}{385+420} \\
 &+ \frac{1}{420+425} + \frac{1}{459+486} + \frac{1}{486+567} \\
 &= \frac{1}{560} + \frac{1}{635} + \frac{1}{531} + \frac{1}{774} + \frac{1}{632} + \frac{1}{700} + \frac{2}{735} + \frac{1}{740} + \frac{1}{657} + \frac{1}{702} + \frac{1}{648} \\
 &+ \frac{1}{783} + \frac{1}{991} + \frac{1}{945} + \frac{1}{826} + \frac{1}{735} + \frac{1}{945} + \frac{1}{805} + \frac{1}{845} + \frac{1}{945} + \frac{1}{1053} \\
 &= 0.03163257708
 \end{aligned}$$

Theorem 7. mDM_2 index of hydroxychloroquine is
 $mDM_2(H) = 0.00018036173$

Proof: From definition,

$$\begin{aligned}
 mDM_2(H) &= \sum_{uv \in E(H)} \frac{1}{d_d(u)d_d(v)} \\
 &= \frac{1}{210 \times 350} + \frac{1}{210 \times 425} + \frac{1}{207 \times 324} + \frac{1}{207 \times 567} + \frac{1}{315 \times 317} + \frac{1}{315 \times 385} \\
 &+ \frac{1}{315 \times 420} + \frac{1}{315 \times 425} + \frac{1}{317 \times 340} + \frac{1}{317 \times 385} + \frac{1}{324 \times 324} + \frac{1}{324 \times 459} \\
 &+ \frac{1}{324 \times 567} + \frac{1}{324 \times 621} + \frac{1}{340 \times 486} + \frac{1}{350 \times 385} + \frac{1}{350 \times 595} + \frac{1}{385 \times 420} \\
 &+ \frac{1}{420 \times 425} + \frac{1}{459 \times 486} + \frac{1}{486 \times 567} \\
 &= 0.00018036173
 \end{aligned}$$

Theorem 8. DB_1 index of chloroquine is
 $DB_1(H) = 9406$

Proof: From definition,

$$\begin{aligned}
 DB_1(H) &= \sum_{uv \in E(H)} \frac{d_d(u)+d_d(v)}{2} \\
 &= \frac{210+350}{2} + \frac{210+425}{2} + \frac{207+324}{2} + \frac{207+567}{2} + \frac{315+317}{2} + \frac{315+385}{2} \\
 &+ \frac{2(315+420)}{2} + \frac{315+425}{2} + \frac{317+340}{2} + \frac{317+385}{2} + \frac{324+324}{2} + \frac{324+459}{2} \\
 &+ \frac{324+567}{2} + \frac{324+621}{2} + \frac{340+486}{2} + \frac{350+385}{2} + \frac{350+595}{2} + \frac{385+420}{2} \\
 &+ \frac{420+425}{2} + \frac{3(459+486)}{2} + \frac{486+567}{2} \\
 &= \frac{560}{2} + \frac{635}{2} + \frac{531}{2} + \frac{774}{2} + \frac{632}{2} + \frac{700}{2} + \frac{2 \times 735}{2} + \frac{740}{2} + \frac{657}{2} + \frac{702}{2} + \frac{648}{2} \\
 &+ \frac{783}{2} + \frac{991}{2} + \frac{945}{2} + \frac{826}{2} + \frac{735}{2} + \frac{945}{2} + \frac{805}{2} + \frac{845}{2} + \frac{3 \times 945}{2} + \frac{1053}{2} \\
 &= 9406
 \end{aligned}$$

Theorem 9. DB_2 index of hydroxychloroquine is
 $DB_2(H) = 1814222.5$

Proof: From definition,

$$\begin{aligned}
 DB_2(H) &= \sum_{uv \in E(H)} \frac{d_d(u)d_d(v)}{2} \\
 &= \frac{210 \times 350}{2} + \frac{210 \times 425}{2} + \frac{207 \times 324}{2} + \frac{207 \times 567}{2} + \frac{315 \times 317}{2} + \frac{315 \times 385}{2} \\
 &+ \frac{2(315 \times 420)}{2} + \frac{315 \times 425}{2} + \frac{317 \times 340}{2} + \frac{317 \times 385}{2} + \frac{324 \times 324}{2} + \frac{324 \times 459}{2} \\
 &+ \frac{324 \times 567}{2} + \frac{324 \times 621}{2} + \frac{340 \times 486}{2} + \frac{350 \times 385}{2} + \frac{350 \times 595}{2} + \frac{385 \times 420}{2} \\
 &+ \frac{420 \times 425}{2} + \frac{3(459 \times 486)}{2} + \frac{486 \times 567}{2} \\
 &= 1814222.5
 \end{aligned}$$

Theorem 10. DB_3 index of hydroxychloroquine is

$$DB_3(H) = 3803337$$

Proof: From definition,

$$\begin{aligned} DB_3(H) &= \sum_{uv \in E(H)} \left(\frac{d_d(u) + d_d(v)}{2} \right)^2 \\ &= \frac{(210+350)^2}{4} + \frac{(210+425)^2}{4} + \frac{(207+324)^2}{4} + \frac{(207+567)^2}{4} + \frac{(315+217)^2}{4} + \frac{(315+385)^2}{4} \\ &+ \frac{2(315+420)^2}{4} + \frac{(315+425)^2}{4} + \frac{(317+340)^2}{4} + \frac{(317+385)^2}{4} + \frac{(324+324)^2}{4} + \frac{(324+459)^2}{4} \\ &+ \frac{(324+567)^2}{4} + \frac{(324+621)^2}{4} + \frac{(340+486)^2}{4} + \frac{(350+385)^2}{4} + \frac{(350+595)^2}{4} + \frac{(385+420)^2}{4} \\ &+ \frac{(420+425)^2}{4} + \frac{3(459+486)^2}{4} + \frac{(486+567)^2}{4} \\ &= \frac{560^2}{4} + \frac{635^2}{4} + \frac{531^2}{4} + \frac{774^2}{4} + \frac{632^2}{4} + \frac{700^2}{4} + \frac{2 \times (735)^2}{4} + \frac{740^2}{4} + \frac{657^2}{4} + \frac{702^2}{4} + \frac{648^2}{4} \\ &+ \frac{783^2}{4} + \frac{991^2}{4} + \frac{945^2}{4} + \frac{826^2}{4} + \frac{735^2}{4} + \frac{945^2}{4} + \frac{805^2}{4} + \frac{845^2}{4} + \frac{3 \times (945)^2}{4} + \frac{1053^2}{4}. \\ &= 3803337 \end{aligned}$$

5. Conclusion

Defined modified domination indices and domination Bhanthi indices of a chemical graph and obtained computational values of chemical drugs such as chloroquine, hydroxychloroquine. These values can be useful in planning the effective use of these two chemical drugs in Medical Science.

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